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Investigation of the aerodynamic characteristics of horizontal axis wind turbine using an active flow control method via boundary layer suction

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Abstract: The boundary layer suction (BLS) has the merit of effectively suppressing the formation and development of separation vortices by removing low-momentum fluid occurs on the leading-edge of airfoil suction surface. The present paper numerically investigates the impacts of BLS on the aerodynamic performance of a horizontal axis wind turbine (HAWT). First, the dynamic mode decomposition method is adopted to gain an insight into the improvement mechanism of BLS control by analyzing the flow patterns of a two-dimensional S809 airfoil. Subsequently, the BLS is arranged on a NREL Phase VI reference turbine to study the power increment and flow field characteristics, and the effects of different working angles α_s and momentum coefficients C_μ are investigated at different tip speed ratios (TSRs). The results indicate that the use of BLS control can increase the pressure difference between the suction surface and the pressure surface, raise the peak negative pressure at the leading edge and shift the airfoil flow separation point backwards, and thus effectively enhance the stability of the flow field. Furthermore, the BLS control can significantly improve the power extraction at low to medium TSR if this active device is appropriately implemented on the HAWT.

Keywords: Aerodynamic performance; HAWT; computational fluid dynamics; active control; boundary layer suction

1. Introduction

Low-carbon clean energy technologies can effectively mitigate climate change brought by the use of traditional fossil energy sources, and the large-scale promotion of renewable energy is the key to achieving a low-carbon energy transition [1]. Wind energy is viewed as having great potential in promoting the renewable energy and achieving a low-carbon energy transition due to its large storage capacity, non-pollution and renewable advantages [2-4]. According to the Global Wind Report 2022 [5], cumulative global wind power capacity reached 837 GW. In 2021, 93.6 GW of capacity was installed, showing year-over-year growth of 12%. The global offshore wind market enjoyed its best year ever, with 21.1 GW commissioned, which represents three times more than the previous year. Wind turbines, as the largest rotating machines, convert wind energy into mechanical energy, and thus into electricity [6]. Nowadays, two forms of wind turbines are widely accepted: horizontal axis wind turbines (HAWTs) and vertical axis wind turbines (VAWTs) [7]. Distinguished from VAWT, which started late and lagged behind in research, the HAWT is the mainstream of modern large-scale commercial wind turbines due to its technical maturity and high wind energy utilization coefficient [8]. The flow separation phenomenon that occurs during the operation of wind turbines is an important factor affecting the aerodynamic performance of the wind turbine [9]. The resulting unsteady flow will lead to the fluctuation of aerodynamic load, thus reducing the lifetime of wind turbine blade [10]. Due to the large separation flow and transitional geometry, the root of HAWT blade contributes less to the total power generation than the top of the blade, and the aerodynamic loss is more than half of the total aerodynamic loss of the blade [11].

Therefore, the use of flow control techniques to mitigate separated flows is important for the improvement of aerodynamic performance and lifetime of the blade. Flow separation is usually controlled by passive flow control (PFC) or active flow control (AFC) [12]. PFC and AFC are widely used in aircraft wings [13], wind turbines [14], and turbomachinery [15], etc.

PFC includes vortex generators [16], slots [17], gurney flap [18], movable flaps [19], and serrated trailing edges

44 [20], etc. For PFC, although its structure is simple, it is difficult to adjust with the change of working conditions, so
45 the control efficiency is low. Wang et al. [21] arranged micro-cylinders on the leading edge of HAWT blades to improve
46 the aerodynamic efficiency of wind turbine. They found that setting appropriate micro-cylinders on the leading edge
47 of blades can effectively suppress the flow separation on the wind turbine blades without increasing the wind turbine
48 load. Moshfeghi et al. [22] analyzed the effect of split position on the aerodynamic performance of HAWT under two
49 wind speeds. The results showed that the aerodynamic performance of the blade was very sensitive to the split position
50 and angle at low tip speed ratios, and its sensitivity decreased as the tip speed ratio increased. Zhang et al. [23]
51 investigated the effect of Gurney flaps arranged on the inner part of the blade at 85% chord location of the pressure
52 surface on the aerodynamic performance of the HAWT. The numerical results show that the arrangement of Gurney
53 flaps can increase the power of the wind turbine by 21% and it has a spanwise effect on the outboard part of the blade.

54 Different from PFC, AFC mainly improves the local and even global flow field structure through a small range
55 of energy input, which has a large range of adaptive conditions and good control effect. Common AFC includes
56 synthetic jets [24], plasma actuators [25], constant jets [26], and suction devices [27], etc. Abdulrahim et al. [28]
57 studied the effect of tip injection on rotor performance and near-wake characteristics of a HAWT. The experimental
58 results show that tip injection can effectively increase the power and thrust coefficient, and make the boundary between
59 wake and free flow more diffuse. Aono et al. [29] investigated the effect of dielectric barrier discharge plasma actuator
60 (DBD-PA) installed on the leading edge of HAWT on the flow structure, and found that DBD-PA delays the leading
61 edge separation of the blade by affecting the separated leading edge shear layer. Mohammadi et al. [30] studied the
62 effects of multi air jet blowing on aerodynamic performance and torque of HAWT blades at different velocity ratios.
63 It is found that the jets in blade outer part has the greatest influence on the aerodynamic performance of the wind
64 turbine and can produce the highest torque increment. Shi et al. [31] proposed a new AFC called Co-Flowing Jet (CFJ),
65 and studied it for three-dimensional numerical simulation of HAWT aerodynamic performance. The study shows that
66 the deployment of CFJ on the suction surface of the blade can effectively delay the separation, and the power raised
67 by the wind turbine is much higher than the power consumed by CFJ.

68 The above control forms will change the aerodynamic shape and bring structural resistance. However, HAWT is
69 usually operated at a small angle of attack (AOA), and the jet or the addition of passive control devices may bring
70 adverse effects. While boundary layer suction (BLS) control has good effect in improving aerodynamic efficiency,
71 another important application of BLS control is drag reduction. In 1904, Prandtl [32] initial investigate the BLS as a
72 kind of AFC to control the flow separation occurs on a cylinder. Since then, a number of scholars applied BLS to fluid
73 machines such as aircraft [33], automobiles [34] and wind turbines [38-46].

74 Wang et al. [35] performed suction control on a thin flat plate airfoil at $Re=6.7\times 10^4$, by means of force and velocity
75 field measurements, they found that a suction momentum coefficient of lower than 3% can increase the maximum lift
76 coefficient of this airfoil by about 65% and delay the maximum stall AOA by about 9° in the post stall region. Lei et
77 al. [36] investigated the effect of suction control on the NACA2415 airfoil laminar separation bubble at low Re using
78 a $\gamma-Re_{\theta t}$ transition model and $k-\omega$ turbulence model, and the simulation results showed that the suction control can
79 effectively suppress the flow separation. Meanwhile, the closer the suction position is to the separation bubble and the
80 faster the suction velocity is, the better the control effect is. Arunraj et al. [37] conducted experiments on the
81 effectiveness of airfoil suction control in a wind tunnel and proved that suction control shows better performance at
82 low suction pressures and small AOA, and that maximum lift coefficients can be obtained by performing suction
83 control at 70% of the chord length (c).

84 The aforementioned researches have only investigated suction control in two-dimensional (2D) airfoil sections,
85 which confirmed the value of suction control for effective delayed separation, but have not been applied to whole-
86 machine simulations or considered three-dimensional (3D) effects. Table 1 summarizes some of the significant work

87 published in research on the application of suction control in wind turbines.

88 **Table 1**

89 Study of the application of suction control in wind turbines

References	Type of wind turbine	Method	Contribution
Morgulis et al. [38] 2016	VAWT	Experiment	The VAWT with periodic suction is beneficial to the increase of wind energy utilization coefficient at both high and low wind speeds. The VAWT efficiency can be increased by up to 30% at a low tip velocity ratio maximally.
Rezaeiha et al. [39, 40] 2019	VAWT	CFD (2D)	The suction amplitude of 0.5% is sufficient to inhibit the flow separation on the VAWT surface. The position of the suction slit at the leading edge has better effect.
Rezaeiha et al. [41] 2020	VAWT	CFD (2D)	The dynamic stall can be avoided with minimal suction amplitude when the suction slit is located within the chordal range of the separator bubble. The use of unsteady suction can reduce energy consumption and thus increases net power.
Sun et al. [42] 2020	VAWT	CFD (2D)	At a tip speed ratio of 2.33, a suction control with a momentum coefficient of 0.0075 can increase the VAWT power coefficient by 34.25%.
Sun et al. [43] 2021	VAWT	CFD (2D)	Influenced by the airfoil separation point and the point of maximum curvature, the best suction point moves with the position of the maximum thickness along the chord towards the trailing edge. When the total suction momentum coefficient is kept constant and the suction slit at $0.3c$ from the leading edge of the airfoil, the power coefficients with both suction slits blades are higher than those of single.
Arnold et al. [44] 2018	HAWT	CFD (3D)	A maximum reduction of 2.5 dB in trailing edge noise for a 2% increase in maximum wind turbine power coefficient. Up to 3.2 dB reduction in trailing edge noise when power coefficient is not considered.
Arnold et al. [45] 2018	HAWT	CFD (3D)	When using suction control, the high noise reduction requirements can compromise the aerodynamic performance of the wind turbine.
Moussavi et al.	HAWT	CFD (3D)	With suction slits on the inside of the blades and suction

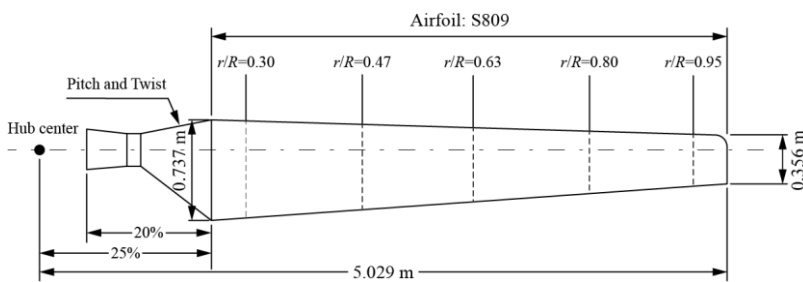
90 For the study of BLS control, most of the studies in wind turbine airfoil and VAWT have been conducted in 2D
 91 methods. However, HAWT has obvious 3D effect [47], and previous results in 2D studies may not be applicable. At
 92 the same time, the few studies on BLS control on HAWT only focus on its excellent noise reduction performance, or
 93 analyze its control effect under a single tip speed ratio (TSR). Different from previous studies, in this research, the
 94 dynamic mode decomposition method is firstly adopted to decompose the airfoil with BLS, and analyze the mode and
 95 characteristic value unit circle of each order of the flow field to gain an insight into the mechanism of BLS. Then, we
 96 studied the power increment effect of BLS arranged at $0.15c$ from the leading edge on HAWT under four TSR, and
 97 comprehensively evaluated the BLS control by analyzing the flow field morphology and start-up parameters under the
 98 consideration of the energy consumption of BLS. Finally, the effect of BLS working angle on its performance is
 99 analyzed. Under the trend of wind turbine shifting from onshore to offshore and from miniaturization to large-scale, it
 100 is no longer satisfied to use PFC to perform flow control. BLS control, as a mature flow control technique of AFC, has
 101 achieved good results in the field of aviation, so it's very necessary for its application research in HAWT. BLS control
 102 is expected to become an effective means to control flow separation of HAWT blades. In this context, the application
 103 of BLS in HAWT is completely studied in this paper, in order to provide a certain theoretical basis for the application
 104 of BLS in HAWTs.

105

106 2. Method and verification

107 2.1 Geometric model and main aerodynamic parameters

108 A series of experiments of wind turbine developed and tested by the National Renewable Energy Laboratory
 109 (NREL) in the NASA Ames wind tunnel (with a $120\text{ m} \times 80\text{ m}$ closed test section) are widely accepted. Among them,
 110 NREL Phase VI HAWT, as one of the experiments providing the most comprehensive data, has been used by a large
 111 number of researchers [48-50]. Therefore, the NREL Phase VI HAWT blade is used as the basic model in this research.
 112 The wind turbine has a diameter of 10.058 m and a rated power of 19.8 kW [51-53]. The model uses the S809 airfoil
 113 at all span positions except for the root ($0\text{-}1.257\text{ m}$). After 25% span, the torsion is zero. Table 2 shows details of the
 114 geometrical parameters of the wind turbine under study and Fig.1 shows the parameters of blade model.



(a) Parameters of the blade model.



(b) HAWT in NASA wind tunnel [51]

Fig.1. Parameters of NREL Phase VI wind turbine blade model.

Table 2

Geometrical parameters of the NREL Phase VI wind turbine

Property [Symbol]	Unit	Value
Rated power [P_R]	kW	19.8
Cut-in wind speed [V_{in}]	m/s	5
Cut-out wind speed [V_{out}]	m/s	25
Rotor diameter [D_r]	m	10.058

115

116

Hub height [H_r]	m	12.192
Cone angle [α_c]	°	0
Pitch angle [β]	°	5

117 In this experiment, through the variable-speed control of fans and the variable-pitch control of fan blade, the
118 velocities in the test section can be accurately controlled from 0 m/s to 50 m/s. The rotor operates at a nominal 72
119 RPM. The time-series measurements for this test were obtained by the NREL data system, which was limited by
120 experimental uncertainty. Among them, the uncertainty of velocity measurement is about 1%, while for the pressure
121 measurement can be estimated as 0.05%, among which the wall pressure is 0.03%. In addition, the turbine blockage
122 was found to be less than 1%.

123

124 2.2 BLS model

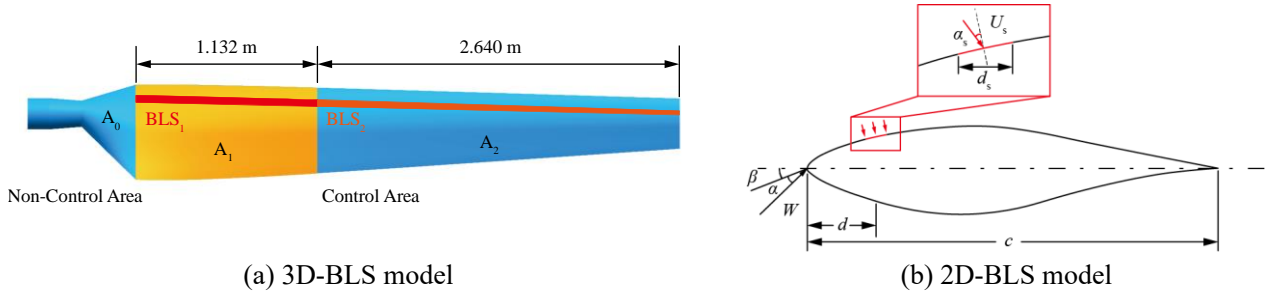


Fig.2. The 3D-BLS model and 2D-BLS blade section model.

125 Modeling of the clean blade and BLS blade by using UG NX12.0, layout of BLS from the 25% span. The control
126 area is divided into two parts, A_1 (root of the blade) in the first 1.132 m and A_2 (middle and tip of the blade) in the
127 second 2.640 m. The 3D-BLS model and 2D-BLS blade section model are shown in Fig.2. In the figure, α_s is the
128 working angle of the BLS, °; d_s is the width of the BLS, m; U_s is the velocity of the BLS, m/s; d is the distance of the
129 BLS from the leading edge, m; c is the chord length of airfoil at this section, m. It is worth noting that the BLS width
130 narrows as the chord length of the spreading section decreases, but possesses a constant ratio of $0.02c$.

131 The suction momentum coefficient (C_{μ}) is chosen as a parameter to measure the quantification of suction control,
132 which is defined as:

$$C_{\mu} = 2\dot{m}V_R / \rho_{\infty}U_{\infty}c \quad (1)$$

133 where \dot{m} is the mass flow rate of BLS working gas, kg/s and the V_R is the velocity ratio, which is defined as:

$$\dot{m} = A_s \cdot U_s \cdot \rho_s \quad (2)$$

$$V_R = U_s / U_{\infty} \quad (3)$$

134 where A_s is the area of the BLS, m^2 ; ρ_s is the density of the working gas, kg/m^3 .

135 As a type of AFC, this research introduces energy consumption (P_{BLS}) as a measure of loss, which is defined as:

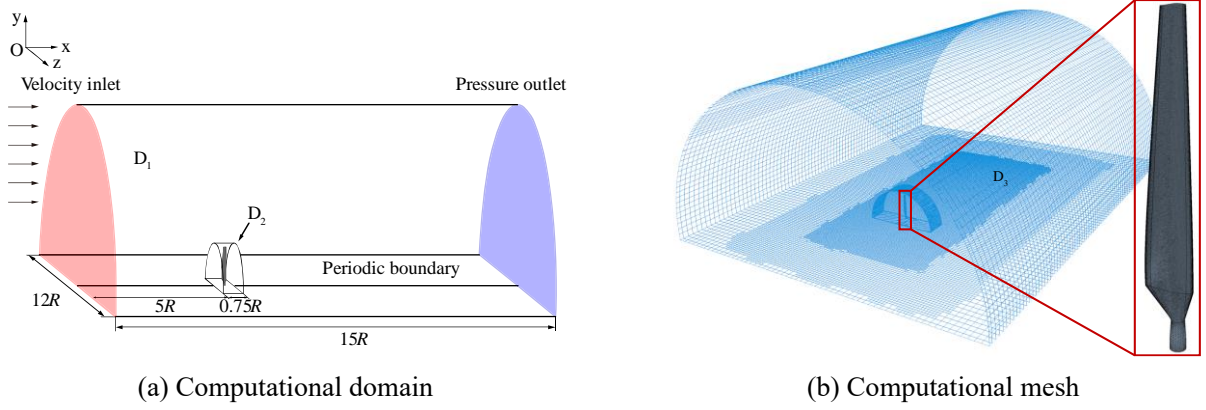
$$P_{BLS} = \frac{\dot{m}c_p T_s}{\eta_s} \left[\left(\frac{P_{\infty}}{P_s} \right)^{\frac{\gamma-1}{\gamma}} - 1 \right] \quad (4)$$

136 where c_p is the constant pressure specific heat capacity, $kJ/(kg \cdot K)$; T_s is the total temperature of the BLS, which is
137 298.15 K; η_s is the efficiency of pump, which is 80%; p_s is the total pressure of the BLS, Pa; γ is the ratio of specific
138 heat, which is 1.4.

139

140 3 Computational and numerical method

141 3.1 Computational domain and meshing



142 **Fig.3.** Computational domain and mesh of the wind turbine.

143 The grid and boundary conditions of wind turbine computing domain are shown in Fig.3. The computational
 144 domain is divided into three sub-domains: the Background zone (D_1), the Rotating zone (D_2), and the Overset refine
 145 zone (D_3). The mesh density of D_2 and D_3 is higher than the other zones, allowing for more accurate aerodynamic
 146 performance calculations and obtaining more precise details of the captured flow field.

147 The left side of Fig.3a (light red area) is the velocity inlet, and the velocity flow is parallel to $x+$; the right side
 148 (light blue area) is the pressure outlet with a gauge pressure of 0 Pa; rotational periodic boundary conditions are used
 149 for the symmetry plane; and no-slip boundary conditions are used for the blade surface. As NREL Phase VI wind
 150 turbine has two blades, the model and flow field are periodic, the simulation is carried out for a single blade to reduce
 151 computational costs. The rotating speed of the wind rotor is fixed at about 7.2 rad/s. In all simulations, air is assumed
 152 to be an incompressible fluid with density $\rho_{\infty}=1.185 \text{ kg/m}^3$ and dynamic viscosity $\mu_{\infty}=1.855 \times 10^{-5} \text{ Pa}\cdot\text{s}$.

153 3.2 Numerical method

154 In order to simulate the flow field around a HAWT blade, the selection of a suitable turbulence model is essential.
 155 For the NREL Phase VI HAWT, the selection of a turbulence model has been studied in depth and detail by many
 156 researchers. Jones et al. [54] believed that the $k-\varepsilon$ model had a good performance in calculating the free flow region
 157 (outside the boundary layer). Wilcox [55] demonstrated that the $k-\omega$ model has good performance in dealing with
 158 internal boundary layer by combining numerical calculation with singular disturbance. However, for HAWT, the $k-\omega$
 159 and $k-\varepsilon$ models cannot simulate the flow around the HAWT blade well due to the large-scale flow separation at the
 160 blade root during stall [56-58]. The SST $k-\omega$ model proposed by Menter [59] in 1994 used the $k-\omega$ model at the near-
 161 wall and the $k-\varepsilon$ model outside the boundary layer. Tachos et al. [60] compared four turbulence models, which
 162 concluded that the SST $k-\omega$ model is more suitable for simulating NREL Phase VI HAWT. Meanwhile, other
 163 researchers also reached similar conclusions [58, 61], this is why the SST $k-\omega$ turbulence model is adopted in this
 164 research for simulation.

165 For the SST $k-\omega$ turbulence model, its k and ω are defined as:

$$\frac{\partial}{\partial x_i}(\rho u_i u_j) = -\frac{\partial}{\partial x_i}(\mu_k \frac{\partial k}{\partial x_i}) + P_k - \rho \beta^* k \omega \quad (5)$$

$$\frac{\partial}{\partial x_i}(\rho \omega u_i) = \frac{\partial}{\partial x_i}(\mu_\omega \frac{\partial \omega}{\partial x_i}) + \frac{\alpha}{v_i} P_k - \rho \beta^* \omega^2 + 2(1-F_1) \rho \frac{\sigma_{\omega,2}}{\omega} \frac{\partial k}{\partial x_i} \frac{\partial \omega}{\partial x_i} \quad (6)$$

166 where μ_k and μ_ω are the effective diffusivities for the turbulent kinetic energy and specific dissipation rate, respectively.

167 To improve the accuracy of the results, unsteady assumptions are used for the simulations. The discretization
 168 method adopts the second order upwind scheme. The simulated time step is set as $T/360$, corresponding to the time
 169 that the HAWT rotates by 1° ($\pi/180$). For better convergence, internal iteration of 10 for clean blade and 25 for BLS
 170 blade are selected. The convergence of the simulation is checked by monitoring momentum residuals less than 10^{-5} .
 171 In addition, the simulation stops when the difference between the average torque value in the current rotation period
 172 and the previous rotation period is less than 3%, and the data used below are the average values of the last rotation
 173 period.

174

175 4. Validation

176 4.1 Grid independence validation

177 During the computational fluid dynamics (CFD) calculations, the study of grid independence is indispensable.
 178 The Grid Convergence Index (GCI) method proposed by Roache in 1994 is still the common method used today to
 179 assess truncation errors [62]. According to the suggestions, we checked by the total number of units (N), with the
 180 refinement factors all greater than 1.3. The specific process is as follows:

181 First define l_g as the grid size:

$$l_g = \left[\frac{1}{N_g} \sum_{i=1}^{N_g} (\Delta V_i) \right]^{\frac{1}{3}} \quad (7)$$

182 where ΔV_i is the volume of each grid cell; N_g is the total number of ΔV_i units used for calculation, which N_1 is for Fine
 183 mesh, N_2 is for Medium mesh and N_3 is for Coarse mesh.

184 The refinement factor (f) between different grids is defined as:

$$f_{g+1,g} = \frac{l_{g+1}}{l_g} \quad (8)$$

185 The torque of the HAWT is taken as the key variable and defined as φ_g , and then the difference $\varepsilon_{g+1,g}$ of two
 186 similar φ is obtained:

$$\varepsilon_{g+1,g} = \varphi_{g+1} - \varphi_g \quad (9)$$

187 Then the relative error $e_{g+1,g}$ is obtained:

$$e_{g+1,g} = \left| \frac{\varepsilon_{g+1} - \varepsilon_g}{\varepsilon_g} \right| \quad (10)$$

188 Calculate the estimate of GCI, which is defined as follows:

$$GCI_{g+1,g} = F_s \frac{e_{g+1,g}}{f_{g+1,g}^p - 1} \quad (11)$$

189 where F_s is the safety factor, which is suggested in literature [63] to be in the range of 1.25-3.00, and 1.25 is selected
 190 in this research. Besides, p is the apparent order, which is defined as:

$$p = \frac{|\ln |\varepsilon_{32} / \varepsilon_{21}| + q(p)|}{\ln(f_{21})} \quad (12)$$

191 Since f is a constant in this research, $q(p)=0$.

192 Table 3 shows the GCI calculations for three grids (Fine, Medium and Coarse) under three different incoming

193 wind speeds (10 m/s, 13 m/s, 15 m/s).

194

Table 3

GCI assessment at different incoming wind speeds

Parameters	Value		
	$U_\infty=10$ m/s	$U_\infty=13$ m/s	$U_\infty=15$ m/s
N_1	4894310	4894310	4894310
N_2	3516274	3516274	3516274
N_3	2634810	2634810	2634810
f_{32}	1.49	1.49	1.49
f_{21}	1.49	1.49	1.49
φ_1	663.930	1280.125	1044.752
φ_2	661.449	1274.388	1043.219
φ_3	630.588	1259.216	1023.541
ε_{32}	-30.861	-15.172	-19.678
ε_{21}	-2.481	-5.737	-1.533
F_s	1.25	1.25	1.25
e_{32}	4.66567%	1.19053%	1.88628%
e_{21}	0.03266%	0.27177%	0.01240%
GCI_{32}^{Medium}	0.50984%	0.90489%	0.19921%
GCI_{21}^{Fine}	0.04083%	0.34063%	0.01550%

196 It can be seen that the convergence of the three grids (N_1 , N_2 , N_3) is monotonically decreasing for all three
 197 incoming wind speeds. The specific performance is 0.510% and 0.041% for GCI_{32}^{Medium} and GCI_{21}^{Fine} under $U_\infty=10$
 198 m/s, respectively; 0.905% and 0.341% under $U_\infty=13$ m/s, respectively; 0.199% and 0.016% under $U_\infty=15$ m/s,
 199 respectively. And the maximum value of GCI_{21}^{Fine} is 0.341%, which is less than 1% and has good convergence. This
 200 means that the Medium mesh is already sufficiently accurate and increasing the amount of mesh is a very small
 201 improvement in accuracy. Therefore, Medium mesh is selected as the computational mesh in this research.

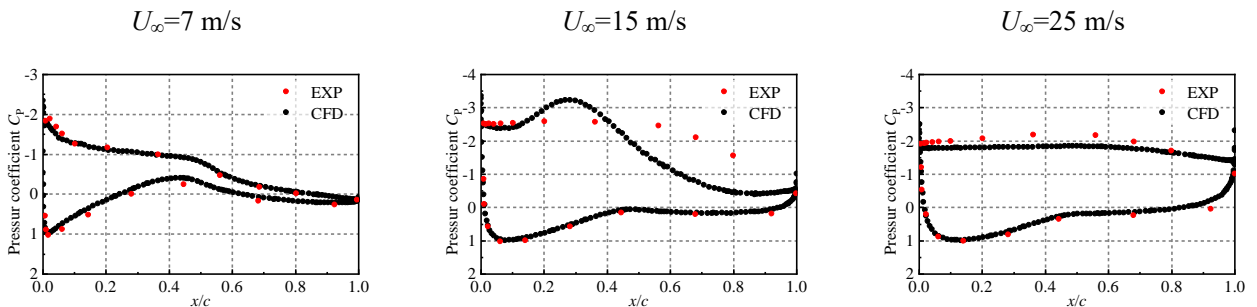
202

203 4.2 Pressure coefficient validation

204 The pressure coefficient (C_p) of the blade cross section along the spanwise direction is defined as:

$$C_p = \frac{2(p_0 - p_\infty)}{\rho_\infty (U_\infty^2 + (r\omega)^2)} \quad (13)$$

205 where p_0 is the surface pressure, Pa; p_∞ is the flow pressure, Pa; U_∞ is the incoming flow speed, m/s; r is the radial
 206 distance of local spanwise station, m; ω is the angular velocity of the rotor, rad/s.



(a) $r/R=0.30$

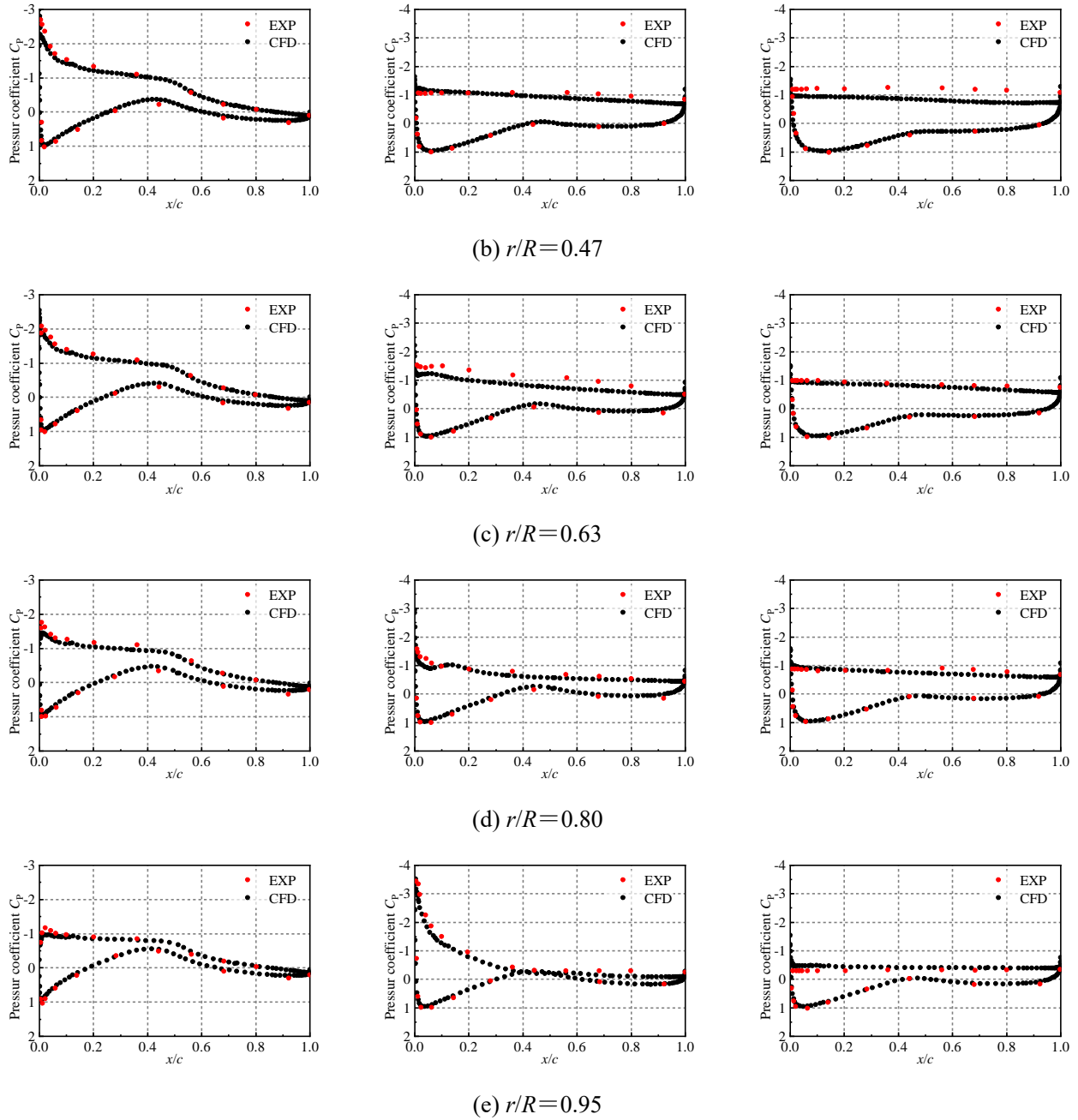


Fig.4. Pressure coefficient compared with experiment.

207 Since the experimental incoming flow speed ranges from 5 m/s to 25 m/s, according to its given data, this research
 208 selects representative surface pressure coefficients of five blade sections under three U_∞ for comparison. At a U_∞ of 15
 209 m/s and $r/R=0.30$, our results appear to deviate from the estimate of the pressure coefficient on the suction surface,
 210 with a good pressure surface match. This should be due to the fact that our results overestimate the stall at the leaf root
 211 when $U_\infty=15$ m/s and its effect on the aerodynamic properties of the blade. Similar results exist in previous calculations
 212 by other researchers [64, 65, 49].

213 In addition, the pressure coefficients at $r/R=0.30, 0.47, 0.63, 0.80$ and 0.95 when the $U_\infty=7$ m/s, 15 m/s and 25
 214 m/s are in high agreement with the experimental values. This indicates that the turbulence model selection and meshing
 215 in this research have high accuracy.

216
 217 *4.3 Torque validation*

218 An important factor in assessing the aerodynamic performance of a wind turbine is the torque (T), which is defined
 219 as:

$$T = \rho_{\infty} A U_d (U_{\infty} - U_w) \quad (14)$$

220 where A is the swept area of wind turbine, m^2 ; U_d is the axial velocity of flow through the wind turbine, m/s ; U_w is the
 221 downstream speed of wind turbine, m/s .

222 Output power of wind turbine (P) can be calculated by torque:

$$P = T U_d \quad (15)$$

223 Further define the power coefficient (C_p) as:

$$C_p = \frac{2P}{\rho_{\infty} A U_{\infty}^3} \quad (16)$$

224 The relative error is calculated as follows:

$$E = \frac{T_{Exp} - T_{Cal}}{T_{Exp}} \times 100 \quad (17)$$

225 where T_{Exp} is the torque of the experiment; T_{Cal} is the torque calculated by CFD.

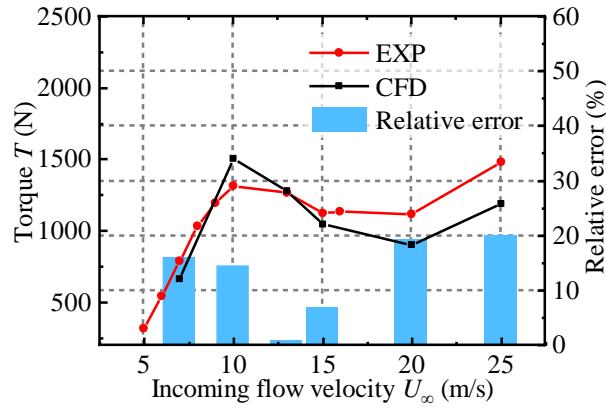


Fig.5. Comparison of experimental and CFD result of torque

226 Fig.5 shows a comparison of the torque curves between the EXP data and the CFD results. As can be seen from
 227 the figure, there is a high degree of similarity between our results and the experimental results, and the relative errors
 228 are all less than 20%. This indicates that our calculations can accurately predict the power of the wind turbine under
 229 various stall conditions (pre-stall, stall, and post-stall). The highest degree of agreement is found when $U_{\infty}=13$ m/s ,
 230 where the relative error is only 0.74%. Besides, since the blade pitch system will operate at high wind speeds, this
 231 research chooses to analyze the blade controlled by BLS when $U_{\infty}=7, 10, 13$ and 20 m/s . TSR and relative velocity of
 232 each section of selected U_{∞} are shown in Table 4.

233 **Table 4**

234 TSR and relative velocity of each section at different incoming wind speeds

Incoming wind speeds (m/s)	TSR	Relative velocity (m/s)				
		$r/R=0.30$	$r/R=0.47$	$r/R=0.63$	$r/R=0.80$	$r/R=0.95$
7	5.4	13.36	19.15	24.89	31.13	36.70
10	3.8	15.15	20.44	25.90	31.94	37.38
13	2.9	17.27	22.06	27.20	33.00	38.30
20	1.9	23.01	26.79	31.16	36.33	41.20

235 The TSR of HAWT blade is a very important parameter for expressing the wind turbine characteristics, which is
 236 defined as:

$$\lambda = \frac{\omega R}{U_\infty} \quad (18)$$

237 where R is the rotor radius, m.

238

239 **5. Results and discussions**

240 *5.1 Dynamic mode decomposition analysis of the S809 airfoil with BLS control*

241 The flow field mode decomposition method is an analytical method that extracts the main features of the flow
242 field and simplifies it. Typical methods of flow field mode analysis are the principal orthogonal decomposition (POD)
243 and the dynamic mode decomposition (DMD) [66].

244 The DMD algorithm is based on a linear operator that best fits the dynamic properties of the flow field,
245 decomposing the flow field into a number of modes with a single characteristic frequency and growth/decay rate.
246 Therefore, DMD can obtain the contribution of different frequency flow structure to the flow field.

247 For an in-depth analysis of the BLS control mechanism, a DMD analysis of the 2D BLS airfoil is first carried out.
248 It takes the section at 75% span, where the line length c is 0.483 m, under a relative velocity of 29.29 m/s. The BLS is
249 arranged at $0.15c$ from the leading edge of the airfoil with $C_\mu=0.01$.

250 For flow field variable information, assume that there exists a matrix A such that there is a linear mapping between
251 adjacent time layers \mathbf{u}_{i+1} and \mathbf{u}_i .

$$\mathbf{u}_{i+1} = A\mathbf{u}_i \quad (19)$$

252 Defining $\boldsymbol{\psi}_0 = [\mathbf{u}_1, \mathbf{u}_2, \dots, \mathbf{u}_{N-1}]$, $\boldsymbol{\psi}_1 = [\mathbf{u}_2, \mathbf{u}_3, \dots, \mathbf{u}_N]$, the following relation can be given:

$$\boldsymbol{\psi}_1 = A\boldsymbol{\psi}_0 = [A\mathbf{u}_1, A\mathbf{u}_2, \dots, A\mathbf{u}_{N-1}] \quad (20)$$

253 For a matrix with rank r_m , usually A is a high dimensional matrix with a large amount of data. The purpose of
254 DMD algorithm is to replace A with a low dimensional optimization approximation matrix \tilde{A} , so that:

$$A = U\tilde{A}U^H \quad (21)$$

255 where \tilde{A} is a square matrix of order r , and U can be obtained by singular value decomposition.

256 Perform a singular value decomposition of $\boldsymbol{\psi}_0$:

$$\boldsymbol{\psi}_0 = USV^H \quad (22)$$

257 where U is a $M \times r_m$ left orthogonal matrix; S is a $r_m \times r_m$ singular value diagonal matrix; V is a $r_m \times N$ right orthogonal
258 matrix; the superscript H denotes the complex conjugate transpose, which in turn leads to the approximation matrix:

$$A \approx \tilde{A} = U^H \boldsymbol{\psi}_1 V S^{-1} \quad (23)$$

259 The DMD mode is defined as follows:

$$\boldsymbol{\varphi}_i = \boldsymbol{\psi}_1 V S^{-1} \mathbf{y}_i \quad (24)$$

260 where \mathbf{y}_i is the eigenvector of the low-dimensional approximation matrix \tilde{A} .

261 The eigenvalues and eigenvectors of the matrix S are given by Eq. (22) as:

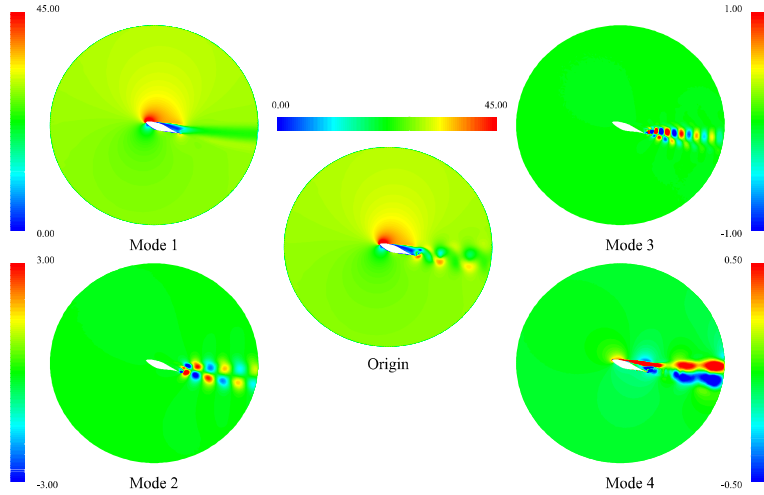
$$S\mathbf{y}_i = \mu_i \mathbf{y}_i \quad (25)$$

262 where μ_i is a complex number, its real part expresses the growth rate of the corresponding mode and the imaginary
263 part contains the frequency information.

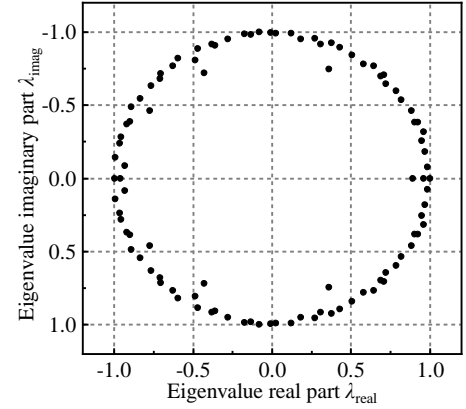
264 When performing stability analysis of modes, a positive growth rate indicates that the corresponding mode is

265 unstable, a negative growth rate indicates that the corresponding mode is stable and a zero growth rate indicates that
 266 the corresponding mode is periodic. This method allows for a quantitative determination of the stability of a mode.

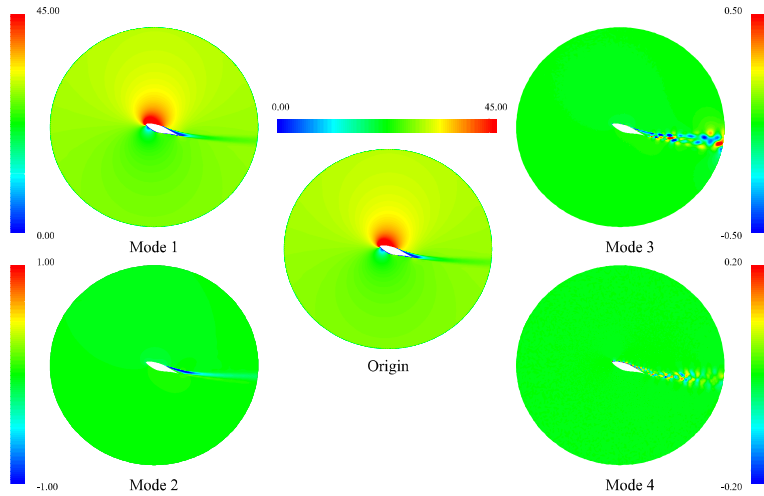
267 Another way of determining stability is to observe the distribution of eigenvalues on the unit circle, with the
 268 horizontal axis being the real part of the eigenvalue and the vertical axis being the imaginary part of the eigenvalue. If
 269 the eigenvalue corresponds to a point outside the unit circle, then its magnification is positive, corresponding to an
 270 unstable mode; if the eigenvalue corresponds to a point inside the unit circle, then its magnification is negative,
 271 corresponding to a stable mode; if the eigenvalue corresponds to a point on the unit circle, then the magnification is
 272 zero, corresponding to a periodic mode.



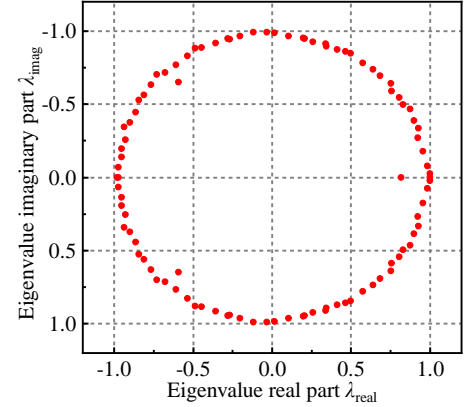
(a) Mode of clean airfoil



(b) Eigenvalue of clean airfoil



(c) Mode of BLS airfoil



(d) Eigenvalue of BLS airfoil

Fig.6. Mode and the eigenvalue of clean airfoil and BLS airfoil.

273 As can be seen in Fig.6a and 6c, at an AOA of 20° , the clean airfoil shows alternating vortex shedding at the
 274 trailing edge. The Mode 1 reflects the mean flow field and shows a large stall area at the suction surface of the clean
 275 airfoil, while the BLS airfoil shows a significantly reduced stall area due to the better fluid attachment at the suction
 276 surface by inhaling low-momentum fluid in the boundary layer. The main structure of Mode 2 is found in the trailing
 277 edge and trailing area: the fluctuating structure of Mode 2 of the clean airfoil forms a bilayer structure with upper and
 278 lower symmetry in the trailing area; Mode 2 of the BLS airfoil is mainly found in the small stall area at the trailing
 279 edge. Mode 3 and 4 are small-scale complex flows captured by the DMD. Obviously, the fluctuation range and
 280 amplitude of BLS airfoil are much smaller than that of clean airfoil.

281 Further observe the distribution of the characteristic values of clean airfoil and BLS airfoil on the unit circle. As

282 seen in Fig.6b and 6d, clean airfoil has 5 pairs of characteristic values outside the unit circle, while BLS airfoil only
 283 has 3 pairs. Compared with clean airfoil, the characteristic values of BLMS airfoil are closer to the unit circle, which
 284 indicates that BLMS control can effectively increase the stability of flow field.

285

286 *5.2 Effect of different momentum coefficients on power increment*

287 Fixing the position of BLS control at $0.15c$ from the leading edge, we simulated the improvement of BLS control
 288 on the work capacity of HAWT with different momentum coefficients at four incoming wind speeds ($U_\infty=7, 10, 13$ and
 289 20 m/s). For each incoming wind speed, 12 cases are set and the results are as follows.

290 Define P_{BLS_Net} as the power increment after considering the BLS energy consumption:

$$P_{BLS_Net} = P - P_{Clean} - P_{BLS} \quad (26)$$

291 where P_{Clean} is the power of clean blade, W.

292

Table 5

293

Power increment and BLS energy consumption of blades at different C_μ under $U_\infty=7$ m/s

Case	C_μ of BLS ₁	C_μ of BLS ₂	Power P (W)	Power increment ΔP (W)	P_{BLS} (W)	P_{BLS_Net} (W)
L1	0.04	0.00	2566.05	72.45	92.30	-19.85
L2	0.09	0.00	2598.80	105.19	138.45	-33.26
L3	0.16	0.00	2637.23	143.63	184.60	-40.97
L4	0.00	0.04	2923.39	429.79	221.33	208.46
L5	0.00	0.09	3039.26	545.65	332.00	213.66
L6	0.00	0.16	3174.42	680.82	442.66	238.16
L7	0.01	0.01	2821.12	327.52	156.82	170.71
L8	0.02	0.02	2896.93	403.33	221.77	181.56
L9	0.04	0.04	3014.60	520.99	313.63	207.36
L10	0.09	0.09	3163.38	669.77	470.44	199.33
L11	0.16	0.16	3308.91	815.31	627.26	188.05
L12	0.25	0.25	3462.14	968.53	784.07	184.46

294

Table 6

295

Power increment and BLS energy consumption of blades at different C_μ under $U_\infty=10$ m/s

Case	C_μ of BLS ₁	C_μ of BLS ₂	Power P (W)	Power increment ΔP (W)	P_{BLS} (W)	P_{BLS_Net} (W)
S1	0.04	0.00	5870.09	200.92	240.60	-39.68
S2	0.09	0.00	5949.42	280.25	360.90	-80.65
S3	0.16	0.00	6038.04	368.87	481.20	-112.33
S4	0.00	0.04	6256.11	586.94	562.66	24.28
S5	0.00	0.09	6580.81	911.63	843.99	67.65
S6	0.00	0.16	6980.39	1311.22	1125.32	185.90
S7	0.01	0.01	7053.40	1384.22	401.63	982.59
S8	0.02	0.02	7251.30	1582.12	567.96	1014.17
S9	0.04	0.04	7500.69	1831.52	803.26	1028.26
S10	0.09	0.09	7847.85	2178.68	1204.89	973.79
S11	0.16	0.16	8216.73	2547.56	1606.51	941.05

S12 0.25 0.25 8612.87 2943.70 2008.14 935.55

296 Table 5-6 show the energy increment and BLS energy consumption of blades at different C_{μ} under $U_{\infty}=7$ m/s and
 297 10 m/s. As can be seen from Table 5, under $U_{\infty}=7$ m/s, BLS control has a very weak power increment effect of blade,
 298 and the maximum improvement is only about 230 W. And when only BLS₂ works, the power increment is greater than
 299 when BLS₁ and BLS₂ work at the same time. When the C_{μ} of BLS₂ is 0.16, the P_{BLS_Net} is highest at 238.16 W.

300 As can be seen from Table 6, when BLS₁ works and BLS₂ shuts down, its effect on power increment of blade is
 301 limited. After taking into account BLS energy consumption, the gain is negative. Interestingly, as the momentum
 302 coefficient increases, its negative gain increases. When BLS₁ shut down and BLS₂ works, it has obvious effect on
 303 power increment of blade. After taking into account the P_{BLS} , the gain is still positive. At this point, with the increase
 304 of momentum coefficient, its power increment increases. However, when both BLS₁ and BLS₂ work, the blade power
 305 is significantly increased and the amount of increment is not simply superimposed, but a greater increment. While
 306 higher C_{μ} has a higher power increment, it also comes with a higher P_{BLS} . When the C_{μ} of BLS₁ and BLS₂ is 0.04, the
 307 $\Delta P - P_{BLS}$ is highest at 1028.26 W.

308 **Table 7**

309 Power increment and BLS energy consumption of blades at different C_{μ} under $U_{\infty}=13$ m/s

Case	C_{μ} of BLS ₁	C_{μ} of BLS ₂	Power P (W)	Power increment ΔP (W)	P_{BLS} (W)	P_{BLS_Net} (W)
M1	0.04	0.00	5375.45	571.12	320.80	250.32
M2	0.09	0.00	4355.58	-448.74	450.41	-899.16
M3	0.16	0.00	4386.67	-417.66	600.5	-1018.21
M4	0.00	0.04	7331.73	2527.40	765.29	1762.12
M5	0.00	0.09	8886.39	4082.06	1147.93	2934.13
M6	0.00	0.16	10866.26	6061.93	1530.58	4531.35
M7	0.16	0.16	14567.93	9763.60	2131.13	7632.47
M8	0.25	0.25	15565.32	10760.99	2663.91	8097.08
M9	0.36	0.36	16420.04	11615.71	3196.70	8419.02
M10	0.49	0.49	17263.90	12459.57	3729.48	8730.10
M11	0.64	0.64	17020.57	12216.24	4262.26	7953.98
M12	0.81	0.81	16621.29	11816.96	4795.04	7021.92

310 **Table 8**

311 Power increment and BLS energy consumption of blades at different C_{μ} under $U_{\infty}=20$ m/s

Case	C_{μ} of BLS ₁	C_{μ} of BLS ₂	Power P (W)	Power increment ΔP (W)	P_{BLS} (W)	P_{BLS_Net} (W)
H1	0.04	0.00	4550.28	1162.13	505.26	656.88
H2	0.09	0.00	4216.15	828.01	757.88	70.12
H3	0.16	0.00	4034.83	646.69	1010.51	-363.83
H4	0.00	0.04	6023.16	2635.01	1181.58	1453.43
H5	0.00	0.09	6918.21	3530.07	1772.38	1757.69
H6	0.00	0.16	7513.90	4125.76	2363.17	1762.59
H7	0.16	0.16	8755.05	5366.91	3373.68	1993.23
H8	0.25	0.25	12195.51	8807.37	4217.10	4590.27
H9	0.36	0.36	16090.80	12702.66	5060.52	7642.14
H10	0.49	0.49	16594.22	13206.07	5903.94	7302.13

H11	0.64	0.64	17014.23	13626.09	6747.36	6878.73
H12	0.81	0.81	17398.78	14010.64	7590.78	6419.86

312 Table 7-8 show the energy increment and BLS energy consumption of blades at different C_{μ} under $U_{\infty}=13$ m/s
313 and 20 m/s. The results obtained under $U_{\infty}=13$ m/s and 20 m/s (Low to medium TSR) are similar to that under $U_{\infty}=7$
314 m/s and 10 m/s (High TSR). The difference is that the power increment to the blades with BLS control at low to
315 medium TSR is much greater than that at high TSR. Under $U_{\infty}=13$ m/s, when the C_{μ} of BLS₁ and BLS₂ is 0.49, the
316 power of clean blade which is 4804.33 W can be increased by 12459.57 W with BLS control. After considering the
317 P_{BLS} , the increment is still 8730.10 W. Under $U_{\infty}=20$ m/s, when the C_{μ} of BLS₁ and BLS₂ is 0.36, the power of clean
318 blade which is 3388.14 W can be increased by 16090.80 W with BLS control. After considering the P_{BLS} , the increment
319 is still 7642.14 W.

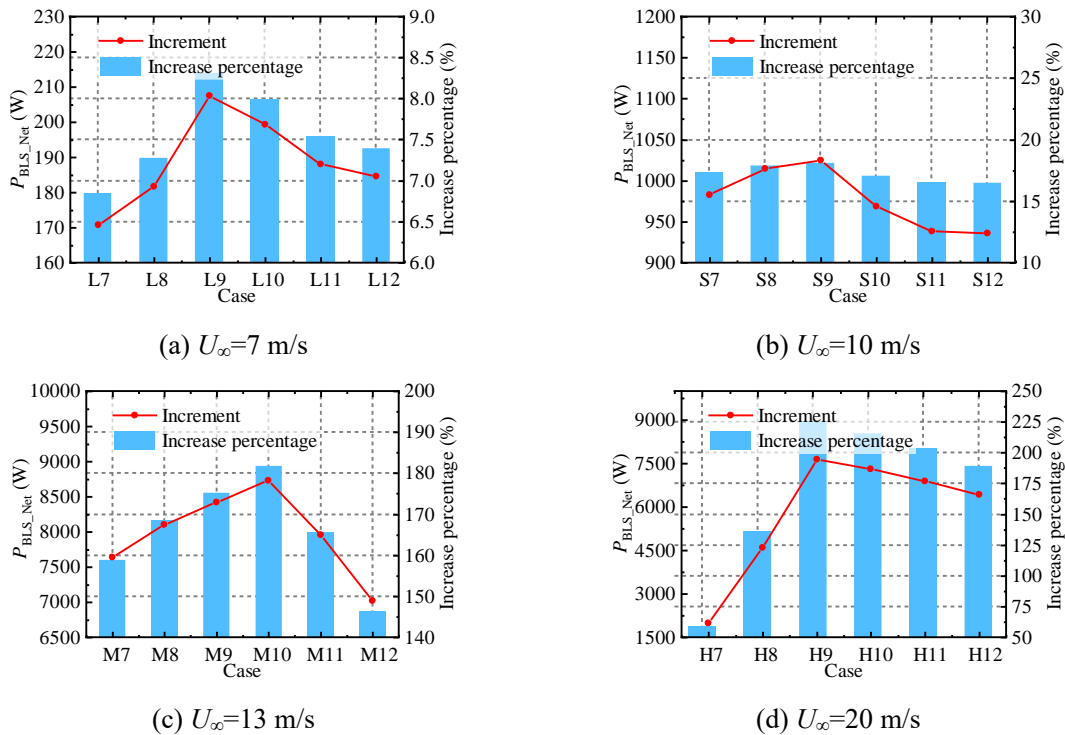


Fig.7. Power increment under $U_{\infty}=7, 10, 13$ and 20 m/s.

320 Further analysis of power increment and increase percentage for different BLS momentum coefficients. Fig.7
321 shows the power increment when BLS energy consumption is considered. As seen in Fig.7a and 7b, under $U_{\infty}=7$ m/s,
322 the average power increment of BLS blade is 188.58 W. Among them, L9 has the most power increment of 207.36 W,
323 which is 8.32% higher than the clean blade. Under $U_{\infty}=10$ m/s, the average power increment of BLS blade is 977.39
324 W. Among them, S9 has the most power increment of 1028.26 W, which is 18.08% higher than the clean blade.

325 As seen in Fig.7c and 7d, under $U_{\infty}=13$ m/s, the average power increment of BLS blade is 7975.76 W Among
326 them, M10 has the most power increment of 8730.10 W, which is 181.71% higher than the clean blade. Under $U_{\infty}=20$
327 m/s, the average power increment is 5804.39 W. Among them, H9 has the most power increment of 7642.14 W, which
328 is 225.56% higher than the clean blade.

329 It can be seen that the power increment is not only the result of single control area, but the result of the joint
330 control of both control areas. Although the contribution of BLS₂ to power increment is much greater than that of BLS₁,
331 the role of BLS₁ cannot be ignored, that is, BLS₁ and BLS₂ are indispensable. In addition, the effect of BLS control is
332 better at low to medium TSR than at high TSR.

333

334 5.3 Correlations to predict power increment curves of the turbine

335 In this section, the correlation equations for HAWT with BLS control have been formed to predict the increment
 336 percent of the HAWT at different TSRs. For low to medium TSR, the V_R is in the range of 0.5-2.5, while for high TSR,
 337 the range of V_R is 2-4.5. The correlation equations to predict increment percent with reference to V_R for different TSR
 338 are as follows:

$$P_{BLS_Net} = 3.30 + 9.54V_R - 5.89V_R^2 + 1.09V_R^3 \quad (27)$$

for TSR = 5.4; $0.5 \leq V_R \leq 2.5$

$$P_{BLS_Net} = 14.37 + 9.13V_R - 7.03V_R^2 + 1.49V_R^3 \quad (28)$$

for TSR = 3.8; $0.5 \leq V_R \leq 2.5$

$$P_{BLS_Net} = 165.53 - 48.42V_R + 32.63V_R^2 - 5.08V_R^3 \quad (29)$$

for TSR = 2.9; $2.0 \leq V_R \leq 4.5$

$$P_{BLS_Net} = -1084.58 + 945.35V_R - 220.83V_R^2 + 16.34V_R^3 \quad (30)$$

for TSR = 1.9; $2.0 \leq V_R \leq 4.5$

339 Fig. 8 show the correlations between increment percent and V_R at different TSR. In the curve fitting process, third
 340 degree polynomials have been fitted through the data points, which give a very high R-squared value, except for
 341 TSR=5.4. It is worth noting that the relevant equation derived in this paper has some limitations, and the equation only
 342 has a good fit in the V_R range at a certain TSR.

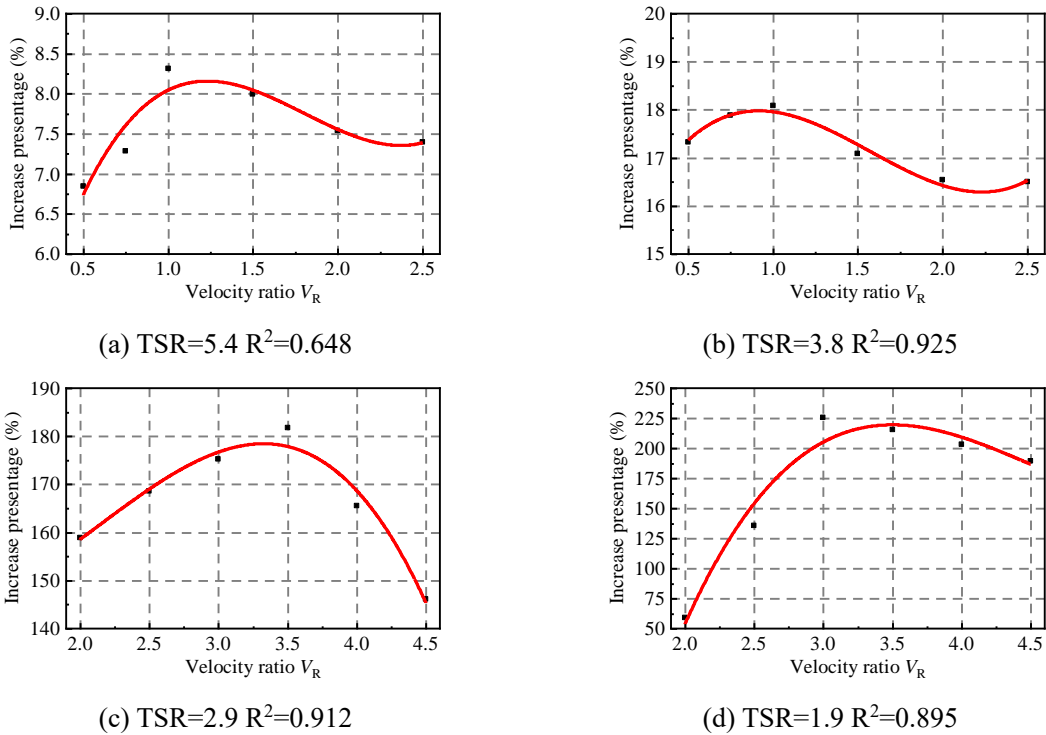


Fig.8. Correlation curves between increment percent and V_R at different TSR.

343

344 5.4 Flow field morphology with BLS control

345 Since the control mechanism of BLS cannot be known by power increment alone, in order to further analyze the
 346 control mechanism of BLS control, the surface streamline, velocity cloud of blade section and pressure coefficient of
 347 clean blade and BLS blade are analyzed.

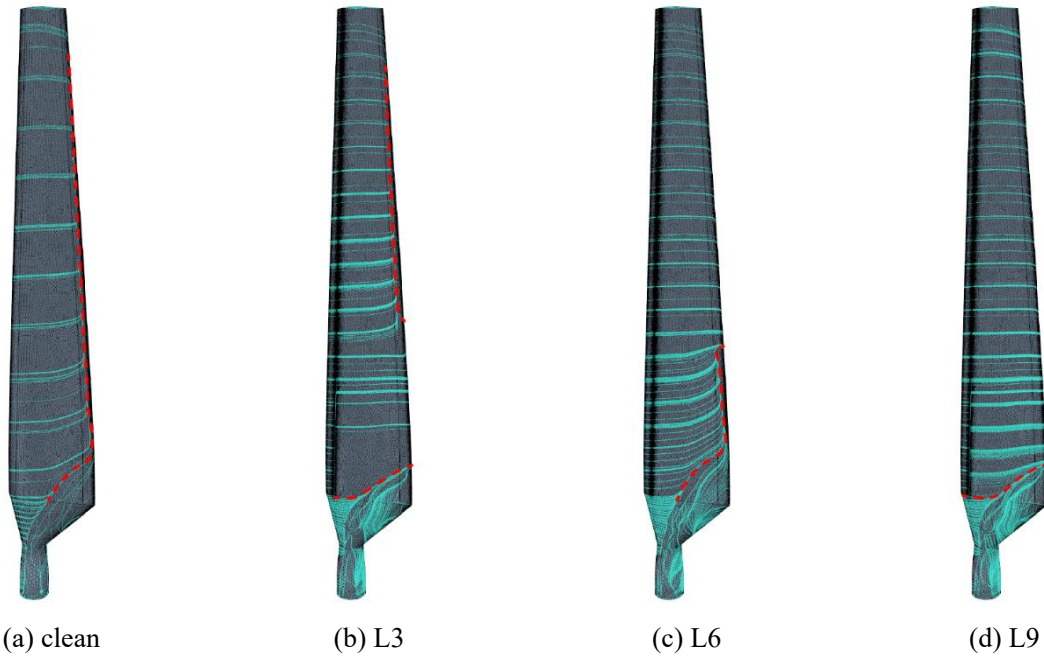


Fig.9. The surface streamline of the clean blades compared with L3, L6 and L9 blades under $U_\infty=7$ m/s.

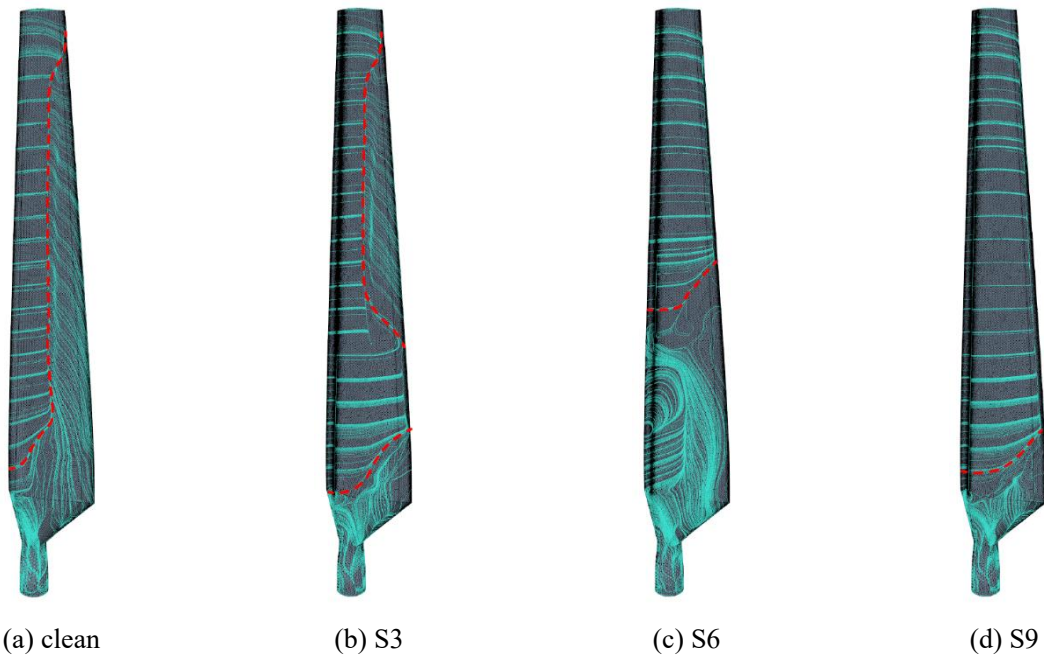


Fig.10. The surface streamline of the clean blades compared with S3, S6 and S9 blades under $U_\infty=10$ m/s.

348 Fig.9 shows the surface streamline of the clean blades compared with L3, L6 and L9 blades under $U_\infty=7$ m/s. As
 349 can be seen from the figure, there is almost no flow separation on the suction surface of clean blade, and only a small
 350 part of trailing edge has non-attachment phenomenon. At this point, BLS control has no significant improvement effect
 351 on surface flow of blade. Fig.10 shows the surface streamline of the clean blades compared with S3, S6 and S9 blades
 352 under $U_\infty=10$ m/s. As can be seen from the figure, the clean blade separation occurs around the middle. The area
 353 controlled by BLS can be significantly improved by making the streamline fit the wall and improving the blade flow.
 354 When BLS₁ shuts down and BLS₂ works, the flow in the A₂ is significantly improved, but the flow in the A₁ is more
 355 complex, which leads to high load fluctuations and is detrimental to the life of the blade. With both BLS₁ and BLS₂
 356 work, the overall blade flow is improved, with only a small flow separation occurs at the root.

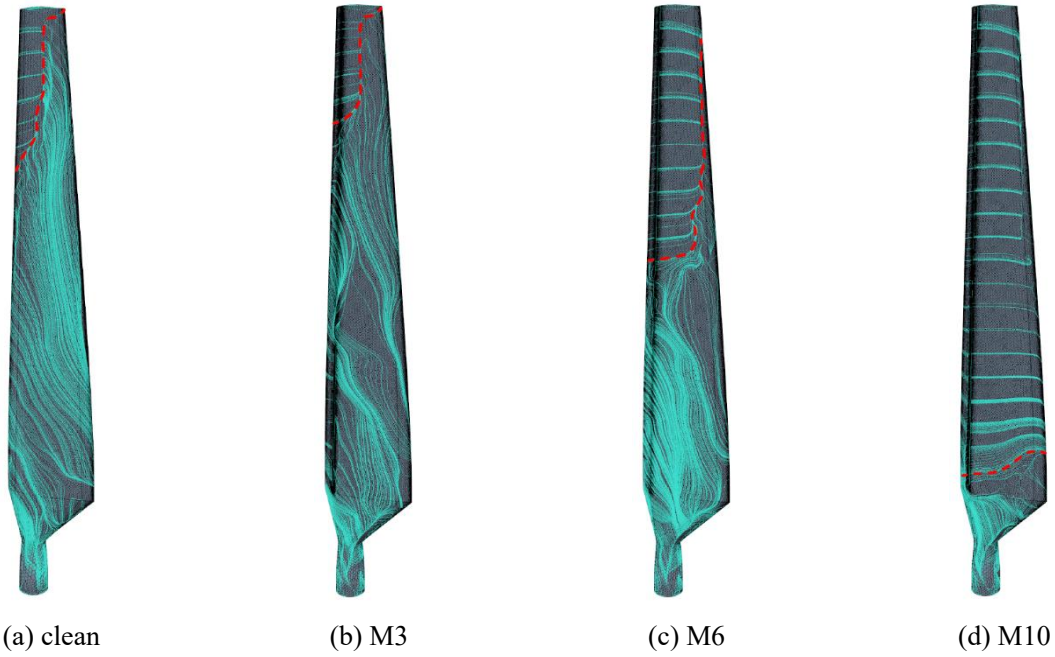


Fig.11. The surface streamline of the clean blades compared with M3, M6 and M10 blades under $U_\infty=13$ m/s.

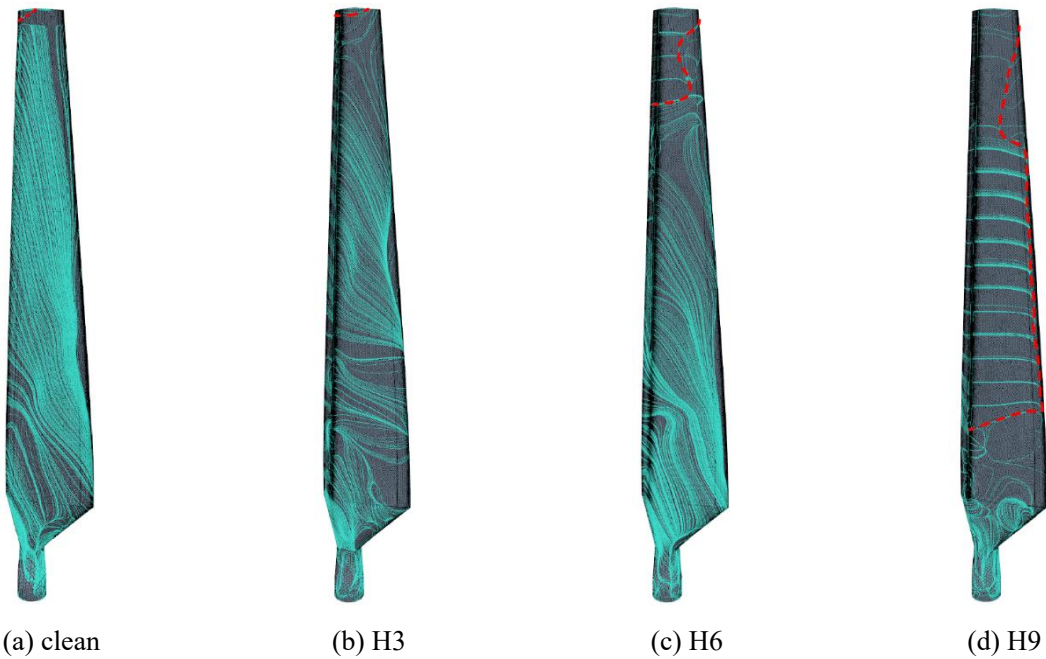
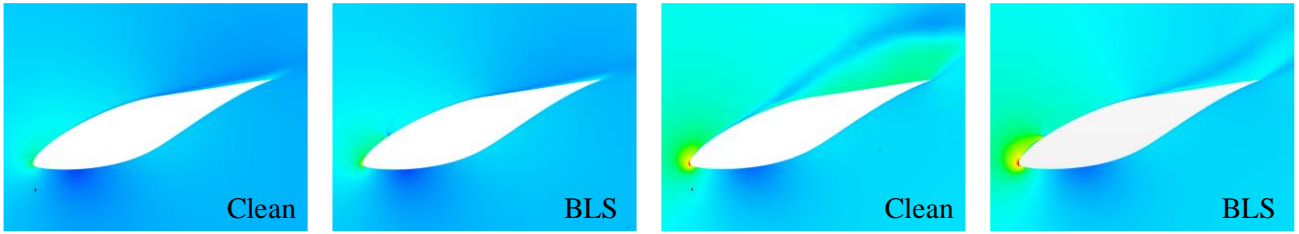
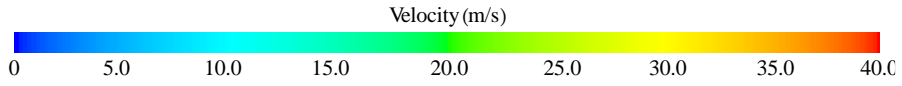


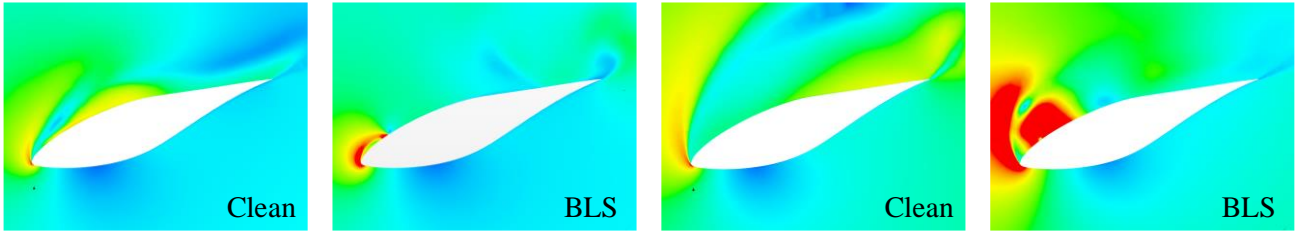
Fig.12. The surface streamline of the clean blades compared with H3, H6 and H9 blades under $U_\infty=20$ m/s.

357 Fig.11 shows the surface streamline of the clean blades compared with M3, M6 and M10 blades under $U_\infty=13$
 358 m/s. As can be seen from Fig.11 a, when $U_\infty=13$ m/s, the clean blade surface presents a large-scale flow separation. At
 359 this time, the effect of BLS_1 control alone is not obvious, while BLS_2 control alone can improve the flow in A_2 . When
 360 BLS_1 and BLS_2 work together, the overall flow of blade is improved, indicating that BLS control is not only effective
 361 in small-scale flow separation, but also significant in large-scale flow separation. Fig.12 shows the surface streamline
 362 of the clean blades compared with H3, H6 and H9 blades under $U_\infty=20$ m/s. It can be seen from the figure that the
 363 result is similar to that of $U_\infty=13$ m/s. However, when $U_\infty=20$ m/s, the flow separation is further intensified, so the
 364 combined work of BLS_1 and BLS_2 cannot completely inhibit the separation, so there are still small areas of flow
 365 separation in the root and tailing edge of blade tip.



$U_\infty=7$ m/s

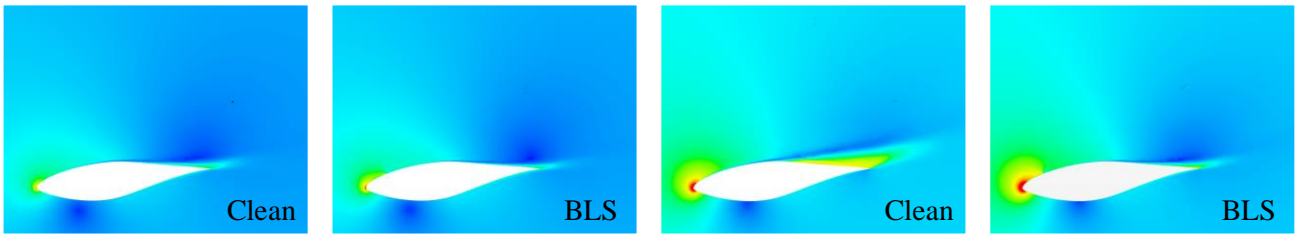
$U_\infty=10$ m/s



$U_\infty=13$ m/s

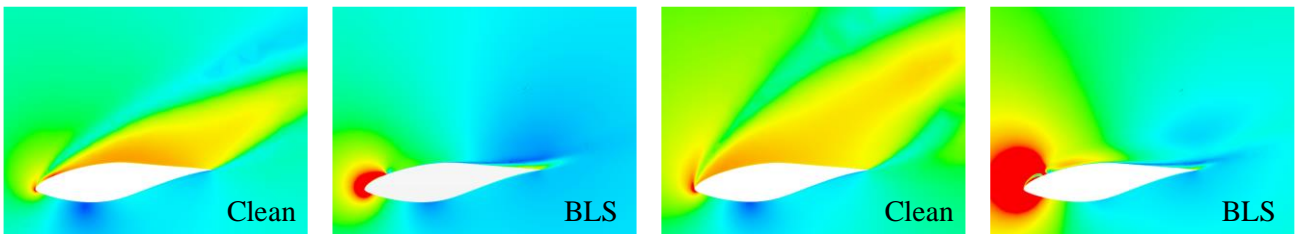
$U_\infty=20$ m/s

(a) $r/R=0.30$



$U_\infty=7$ m/s

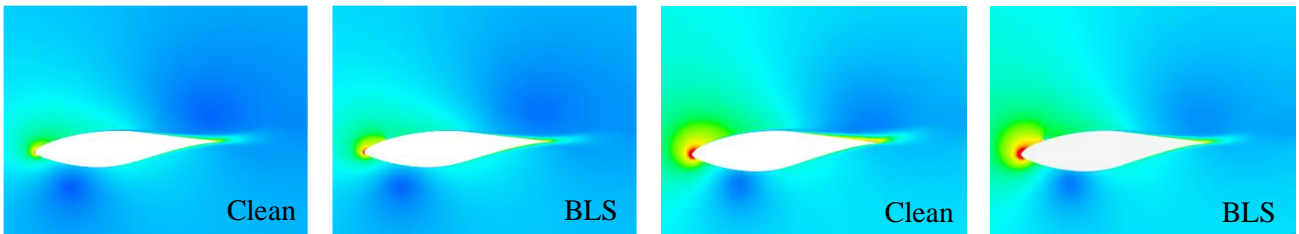
$U_\infty=10$ m/s



$U_\infty=13$ m/s

$U_\infty=20$ m/s

(b) $r/R=0.63$



$U_\infty=7$ m/s

$U_\infty=10$ m/s

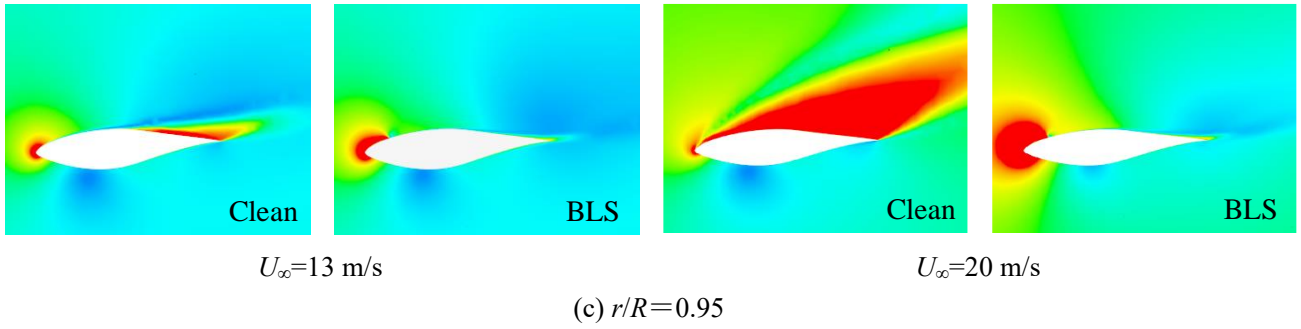
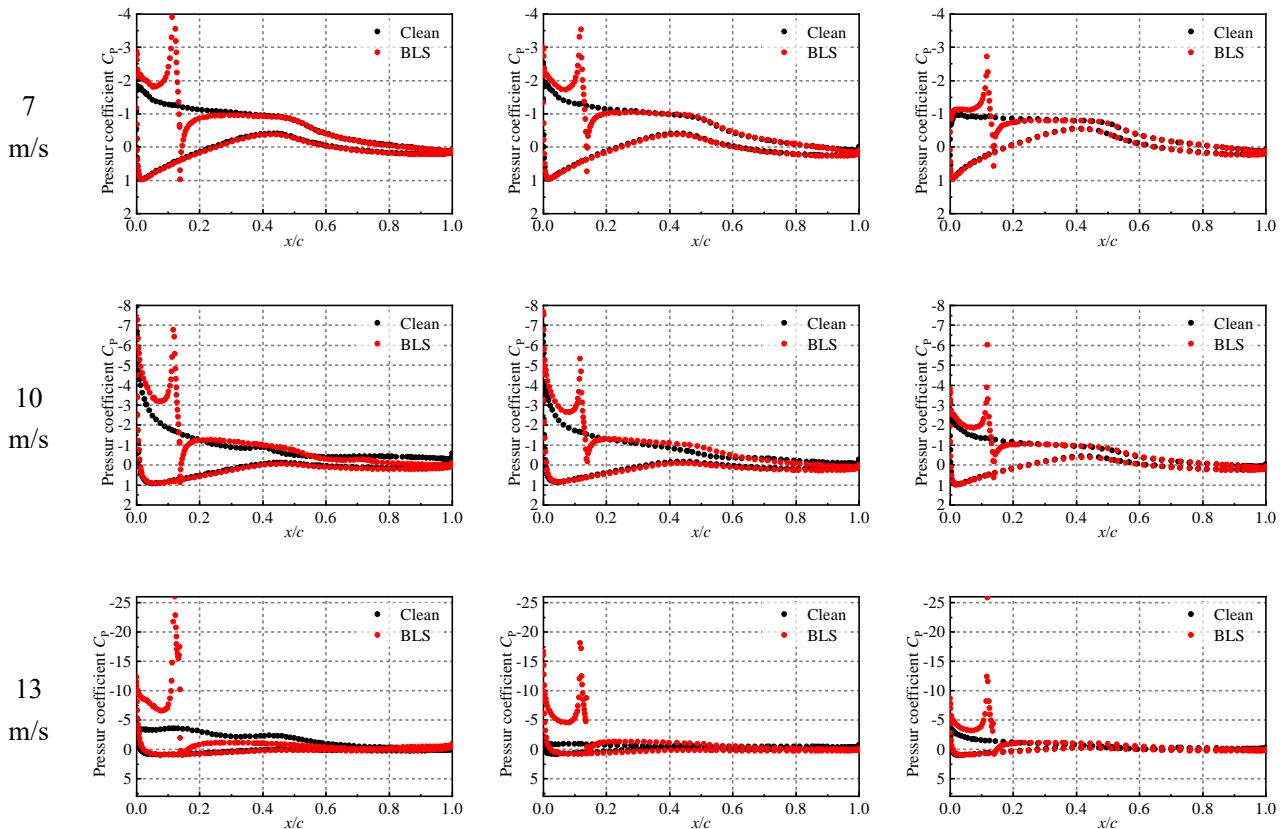


Fig.13. Velocity flow field of blade sections with (L9, S9, M10 & H9) and without BLS control.

366 In order to further deepen the understanding of BLS control, the velocity flow field of each section of the blade
 367 is demonstrated, while its pressure coefficients are plotted. Fig.13 shows the velocity flow field of blade sections with
 368 and without BLS control under $U_\infty=7, 10, 13$ and 20 m/s. As can be seen from the figure, when $U_\infty=7$ m/s, each section
 369 of the blade almost has no stall zone, and the BLS control effect is not obvious at this time. With the decrease of TSR,
 370 the flow separation gradually appeared on the blade surface, when $U_\infty=10$ m/s, there is a small stall zone at trailing
 371 edge of each section of the blade. After adopting BLS control, the stall is significantly improved.

372 As can be seen from Fig.13, when $U_\infty=13$ m/s, there are large stall areas at $r/R=0.30, 0.47, 0.63$ and 0.80 . After
 373 adopting BLS control, the low-velocity fluid in the separation zone is removed, and the formation and development of
 374 leading edge vortices are inhibited, thus the flow field is significantly improved. Combined with Fig.14, it can be seen
 375 that the BLS control can effectively increase the pressure difference between the suction surface and the pressure
 376 surface, which significantly raises the peak negative pressure at the leading edge, shifts the airfoil flow separation
 377 point back, reduces the range of separation vortices over a large area and mitigates the effect of stall on the aerodynamic
 378 performance of the blade. Compared with high TSR, the BLS control effect is particularly obvious at low to medium
 379 TSR.



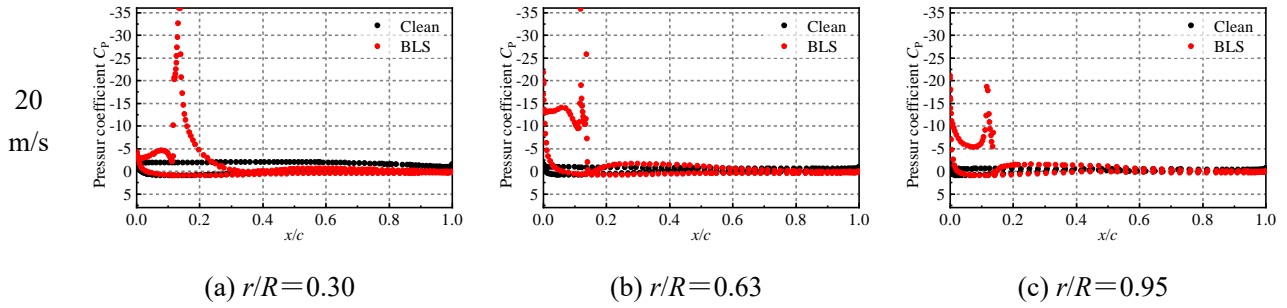


Fig.14. Comparison of pressure coefficients of each section.

380

381 *5.5 Influence of the BLS working angle*

382 In addition to the BLS momentum coefficient, the BLS working angle also has an important influence on the
 383 control efficiency. Therefore, the effect of BLS working angle on control efficiency is further analyzed by dividing the
 384 working angle into nine cases at 20° intervals, as can be seen in Fig.15a. When the C_{μ} of BLS₁ and BLS₂ is 0.16 under
 385 $U_{\infty}=13$ m/s, the case Q7 is analyzed. Fig.15b shows the variation of power increment for different working angles.

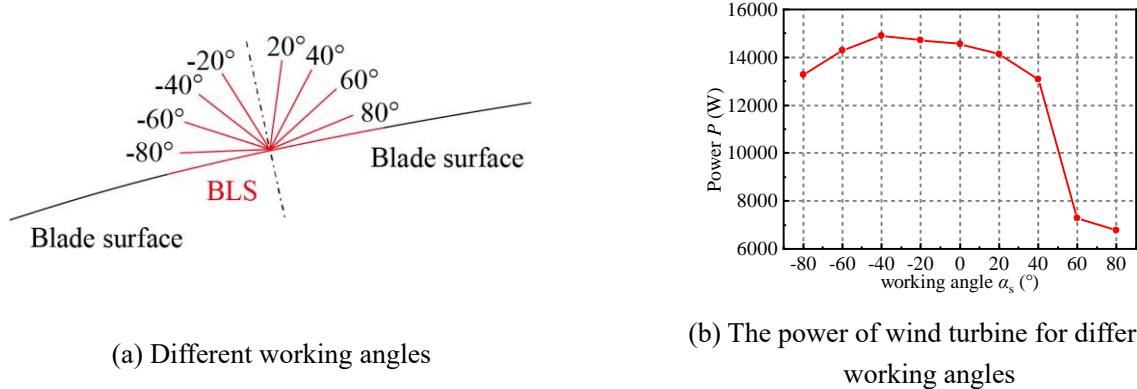


Fig.15. The variation of power for different working angles.

386 As can be seen from Fig.15b, the BLS control obtains higher power at -40° and -20° working angle than at 0°,
 387 which means that the control efficiency of BLS control is enhanced at these two angles. Among them, the power is
 388 highest at -40°, and we believe that BLS can achieve the highest control efficiency at working angle of about -40°.
 389 Combined with Fig.16, it can be seen that under the excessive forward angle, the angle of BLS suction is too large
 390 (nearly 180°) with the incoming flow, resulting in the appearance of additional irregular vortices. At this time, BLS
 391 control has little effect on the improvement of flow field, and even has negative benefit.



Fig.16. Flow field at $r/R=0.63$ for BLS working angle of 80°.

392

393 **6. Conclusion**

394 This research evaluates the possible benefits of applying BLS on HAWT blades. In fact, in the field of aircraft,
 395 BLS is considered as a simple and effective method to improve lift-to-drag ratio of the airfoil and reduce the flow

396 separation. Within the wind energy market and research, the flow control of HAWT is experiencing a new interest.

397 In this research, a lot of work has been done in pre-validation in order to better display the flow field
398 characteristics. Based on the experience of researchers, the SST $k-\omega$ turbulence model is considered to be the most
399 suitable for NREL Phase VI simulations. In addition, the computational burden of the 3D flow field is very high, and
400 in this research, the effect of hub and tower is neglected to simulate a single blade while ensuring the computational
401 accuracy. Although the CFD results overestimate the stall speed at the leaf root at $U_\infty=15$ m/s and $r/R=0.30$, the overall
402 results show that our CFD simulations have reliable results.

403 First, we evaluated the effect of the BLS arranged at the leading edge of the airfoil under 2D simulations. The
404 dynamic mode decomposition is used to decompose the flow field of clean airfoil and BLS airfoil into four modes to
405 deeply analyze the mechanism of BLS control. Subsequently, the effect of BLS on the HAWT blade is analyzed by
406 selecting four kinds of incoming wind speeds ($U_\infty=7, 10, 13$ and 20 m/s). The location of BLS was fixed at $0.15c$ from
407 the leading edge, and the effect of power increment and flow field improvement on the HAWT blade was analyzed by
408 changing the momentum coefficient of BLS. In addition, we provide the relevant equations for these four TSRs in a
409 specific V_R range. Finally, since the working angle of BLS is another factor affecting the control efficiency, this
410 research further analyzes the effect of working angle on the control efficiency by dividing the working angle by 20°
411 interval. The conclusions are as follows:

412 (1) The BLS control can significantly reduce the range of stall area by inhaling low-momentum fluid in the
413 boundary layer and making the fluid better attached to the suction surface. Meanwhile, the analysis of the characteristic
414 value unit circle shows that the use of BLS can effectively increase the stability of the flow field.

415 (2) The BLS control can effectively increase the pressure difference between the suction surface and the pressure
416 surface, significantly increasing the peak negative pressure at the leading edge, shifting the airfoil flow separation
417 point backwards, reducing the separation vortex range over a large area and mitigating the effect of stall on the
418 aerodynamic performance of the blade.

419 (3) At high TSRs, the BLS control has no significant improvement effect on surface flow of blade because there
420 is almost no flow separation on blade surface. With the decrease of the TSR, the flow separation area of the blade
421 increases. At low to medium TSRs, when the surface flow of blade is complex, the use of BLS control can significantly
422 improve the surface flow of blade.

423 (4) When only the root part of the blade is controlled, the gain is negative after considering the energy
424 consumption of BLS. The BLS control at the middle of the blade and the tip plays the main role. However, the amount
425 of gain obtained when both regions are controlled simultaneously is not simply superimposed, but has a greater
426 increment, which indicates that the power increment is not only the result of single region control, but the result of two
427 control regions together.

428 (5) The BLS control can effectively improve the power capability of HAWT. Considering the BLS energy
429 consumption comprehensively, the maximum increment of power can be 207.36 W under $U_\infty=7$ m/s and 1028.26 W
430 under $U_\infty=10$ m/s, which is 8.32% and 18.08% higher than the clean blade. The maximum increment of power can be
431 8730.10 W under $U_\infty=13$ m/s and 7642.14 W under $U_\infty=20$ m/s, which is 181.71% and 225.56% higher than the clean
432 blade.

433 (6) The working angle of BLS should be shifted towards the leading edge of the airfoil to eliminate the separation
434 bubble in advance, thus inhibiting the formation and development of shedding vortices more effectively. It is concluded
435 that the α_s of -40° perform the best energy production.

436 In practical engineering applications, a separate gas source for BLS control should be considered. However,
437 further studies are needed to better assess the benefits of BLS for HAWT. For example, the placement of these BLS
438 means an increase in the extra weight of the blades, as well as an increase in the stress the blades are subjected to,

439 which inevitably has an impact on the cost of wind turbine construction. However, after actual layout, the working
440 angle of BLS cannot be accurately determined due to technical limitations, and we suggest an acceptable working
441 angle of 0° to -40° .
442

443 **7. Future work**

444 This paper mainly studied the influence of different BLS control momentum coefficients on HAWT aerodynamic
445 performance and the contribution of the two control regions to power increment under four TSR from high to low. The
446 following may be undertaken in the future:

447 (1) In this research, the BLS control is fixed on the suction surface at a position $0.15c$ from the leading edge, and
448 the effect of different arrangement positions on the power increment of the HAWT can be studied.

449 (2) In this research, the control area is divided into two regions, and the control area can be further subdivided.

450 (3) Considering only the single BLS, different number of BLS with different momentum coefficients can be
451 arranged for different positions of blades to achieve more accurate flow control.

452 (4) The BLS control in this research is constant, and unsteady control may have different effects on power saving
453 and noise reduction.
454

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458

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