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# **DIRECT DAMAGE CONTROLLED DESIGN OF PLANE STEEL MOMENT RESISTING FRAMES USING STATIC INELASTIC ANALYSIS**

**GEORGE S. KAMARIS, GEORGE D. HATZIGEORGIOU AND DIMITRI E.  
BESKOS\***

A new direct damage controlled design method for plane steel frames under static loading is presented. Seismic loading can be handled statically in the framework of a pushover analysis. This method, in contrast to existing steel design methods, is capable of directly controlling damage, both at local and global level, by incorporating in the analysis continuum damage mechanics for ductile materials. The design process is accomplished with the aid of a two-dimensional finite element program, which takes into account material and geometric nonlinearities by using a nonlinear stress-strain relation through the beam-column fiber modeling and including  $P-\delta$  and  $P-\Delta$  effects, respectively. Simple expressions relating damage to the plastic hinge rotation of member sections and the interstorey drift ratio for three performance limits states are derived by conducting extensive parametric studies involving plane steel moment resisting frames under static loading. Thus, a quantitative damage scale for design purposes is established. Using the proposed design method one can either determine damage for a given structure and loading, or dimension a structure for a target damage and given loading, or determine the maximum loading for a given structure and a target damage level. Several numerical examples serve to illustrate the proposed design method and demonstrate its advantages in practical applications.

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\*: Corresponding author: Tel.: +30.2610.996559; Fax: +30.2610.996579

E-mail address: [d.e.beskos@upatras.gr](mailto:d.e.beskos@upatras.gr)

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## 1. Introduction

Current steel design codes, such as the AISC [1998] and EC3 [1992], are based on ultimate strength and the associated failure load. In both codes, member design loads are usually determined by global elastic analysis and inelasticity is taken into account indirectly through the interaction equations involving design loads and resistances defined for every kind of member deformation. Instability effects are also taken in an indirect and approximate manner through the use of the effective length buckling factor, while displacements are checked for serviceability at the end of the design process. Seismic design loads are obtained with the aid of seismic codes, such as the AISC [2005] and the EC 8 [2004]. In this case the global analysis can be elastostatic as before, spectral dynamic, static inelastic (pushover) or nonlinear dynamic.

Damage of materials, members and structures is defined as their mechanical degradation under loading. Control of damage is always desirable by design engineers. Eventhough current methods of design [AISC 1998; EC3 1992; AISC 2005; EC8 2004] are associated with ultimate strength and consider inelastic material behavior indirectly or directly, they are force-based and cannot achieve an effective control of damage, which is much better related to displacements than forces. For example, the percentage of the inter-story drift ratio (IDR) of seismically excited buildings is considered a solid basic indicator of the level of damage, as suggested by the HAZUS99-SR2 Technical Manual of FEMA [2001]. Even the displacement-based seismic design method [Priestley et al. 2007], in which displacements play the fundamental role in design and are held at a permissible level (target displacements), does not lead into a direct and transparent control of damage.

To be sure, there are many works in the literature dealing with the determination of damage in members and structures, especially in connection with the seismic design of reinforced concrete structures. More specifically, damage determination of framed buildings at the local and global level can be done with the aid of damage indices computed on the basis of deformation and/or energy dissipation, as shown, e.g., by Park and Ang [1985] and Powell and Allahabadi [1998]. On the other hand, the finite element method has been employed in the analysis of steel and reinforced concrete structures in conjunction with a concentrated inelasticity (plasticity and damage) beam element by Florez-Lopez [1998]. Damage determination in reinforced concrete and masonry structures has also been done by employing continuum theories of distributed damage in the framework of the finite element method [Cervera et al. 1995; Hatzigeorgiou et al. 2001; Hanganu et al. 2002]. It should be noted that all of the above research works have been proposed to determine damage as an additional structural design information and cannot lead to a structural design with controlled damage.

In this paper, the Direct Damage Controlled Design (DDCD) method, a new design method recently proposed by Hatzigeorgiou and Beskos [2007] for concrete structures, is extended here to structural steel design. The basic advantage of DDCD is the dimensioning of structures with damage directly controlled at both local and global levels. In other words, the designer can select a priori the desired level of damage in a structural member or a whole structure and direct his design in order to achieve this preselected level of damage. Thus, while the DDCD deals directly with damage, inelastic design approaches, such as [AISC 1998; EC3 1992; AISC 2005; EC8 2004; Priestley et al. 2007] are concerned indirectly with damage. Furthermore, the a priori knowledge of damage, as it is the case with DDCD, ensures a controlled safety level, not only in strength but also in deflection terms. Thus, the present work, unlike all previous works on damage of steel structures, develops for the first

time a direct damage controlled steel design method, which is not just restricted to damage determination as an additional structural design information.

More specifically, the present work develops a design method for plane steel moment resisting frames under static monotonic loading capable of directly controlling damage, both at local and global level. Seismic loading can be handled statically in the framework of a pushover analysis. Local damage is defined point-wise and expressed as a function of deformation on the basis of continuum damage mechanics theory for ductile materials [Lemaitre 1992]. On the other hand, global damage definition is based on the demand-and-capacity-factor design format as well as on various member damage combination rules. The method is carried out with the aid of the two-dimensional (2-D) finite element program DRAIN-2DX [Prakash et al.1993], which takes into account material and geometric nonlinearities, modified by the authors to employ damage as a design criterion in conjunction with appropriate damage levels. Material nonlinearities are implemented in the program by combining a nonlinear stress-strain relation for steel with the beam-column fibered plastic hinge modeling. Geometric nonlinearities involve  $P-\delta$  and  $P-\Delta$  effects. Thus, the proposed method belongs to the category of design methods using advanced methods of analysis [Chen and Kim 1997; Kappos and Manafpour 2001; Vasilopoulos and Beskos 2006], which presents significant advantages over the code-based methods. Local buckling can be avoided by using only class 1 European steel sections, something which is compatible with the inelastic analysis employed herein. Furthermore, all structural members are assumed enough laterally braced in order to avoid lateral-torsional buckling phenomena. Using the proposed design method one can either determine damage for a given structure and loading, or dimension a structure for a target damage and given loading, or determine the maximum loading for a given structure and a target damage level.

## 2. Stress-strain relations for steel

Essential features of a steel constitutive model applicable to practical problems should be, on the one hand the accurate simulation of the actual steel behavior and on the other hand the simplicity in formulation and efficiency in implementation in a robust and stable non-linear algorithmic manner. In this work, a multi-linear stress-strain relation for steel characterized by a good compromise between simplicity and accuracy and a compatibility with experimental results, is adopted. The stress-strain  $(\sigma, \varepsilon)$  relation in tension for this steel model is of the form

$$\begin{aligned}\sigma &= E\varepsilon && \varepsilon \leq \varepsilon_y \\ \sigma &= \sigma_y + E_h(\varepsilon - \varepsilon_y) && \text{for } \varepsilon_y < \varepsilon \leq \varepsilon_u \\ \sigma &= \sigma_u && \varepsilon_u < \varepsilon\end{aligned}\quad (1)$$

Equation (1) describes a tri-linear stress-strain relation representing elastoplastic behavior with hardening, as shown in Fig. 1, with  $E$  and  $E_h$  being the elastic and the inelastic moduli, respectively,  $\varepsilon_y$  and  $\varepsilon_u$  the yield and the ultimate strains, respectively and  $\sigma_y$  and  $\sigma_u$  the yield and ultimate stress, respectively. The negative counterpart to the above relation can be adopted for the compression stress state, as shown in Fig. 1. It should be noticed that similar stress-strain curves have been proposed in the past by others (e.g. Gioncu and Mazzolani [2002]) and that European and American steels exhibit a stress-strain behavior as that of Fig. 1. Thus, the adopted model of Eq. (1) can effectively depict the true behavior of structural steel.

## 3. Local damage

Local damage is usually referred to a point or a part of a structure and is one of the most appropriate indicators about their loading capacity. In the framework of continuum damage

mechanics, the term “local” is associated with damage indices describing the state of the material at particular points of the structure, and the term “global” with damage indices describing the state of any finite material volume of the structure. Thus, global damage indices can be referred to any individual section, member, substructure, or the whole structure. This categorization of damage is in agreement with continuum mechanics principles stipulating that constitutive models are defined at point level and all other quantities are obtained by integrating point-wise information.

Continuum damage mechanics has been established for materials with brittle or ductile behavior and attempts to model macroscopically the progressive mechanical degradation of materials under different stages of loading. For structural steel, damage results from the nucleation of cavities due to decohesions between inclusions and the matrix followed by their growth and their coalescence through the phenomenon of plastic instability. The theory assumes that the material degradation process is governed by a damage variable  $d$ , the local damage index, which is defined pointwise as [Lemaitre 1992]

$$d = \lim_{S_n \rightarrow 0} \frac{S_n - \bar{S}_n}{S_n} \quad (2)$$

where  $S_n$  stands for the overall section in a damage material volume,  $\bar{S}_n$  for the effective or undamaged area, while  $(S_n - \bar{S}_n)$  denotes the inactive area of defects, cracks and voids (Fig. 2). This index corresponds to the density of material defects and voids and has a zero value when the material is in the undamaged state and a value of unity at material rupture or failure.

The main goal of continuum damage mechanics is the determination of initiation and evolution of the damage index  $d$  during the deformation process. Lemaitre [1992], by assuming that damage evolution takes place only during plastic loading (plasticity induced

damage) was able to propose a simple damage evolution law, as shown in Fig. 3, which can successfully simulate the behavior of steel or other ductile materials. Damage index  $d$  is represented by a straight line in damage-strain space, with end points at  $d=0$  for  $\varepsilon=\varepsilon_y$ , and  $d=1$  for  $\varepsilon=\varepsilon_u$ , where strain values are assumed to be absolute. This damage evolution law can be expressed as

$$\begin{aligned}
 d &= 0 && \varepsilon \leq \varepsilon_y \\
 d &= \frac{\varepsilon - \varepsilon_y}{\varepsilon_u - \varepsilon_y} && \text{for } \varepsilon_y < \varepsilon \leq \varepsilon_u
 \end{aligned} \tag{3}$$

A similar linear damage evolution law has also been proposed by Florez-Lopez [1998]. Both laws are supported by experiments. One can observe that while the damage evolution law for concrete [Hatzigeorgiou and Beskos 2007] was derived by appropriately combining basic concepts of damage mechanics and a nonlinear stress-strain equation for plain concrete, the present damage evolution law for steel (Eq. (3)), was taken directly from the literature [Lemaitre 1992].

#### **4. Global damage**

Global damage is referred to a section of a member, a member, a substructure or a whole structure and constitutes one of the most suitable indicators about their loading capacity. Several methods to determine an indicator of damage at the global level have been presented in the literature. In general, these methods can be divided into four categories involving the following structural demand parameters: stiffness degradation, ductility demands, energy dissipation, and strength demands. According to the first approach, one of the most popular ways is to relate damage to stiffness degradation indirectly, i.e., to the variation of the



fundamental frequency of the structure during deformation [DiPasquale and Cakmak 1990]. However, this approach is inappropriate for the evaluation of the global damage of a substructure or its impact on the overall behavior. Furthermore, in order to evaluate the complete evolution of global damage with loading, a vast computational effort is needed due to the required eigenvalue analysis at every loading step. An alternative way to determine global damage is by computing the variation of the structural stiffness during deformation (e.g., Ghoborah et al. [1999]), but again, evaluation of the global damage evolution requires heavy computational work at every loading step. Many researchers determine damage in terms of the IDR. Whereas macroscopic quantities such as IDR's are good indicators of global damage in regular structures, this is not generally the case in more complex and/or irregular structures. Damage determination has also been done with the aid of damage indices computed on the basis of ductility (defined in terms of displacements, rotations or curvatures) and/or energy dissipation, as is evident in the method of Park and Ang [1985] for framed concrete buildings or in the review article of Powell and Allahabadi [1988]. For computation of damage in steel structures under seismic loading, one can mention the recent works of Vasilopoulos and Beskos [2006] and Benarent-Climent [2007]. However, it should be noted that all these indices are adequate for seismic analyses only. They are not applicable to other types of problems, such as static ones [Hanganu et al. 2002].

In this work, for the section damage index  $D_s$  of a steel member, the following expression is proposed

$$D_s = \frac{c}{d} = \frac{\sqrt{(M_S - M_A)^2 + (N_S - N_A)^2}}{\sqrt{(M_B - M_A)^2 + (N_B - N_A)^2}} \quad (4)$$

In the above, the bending moments  $M_A$ ,  $M_S$  and  $M_B$  and the axial forces  $N_A$ ,  $N_S$  and  $N_B$  as well as the distances  $c$  and  $d$  are those shown in the moment  $M$  – axial force  $N$  interaction diagram of Fig. 4 for a plane beam-column element. The bending moment  $M_S$  and axial force  $N_S$  are design loads incorporating the appropriate load factors in agreement with EC3 [1992]. Figure 4 includes a lower bound damage curve, the limit between elastic and inelastic material behavior and an upper bound damage curve, the limit between inelastic behavior and complete failure. Thus, damage at the former curve is zero, while at the latter curve is one. Equation (4) is based on the assumption that damage evolution varies linearly between the above two damage bounds. These lower and upper bound curves can be determined accurately with the aid of the beam-column fibered plastic hinge modeling described in the next section. For their determination, the resistance safety factors are taken into account in agreement with EC3 [1992]. The bound curves of Fig. 4 can also be determined approximately by code type of formulae. Thus, the lower bound curve can be expressed as

$$\frac{M}{M_y} + \frac{N}{N_y} = 1 \quad (5)$$

where  $N_y$  and  $M_y$  are the minimum axial force and bending moment, respectively, which cause yielding, while the upper bound curve can be expressed as

$$\frac{M}{M_u} + \left( \frac{N}{N_u} \right)^2 = 1 \quad (6)$$

where  $N_u$  and  $M_u$  are the ultimate axial force and bending moment, respectively, which cause failure of the section. Equations (5) and (6) can be used for the construction of the bounding

curves of Fig. 4. It should be noticed that EC3 [1992] provisions give a M-N interaction formula similar to Eq. (6), with the hardening effect not taken into account, i.e., with  $\sigma_u = \sigma_y$  or equivalently,  $N_u = N_y$ . Furthermore, since EC3 [1992] allows inelastic analysis only for section class 1, the proposed method is limited to sections of that class.

One can observe that the proposed section damage index of Eq. (4) actually represents an extension of Eq. (3) from strains (or stresses) to forces and moments, i.e. stress resultants. Expressions for damage in terms of stress resultants are also mentioned in [Lemaitre 1992]. Furthermore, Florez-Lopez [1998] adopts the “generalized effective stress”, which corresponds to bending moment, by analogy with the definition of the “effective stress”, which corresponds to inelastic stress. However, his formulation includes only bending moments without any interaction with axial forces. It should be noted that the proposed section damage index corresponds to the aforementioned fourth type of damage indicators, which are related to the strength demand approach. More specifically, this index is based on the demand-and-capacity-factor design format. There is an analogy or correspondence between the capacity ratio of interaction equations of EC3 [1992] and the proposed damage index (see Fig. 4). Furthermore, this format is similar to the one implemented for performance evaluation of new and existing steel moment resisting structures in FEMA 350 [2000a] and FEMA 351 [2000b], respectively. The member damage index  $D_M$  is taken as the largest section damage index, along the member. This is a traditionally and effective assumption in structural design [Kappos and Manafpour 2001].

Therefore,

$$D_M = \max(D_S) \quad (7)$$

To provide an overall damage index that is representative of the damage state of a complex structure, the member damage indices must be combined in a rational manner to reflect both the severity of the member damage and the geometric distribution of damage within the overall structure. Various weighted-average procedures have been proposed for combining the member damage indices into an overall damage index. Thus, for a structure composed of  $m$ -members, the overall damage index,  $D_O$ , has the form

$$D_O = \left( \frac{\sum_{i=1}^m D_{M,i}^2 W_i}{\sum_{i=1}^m W_i} \right)^{1/2} \quad (8)$$

where  $D_{M,i}$  and  $W_i$  denote the damage and weighting factor of the  $i^{\text{th}}$  member, respectively. The above expression is in agreement with the fact that the most damaged members affect the overall damage much more than the undamaged (elastic) members. Park and Ang [1985], assuming that the distribution of damage is correlated with the distribution of plastic strain energy dissipation, applied Eq. (8) with the weighting factors to correspond to the amount of plastic strain energy dissipation. Similar approaches to the Park and Ang [1985] hypothesis have been also proposed by other researchers, e.g. Powell and Allahabadi [1988]. However, all these approaches are exclusively applied to seismic problems where the external loads have a cyclic form. It is evident that the amount of plastic strain energy dissipation is an inappropriate measure for static monotonic problems. For this reason, the overall damage index  $D_O$  is assumed here to be of the form [Cervera et al 1995]

$$D_o = \left( \frac{\sum_{i=1}^m D_{M,i}^2 \Omega_i}{\sum_{i=1}^m \Omega_i} \right)^{1/2} \quad (9)$$

where  $\Omega_i$  denotes the volume of the  $i^{\text{th}}$  member. This relation reflects both the severity of the member damage and the geometric distribution of damage within the structure.

## 5. Global damage levels

**5.1 Introduction.** Damage is used here as a design criterion. Thus, the designer, in addition to a method for determining damage, also needs a scale of damage in order to decide which level of damage is acceptable for his design. Many damage scales can be proposed in order to select desired damage levels associated with the strength degradation and capacity of a structure to resist further loadings. Table 1 provides the three performance levels (I.O. = Immediate Occupancy, L.S. = Life Safety and C.P. = Collapse Prevention) associated with modern performance-based seismic design with the corresponding limit response values (performance objectives) in terms of IDR = interstorey drift ratio,  $\theta_{pl}$  = plastic rotation at member end,  $\mu_\theta$  = local ductility and  $d$  = damage as well as the relevant references. The selection of the appropriate damage level depends on various factors, such as the importance factor or the “weak beams – strong columns” rule in seismic design of structures. Thus, e.g., nuclear power plants should be designed with zero damage and plane frames with 60% and 30% maximum damage in beams and columns, respectively. The proposed design method uses the damage level scale that has been derived with the aid of extensive parametric studies on plane frames and corresponds to the three performance levels of FEMA-273 [1997]. It should be noted that damage characterizations like minor, major etc. given by modern seismic codes are qualitative and very general and hence inappropriate to be used in practical

design. In contrast to them, the proposed values of damage indices can be easily used in practical design.

The following subsections provide details concerning the parametric studies conducted herein for the derivation of simple expressions relating damage to the plastic hinge rotation of the member sections and the IDR of the plane steel frames considered to be used for the construction of a practical quantitative damage scale.

**5.2 Frame geometry and loading.** A set of 36 plane steel moment resisting frames was employed for the parametric studies of this work. These frames are regular and orthogonal with storey heights and bay widths equal to 3 m and 5 m, respectively. Furthermore, they are characterized by a number of stories  $n_s$  with values 3, 6, 9, 12, 15 and 20 and a number of bays  $n_b$  with values 3 and 6. The frames were subjected to constant uniform vertical loads  $1.35G+1.5Q=30\text{kN/m}$  and horizontal variable loads  $1.35W$ , where  $G$ ,  $Q$  and  $W$  correspond to dead, live and wind loads, respectively. The material properties taken from structural steel grade S235, were divided by a factor of 1.10 for compatibility with EC3[1992] provisions. The frames were designed in accordance with Eurocodes EC3 [1992] and EC8 [2004]. Data of the frames, including values for  $n_s$ ,  $n_b$ , beam and column sections and first and second natural periods, are presented in Table 2 taken from [Karavasilis et al. 2007]. In that table, expressions of the form, e.g., 260-360(1-4) + 240-330(5-6) mean that the first four stories have columns with HEB260 sections and beams with IPE360 sections, whereas the next two higher stories have columns with HEB240 sections and beams with IPE330 sections.

**5.3 Proposed global damage level values.** The previously described plane steel frames were analyzed by the computer program DRAIN-2DX [Prakash et al. 1993]. Use was made of its beam-column element with two possible plastic hinges at its ends modeled by fibers. During

the analyses, the vertical loads of the frames remained constant, while the horizontal ones were progressively increased in order to identify the damage corresponding to each performance level of Table 1. Damage was calculated at section and structural levels by using expressions (4), (7) and (9). In addition, the interstorey drift ratio (IDR) and the plastic hinge rotation at the end of each member were computed. The latter one was computed in the form  $\frac{\theta_{pl}}{\theta_y}$ , where  $\theta_y$  is the rotation at yielding expressed by FEMA 273 [1997] as

$$\theta_y = \frac{M_{pl} \cdot L}{6 \cdot E \cdot I} \quad (10)$$

where L is the member length, E is the modulus of elasticity of the material and I is the moment of inertia of the section. When members, such as columns, are subjected to an axial compressive force P, the right hand side of Eq.(10) is multiplied by the factor  $1 - \frac{P}{P_y}$  where  $P_y$  is the axial yield force of the member.

This subsection presents the results of the aforementioned parametric studies. Figures 5 and 6 show the variation of the section damage index  $D_s$  versus the ratio  $\frac{\theta_{pl}}{\theta_y}$  for low (3 and 6 stories) and high (9,12,15 and 20 stories) rise frames, respectively. Figures 7 and 8 show the variation of the overall damage index  $D_o$  versus IDR for low (3 and 6 stories) and high (9,12,15 and 20 stories) rise frames respectively. Using the method of least squares the mean values of these variations were determined and plotted as straight line segments in Figs 5-8. The analytical expressions of these lines are of the following form:

For the low rise frames

$$D_s = 12.526 \cdot \left( \frac{\theta_{pl}}{\theta_y} \right) \quad \text{for} \quad \frac{\theta_{pl}}{\theta_y} \leq 2.2 \quad (11)$$

$$D_s = 3.54 \cdot \left( \frac{\theta_{pl}}{\theta_y} \right) + 20.14 \quad \frac{\theta_{pl}}{\theta_y} > 2.2$$

$$D_o = 4.67 \cdot IDR \quad (12)$$

For the high rise frames

$$D_s = 2.42 \cdot \left( \frac{\theta_{pl}}{\theta_y} \right) \quad (13)$$

$$D_o = 0.94 \cdot IDR \quad (14)$$

The coefficient of determination  $R^2$  of Eqs. (11) and (13) is 0.96 and 0.79 respectively, showing that there is a good correlation between the section damage and the plastic hinge rotation. On the contrary, the correlation between structure damage and the IDR is not so good as the coefficient of determination is 0.53 and 0.72 for Eqs. (12) and (14), respectively.

Using the values of  $\theta_{pl}$  and IDR given in FEMA-273[1997] for the three performance levels of Table 1 into Eqs. (11)-(14), a section and overall damage scale is constructed for low and rise frames and given in Table 3. The low values of damage in the high rise frames in that table can be explained by the instabilities caused in the analyses due to the concentration of damage in one or two sections and the P- $\delta$  and P- $\Delta$  effects. In the case of structural damage, this concentration combined with the definition of  $D_o$  in Eq. (9) explains these very small values. It is apparent from Eq. (9) that even if one has large values of section damage in a few sections, the overall damage will have a small value because of the small or zero values in other sections. For this reason, the overall damage index is not considered as a representative one, and the section damage index is used in the applications.



## 6. Direct damage controlled steel design

The application of the proposed Direct Damage Controlled Design (DDCD) method to plane steel members and framed steel structures is done with the aid of the DRAIN-2DX [Prakash et al. 1993] computer program, modified properly by the authors to perform both analysis and design. This program can statically analyze with the aid of the finite element method plane beam structures taking into account material and geometric nonlinearities. Material nonlinearities are accounted for through fiber modeling of plastic hinges in a concentrated plasticity theory (element 15 of DRAIN-2DX [Prakash et al. 1993]). Geometric nonlinearities include the  $P-\delta$  effect (influence of axial force acting through displacements associated with member bending) and the  $P-\Delta$  effect (influence of vertical load acting through lateral structural displacements), which are accounted for by utilizing the geometric stiffness matrix.

The beam-column section is subdivided in a user-defined number of steel fibers (Fig. 10). Sensitivity studies have been undertaken to define the appropriate number of fibers for various types of sections. For example, for an I-section under axial force and uniaxial bending moment one can have satisfactory accuracy by dividing that section into 30 fibers (layers). Thus, for every structural steel member, selected sections are divided into steel fibers and the stress–strain relationship of Eq. (1) is used for tension and compression.

In the analysis, every member of the structure needs to be subdivided into several elements (usually three or four) along its length to model the inelastic behavior more accurately. The analysis leads to highly accurate results, but is, in general, computationally intensive for large and complex structures. Figure 9 shows the flow chart of the modified DRAIN-2DX [Prakash et al. 1993] computer program for damage controlled steel design.

Using this modified DRAIN-2DX program [Prakash et al. 1993], the user has three design options at his disposal in connection with damage controlled steel design:

- a) determine damage for a given structure under given loading
- b) dimension a structure for given loading and given target damage
- c) determine the maximum loading a given structure can sustain for a given target damage.

The first option is the one usually done in current practice. The other two options are the ones which actually make the proposed design method a direct damage controlled one.

## 7. Examples of application

This section describes two numerical examples to illustrate the use of the proposed design method and demonstrate its advantages.

**7.1 Static design of a plane steel frame.** A plane two bay – two storey steel frame is examined in this example. Figure 11 shows the geometry and loading of the frame. Columns consist of standard HEB sections, while beams of standard IPE sections. The beams are subjected to uniform vertical loads  $G=15.0$  kN/m and  $Q=20.0$  kN/m, where  $G$  and  $Q$  correspond to permanent and live loads, respectively. Additionally, the frame is subjected to horizontal wind loads  $W=12.6$  kN at the first floor level and  $W=22.2$  kN/m at the second. Steel is assumed to follow the material properties of steel grade S235 with trilinear stress-strain curve. Without loss of generality, only one loading combination of EC3 [1992] is examined here, that corresponding to  $1.35(G+Q+W)$ .

In the following, the frame is studied for the three design options of the proposed design method. Initially, the first design option, related to the determination of damage for a given structure and known loading, is examined. In this case, the structure is designed according to the EC3[1992] method. In order to design this frame, four different member sections are

determined, as shown in Fig. 11:a) columns of the 1<sup>st</sup> floor; b)columns of the 2<sup>nd</sup> floor; c)beams of the 1<sup>st</sup> floor; d)beams of the 2<sup>nd</sup> floor

The most appropriate standard sections have been found to be those in Table 4. These sections have been obtained on the basis of a first order elastic analysis according to EC3 [1992]. In order to determine the damage level, the structure is analyzed by the modified DRAIN-2DX [Prakash et al. 1993] program taking into account inelasticity and second order phenomena. The damage determined in all the members was found equal to zero (Table 4) indicating linear elastic behavior of the structure.

The second design option has to do with member dimensioning for a pre-selected target damage level and known loading. Thus, using the modified DRAIN-2DX program [Prakash et al. 1993], one can determine the most appropriate sections in order to have the selected target (maximum) damage at members, for the same loading combination as above. Two different damage levels are considered by setting the maximum member damage equal to 25% and 75% for columns and beams, respectively. The sections found appear also in Table 4. For those sections, the computed values of maximum member damage  $D_s$  become 24.2% and 73.7%, for columns and beams, respectively i.e., very close from below to the preselected (target) values of 25% and 75%, respectively. It is evident that the acceptance of greater damage levels decreases the sizes of the sections.

Finally, the third design option associated with the determination of maximum loading for a given structure and pre-selected target damage is examined. Use is made again of the modified DRAIN-2DX program [Prakash et al. 1993]. The examined structure is assumed to consist of the standard sections obtained in the second design option (see Table 4). In this case, vertical (permanent and live) loads are assumed to remain the same. Thus, allowing maximum values of damage  $D_s = 30\%$  and  $0\%$  for beams and columns, respectively, one can

determine the maximum wind load. Indeed, one can find allowable maximum wind load equal to 11.5 and 20.2, kN for the first and second floor, respectively.

**7.2 Seismic design of a plane steel frame by pushover.** Consider a S235 plane steel moment resisting frame of three bays and three storeys. The bay width is assumed equal to 5 m and the storey height equal to 3 m. The load combination  $G+0.3Q$  on beams is equal to 27.5 KN/m. HEB profiles are used for the columns and IPE profiles for the beams. The frame was designed according to structural Eurocodes EC3 [1998] and EC8 [2004] for a peak ground acceleration equal to 0.4g, a soil class D and a behaviour factor  $q=4$  with the aid of SAP2000 [2005] program in conjunction with the capacity design requirements of EC8 [2004]. Thus, for a design base shear of 355 kN, the following column and beam sections were obtained for the three stories: (HEB280-IPE360) + (HEB260-IPE330) + (HEB240-IPE300). The maximum elastic top floor displacement was found equal to 0.0465 m. Thus, according to EC8 [2004], the corresponding inelastic displacement will be  $0.0465q=0.186\text{m}$ , following the well known equal displacement rule.

The frame is subsequently analyzed using static inelastic pushover analysis with an inverted triangle type of profile of horizontal forces. The forces are progressively increased until the maximum inelastic displacement of the frame reaches the previously computed one of 0.186m.

The damage distribution in the frame is shown in Fig. 12. It is observed that plastic hinges are formed both in beams and columns, which implies that in reality the capacity design requirement is not satisfied. Damage values are up to about 47% in the beams and up to 26% in columns (44% at their bases). The DDCD can overcome this drawback of formation of plastic hinges in the columns, because it can directly control damage and plastic hinge formation in the frame. Indeed, this frame is designed for the C.P. performance level of table

3 by assuming target damage of 45% in the beams and 0% in all columns except those of the first floor where the target damage at their bases is 40%. For this target damage distribution and design base shear computed with the aid of the EC8 [2004] spectrum, the sections of the frame are obtained. For the resulting frame the pushover curve is used to determine the elastic displacement for the aforementioned base shear. This displacement is multiplied by  $q$  in order to find the maximum inelastic one and hence the corresponding base shear from the pushover curve. For this base shear the distribution of damage is obtained. If this distribution is in accordance with the target one, the selected sections are acceptable. Otherwise, the sections are changed and the previous procedure is repeated. Thus, for the damage distribution of Fig. 13 with damage values up to about 44% in the beams and up to 37% in column bases, the column and beam sections for the three stories of the frame were found to be (HEB300-IPE330) + (HEB300-IPE330) + (HEB280-IPE300). This selection results in a global collapse mechanism satisfying completely the capacity design requirement.

## 8. Conclusions

On the basis of the preceding developments, the following conclusions can be stated:

- 1) A new design method of plane steel moment resisting frames under static loading, the Direct Damage Controlled Design (DDCD) has been developed.
- 2) The method works with the aid of the finite element method incorporating material and geometric nonlinearities, a continuum mechanics definition of damage and a damage scale derived on the basis of extensive parametric studies.
- 3) This method allows the designer to either determine the damage level for a given structure and known loading, or dimension a structure for a target damage level and known loading, or determine the maximum loading for a given structure and a target damage level.

4) The method can also be used for the case of seismic loading in the framework of the static inelastic (pushover) analysis providing a reliable way for achieving seismic capacity design.

## References

- [AISC 1998] AISC, “ *Load & Resistance Factor Design* “, Structural Members, Specifications & Codes, *American Institute of Steel Construction, Inc.*, Chicago, 1998.
- [AISC 2005] AISC, ”*Seismic Provisions for Structural Steel Buildings*”, *American Institute of Steel Construction, Inc.*, Chicago, 2002.
- [Applied Technology Council 1985] Applied Technology Council (ATC13), “Earthquake Damage Evaluation for California”, Redwood City, California, 1985.
- [Benarent-Climent 2007] Benarent-Climent A., “An energy-based damage model for seismic response of steel structures”, *Earthquake Engng. Struct. Dyn.* **36** (2007), 1049-1064.
- [Cervera et al 1995] Cervera M., Oliver J., Faria R., “Seismic evaluation of concrete dams via continuum damage models”, *Earthquake Engng Struct. Dyn.* **24** (1995), 1225-1245.
- [Chen and Kim 1997] Chen W.F. and Kim S. E., “LRFD Steel Design Using Advanced Analysis”, CRC Press, Inc., Boca Raton, Florida, USA, 1997.
- [DiPasquale and Cakmak 1990] DiPasquale E., Cakmak A. S., “Detection of seismic structural damage using parameter-based global indices”, *Probab. Engng Mech.*, **5** (1990), 60-65.
- [EC3 1992] EC3,” Design of Steel Structures – Part 1-1: General Rules for Buildings, ENV1993-1-1”, *European Committee on Standardization (CEN)*, Brussels, 1992.
- [EC8 1998] EC8, Eurocode 8, “Design of structures for earthquake resistance, Part 1: General rules, seismic actions and rules for buildings, European Standard EN 1998-1”, *European Committee for Standardization (CEN)*, Brussels, 2004.

- [FEMA 1997] FEMA-273 Building Seismic Safety Council, "NEHRP guidelines for the seismic rehabilitation of buildings", Washington (DC): Federal Emergency Management Agency, 1997.
- [FEMA 2000a] Federal Emergency Management Agency (FEMA). "Recommended seismic design criteria for new steel moment-frame buildings", Report no. FEMA-350. SAC Joint Venture; Washington D.C. 2000.
- [FEMA 2000b] Federal Emergency Management Agency (FEMA), "Recommended seismic evaluation and upgrade criteria for existing welded steel moment-frame buildings", Report no. FEMA-351. SAC Joint Venture; Washington D.C. 2000.
- [FEMA 2001] Federal Emergency Management Agency (FEMA), "HAZUS99 User's Manual", Service Release 2; Washington D.C. 2001.
- [Florez-Lopez 1998] Florez-Lopez J., "Frame analysis and continuum damage mechanics", *Europ. J. Mech.A/Solids*, **17**, (1998), 269-283.
- [Gioncu and Mazzolani 2002] Gioncu V., Mazzolani F. M., "Ductility of Seismic Resistant Steel Structures", Spon Press, London, 2002.
- [Ghoborah et al. 1999] Ghoborah A., Abou-Elfath H., Biddah A., "Response-based damage assessment of structures", *Earthquake Engng. Struct. Dyn.* **28** (1999); 79-104.
- [Hanganu et al. 2002] Hanganu A. D., Onate E., Barbat A. H., "A finite element methodology for local/global damage evaluation in civil engineering structures", *Comput.Struct.*, **80** (2002), 1667-1687.
- [Hatzigeorgiou and Beskos 2007] Hatzigeorgiou G. D., Beskos D. E., "Direct damage controlled design of concrete structures", *J. Struct. Engng.*, ASCE, **133** (2) (2007), 205-215.

- [Hatzigeorgiou et al. 2001] Hatzigeorgiou G. D., Beskos D. E., Theodorakopoulos D. D., Sfakianakis M., “A simple concrete damage model for dynamic FEM applications”, *Int. J. Comput. Engng Sci.*, **2** (2001), 267-286.
- [Kappos and Manafpour 2001] Kappos A. J., Manafpour A., “Seismic design of R/C buildings with the aid of advanced analytical techniques”, *Engng Struct.*, **23** (2001), 319–332.
- [Karavasilis et al. 2007] Karavasilis, T. L., Bazeos, N., Beskos, D. E., “Behavior factor for performance-based seismic design of plane steel moment resisting frames”, *Journal of Earthquake Engineering*, **11 (4)** (2007), 531-559.
- [Leelataviwat et al. 1999] Leelataviwat S., Goel S. C., Stojadinović B. “Toward Performance-Based Seismic Design of Structures”, *Earthquake Spectra*, **15 (3)** (1999), 435-461.
- [Lemaitre 1992] Lemaitre J. “A Course on Damage Mechanics”, Springer-Verlag, Berlin, 1992.
- [Park and Ang 1985] Park Y. J., Ang A.H.S., “Mechanistic seismic damage model for reinforced concrete”, *J. Struct. Engng., ASCE*, **111** (4) (1985); 722-739.
- [Powell and Allahabadi 1988] Powell G. H. , Allahabadi R., “Seismic damage prediction by deterministic methods: concepts and procedures”, *Earthquake Engng Struct. Dyn.*, **16** (1988), 719-734.
- [Prakash et al. 1993] Prakash V., Powell G. H., Campell S. “*DRAIN-2DX*, Base program description and user guide”, *version 1.10,1993*, University of California at Berkeley.
- [Priestley et al. 2007] Priestley M.J.N., Calvi G.M. and Kowalsky M.J. “Displacement-Based Seismic Design of Structures”, IUSS Press, Pavia, Italy, 2007.
- [SAP2000 2005] SAP2000, “Static and Dynamic Finite Element Analysis of Structures”, *Vers. 9.1.4*, Computers and Structures Inc., Berkeley, California, 2005.



[SEAOC 1999] SEAOC, “Recommended Lateral Force Requirements and Commentary”, 7<sup>th</sup> edition, Seismology Committee, Structural Engineers Association of California, Sacramento, CA, 1999

[Vasilopoulos et al. 2008] Vasilopoulos , A. A., Bazeos N., Beskos D. E., “Seismic design of irregular space steel frames using advanced methods of analysis”, *Steel and Composite Structures*, **8** (2008), 53-83.

[Vasilopoulos and Beskos 2006] Vasilopoulos A. A., Beskos D. E., “Seismic design of plane steel frames using advanced methods of analysis”, *Soil Dyn. Earthquake Engng*, **26** (2006), 1077–1100.

**GEORGE S. KAMARIS:** kamaris@upatras.gr

Department of Civil Engineering, University of Patras, GR-26500 Patras, Greece.

**GEORGE D. HATZIGEORGIU:** gchatzig@env.duth.gr

Department of Environmental Engineering, Democritus University of Thrace, GR-67100 Xanthi, Greece.

**DIMITRI E. BESKOS:** d.e.beskos@upatras.gr

Department of Civil Engineering, University of Patras, GR-26500 Patras, Greece.

CAPTIONS OF FIGURES	
1.	Stress-strain relation for steel
2.	Cross section of a damaged material
3.	Damage-strain curve for steel
4.	Section damage definition
5.	Ds versus $\theta_{pl}/\theta_y$ curves for low rise frames
6.	Ds versus $\theta_{pl}/\theta_y$ curves for high rise frames
7.	D <sub>O</sub> versus IDR curves for low rise frames
8.	D <sub>O</sub> versus IDR curves for high rise frames
9.	The flow chart of the modified program DRAIN-2DX
10.	Fiber modeling of a general section
11.	Geometry and loads for the frame of example 7.1
12.	Distribution of damage in the frame of example 7.2 designed according to EC3 [1998] and EC8 [2004]
13.	Distribution of damage in the frame of example 7.2 designed according to DDCCD

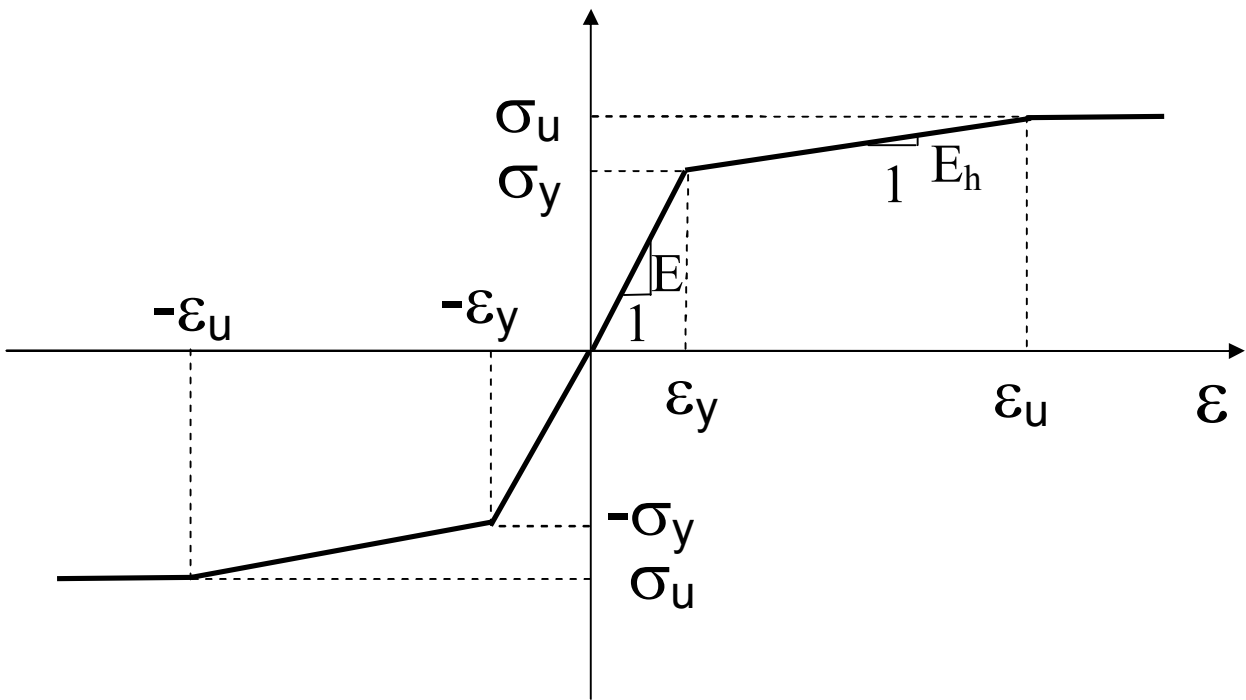


Figure 1

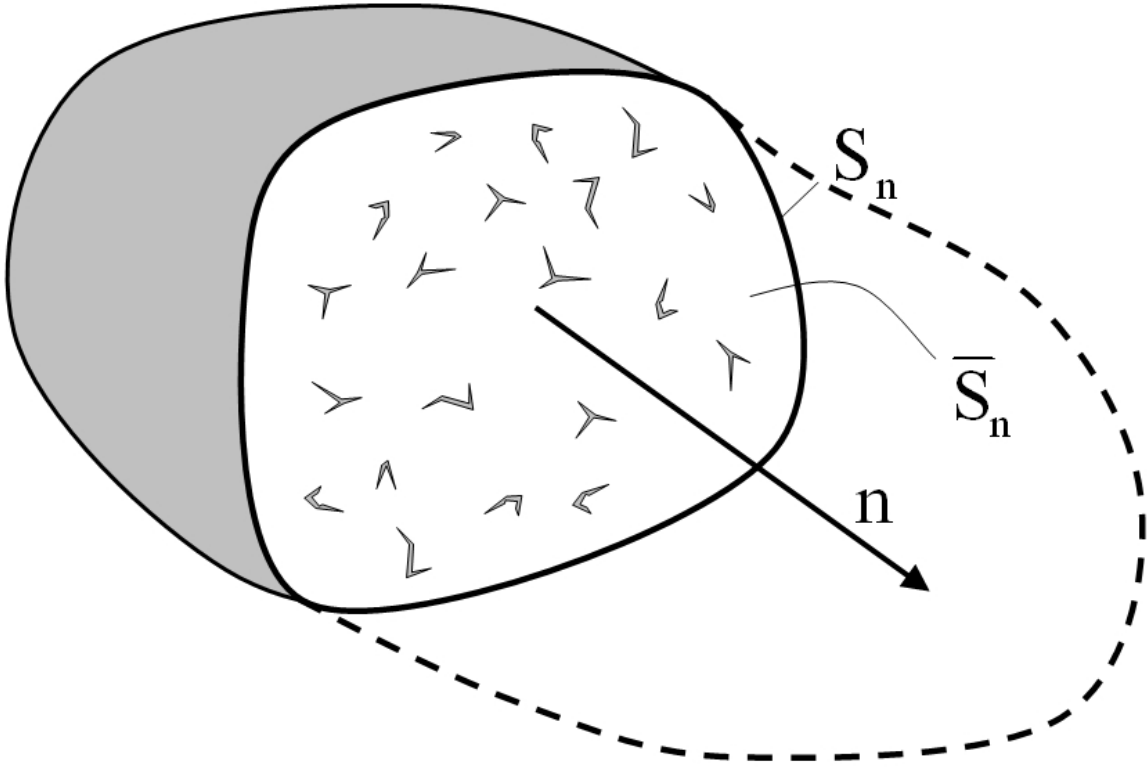
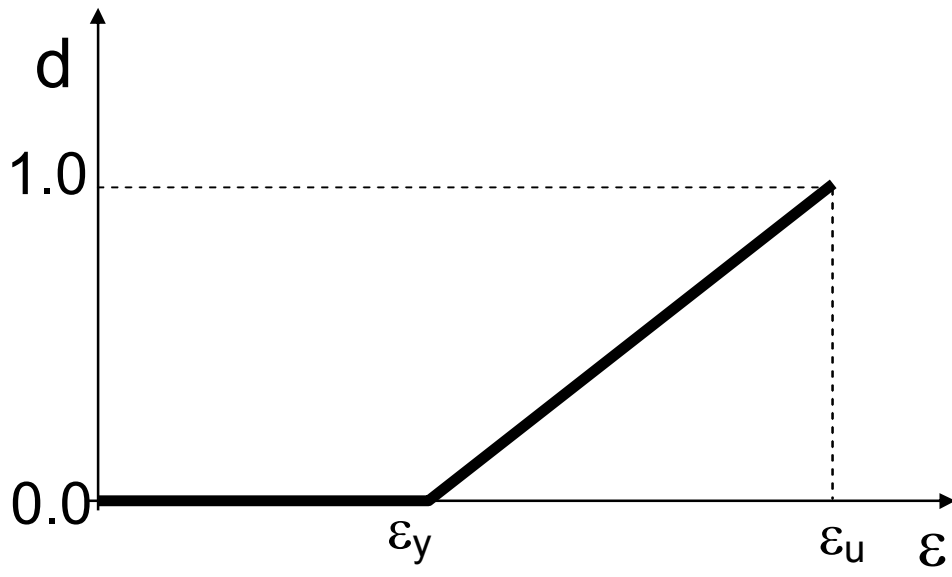


Figure 2



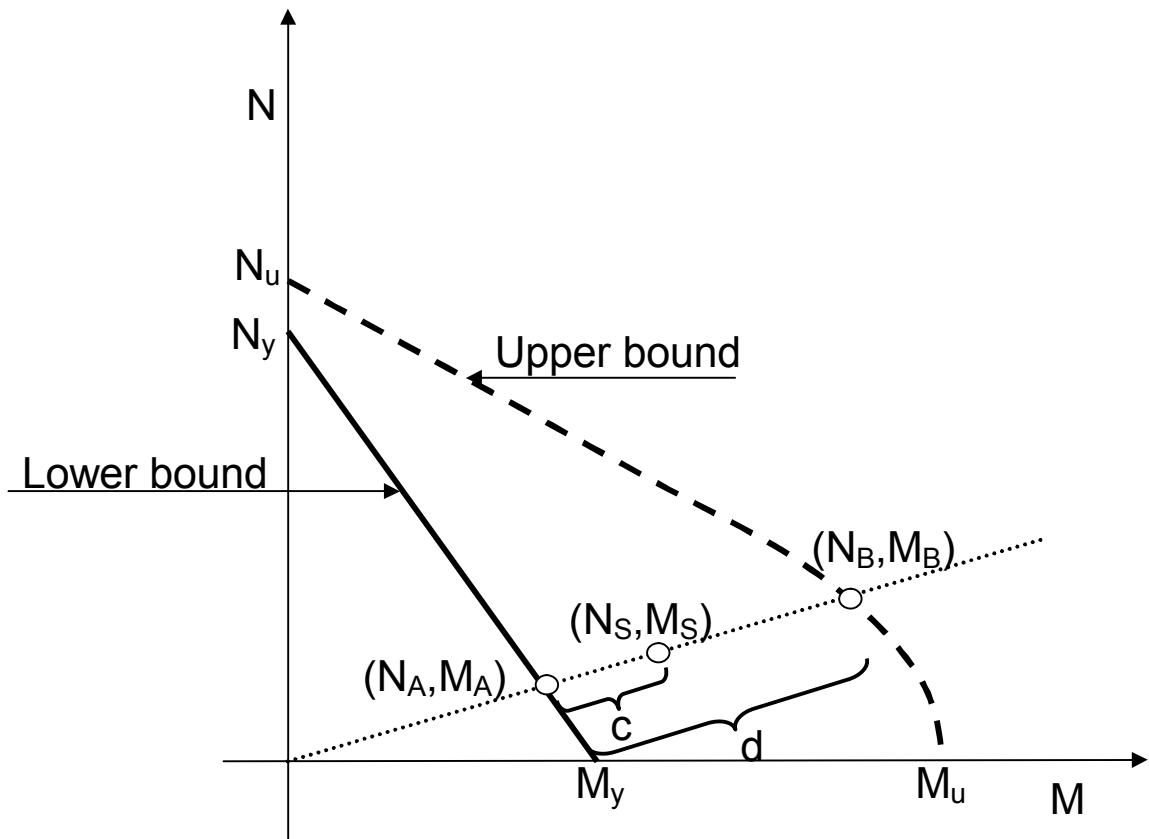


Figure 4

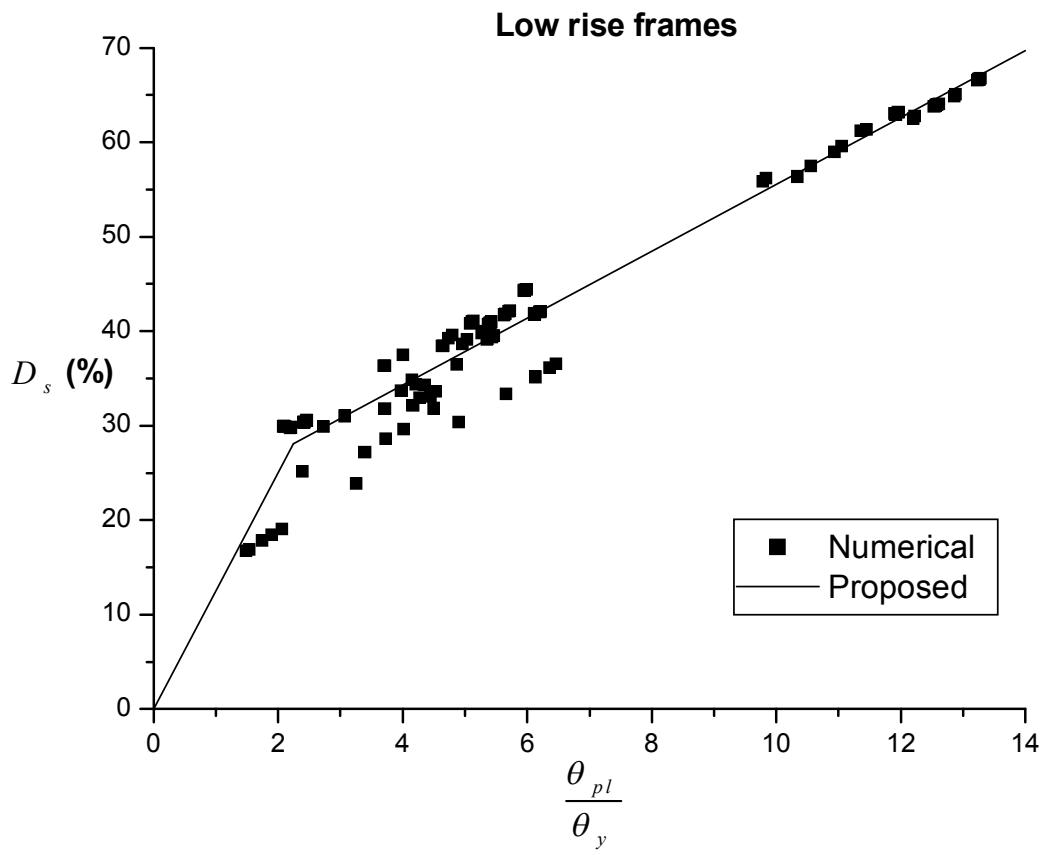


Figure 5

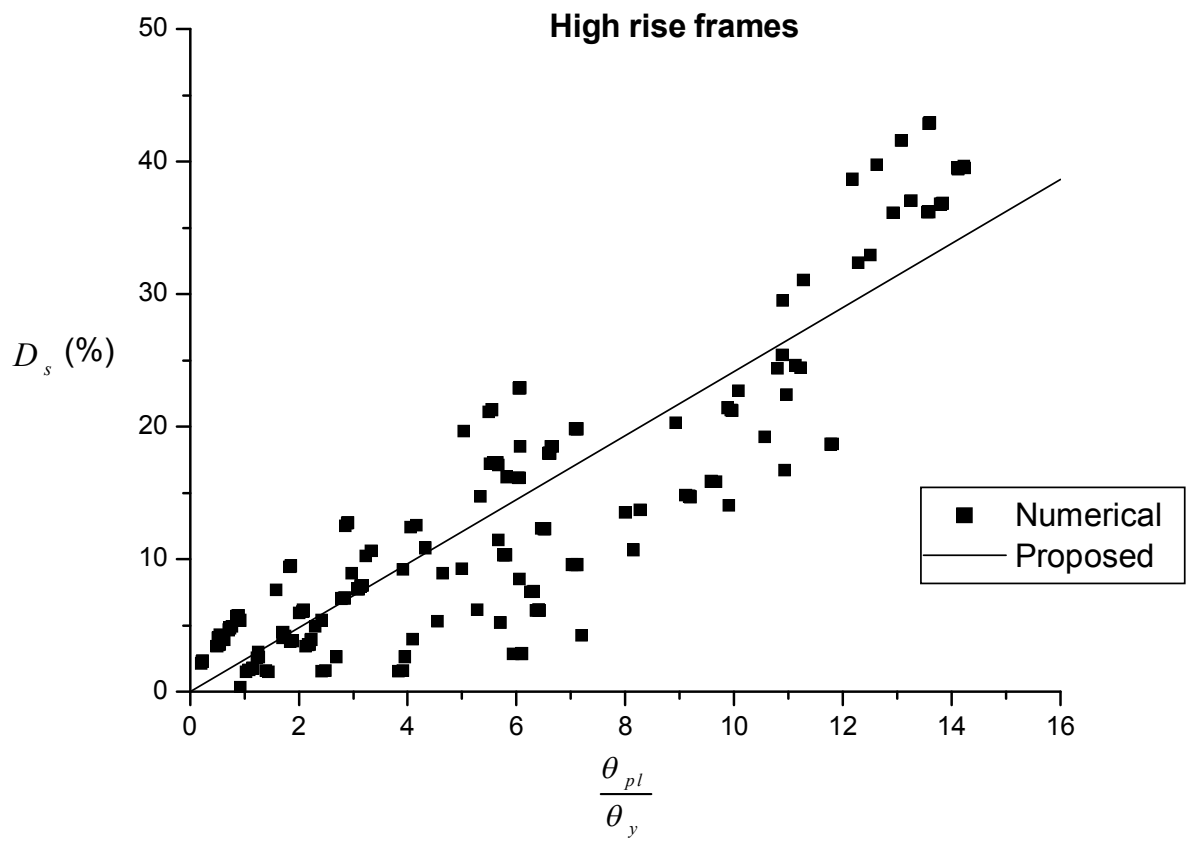
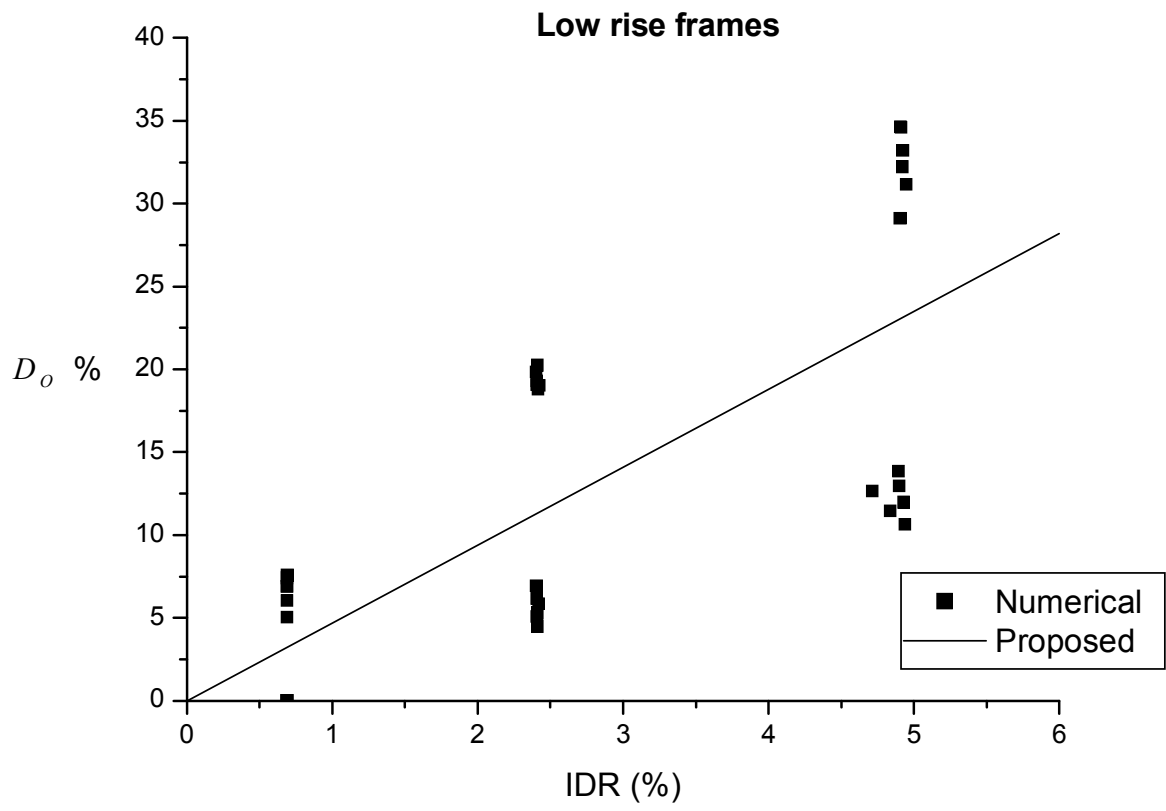


Figure 6





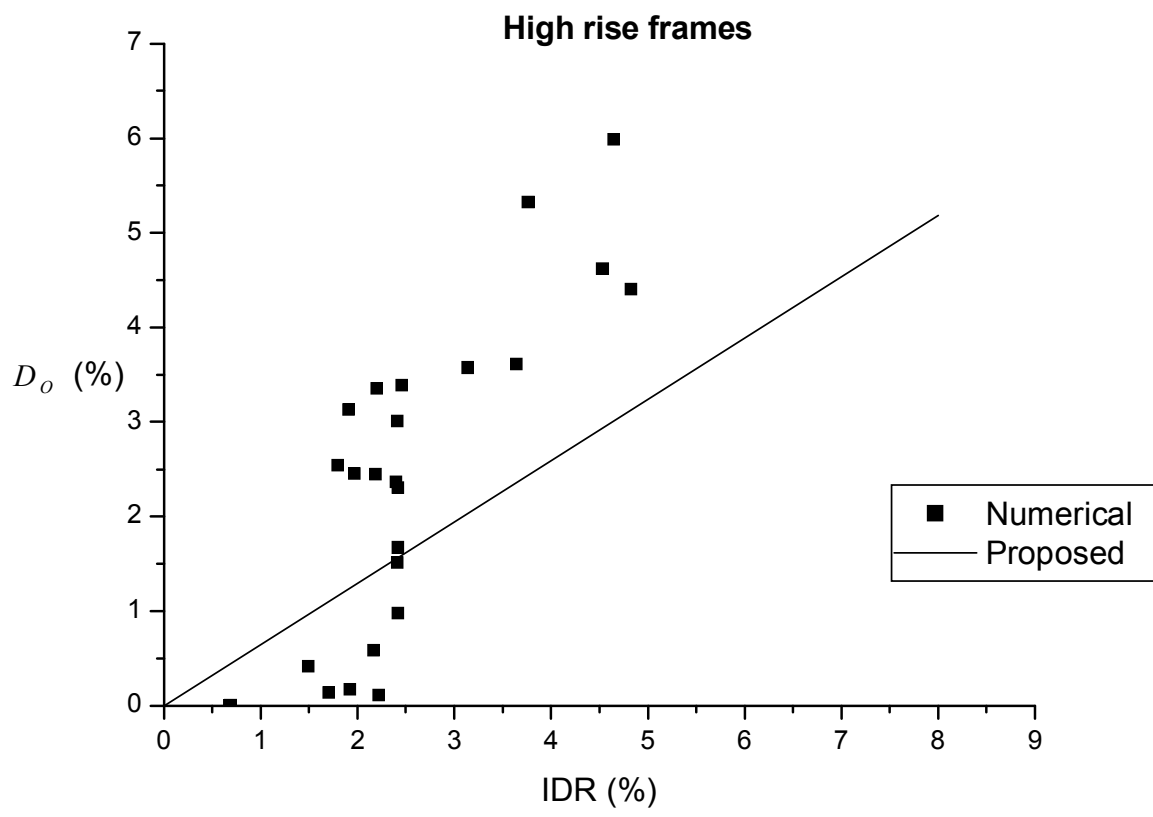


Figure 8

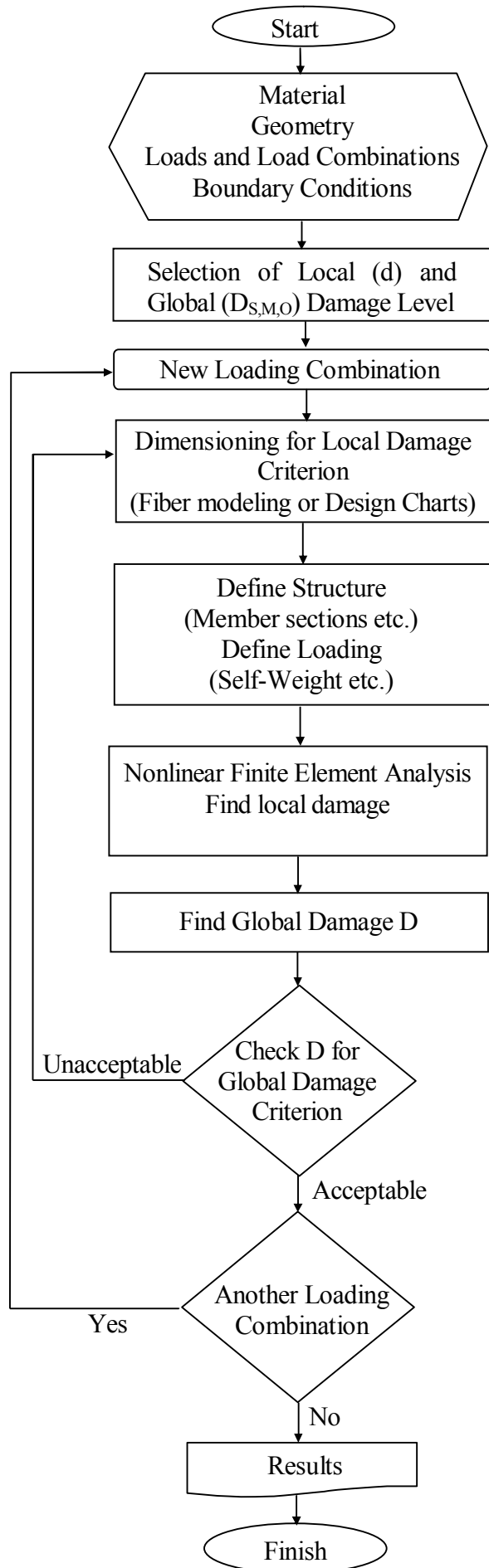


Figure 9

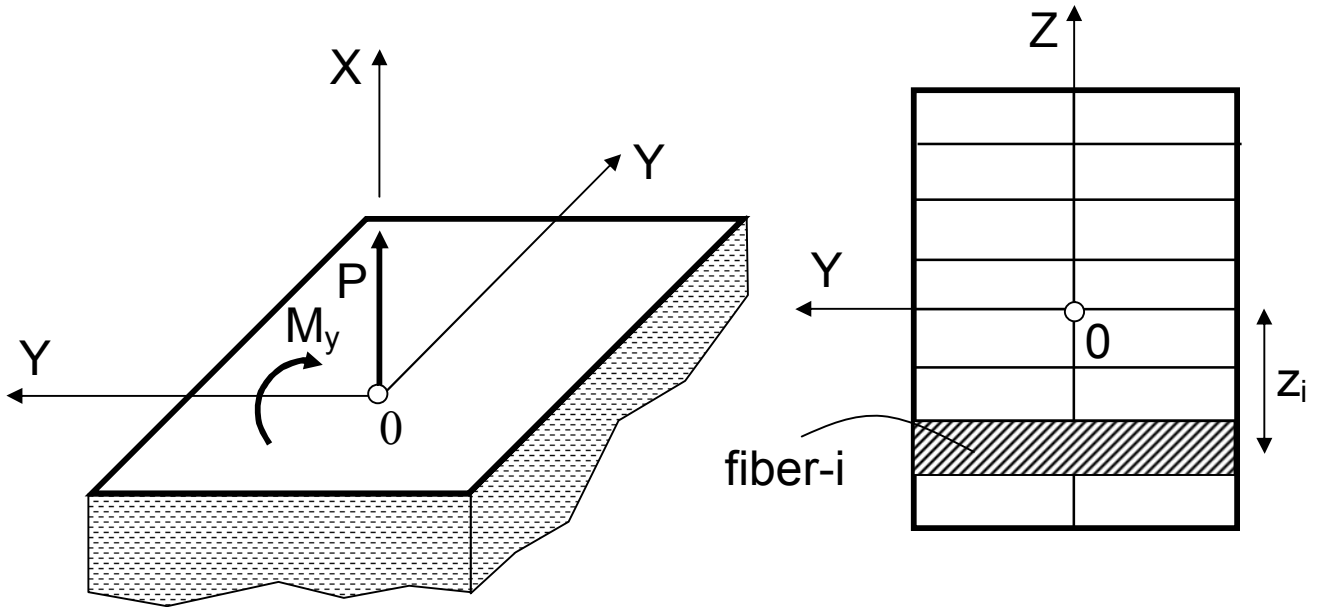


Figure 10

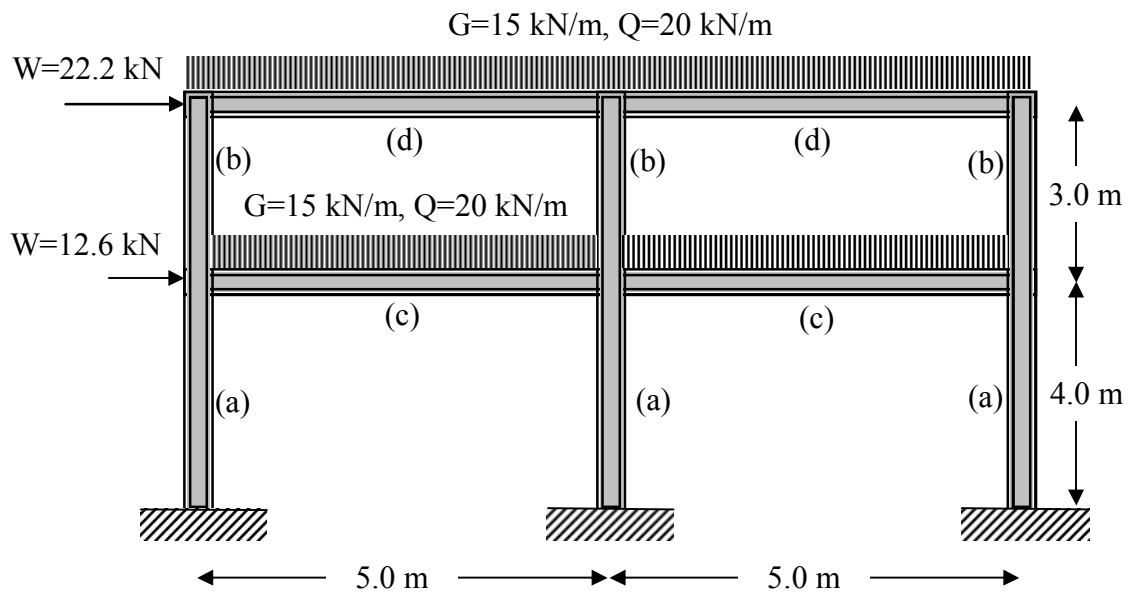


Figure 11

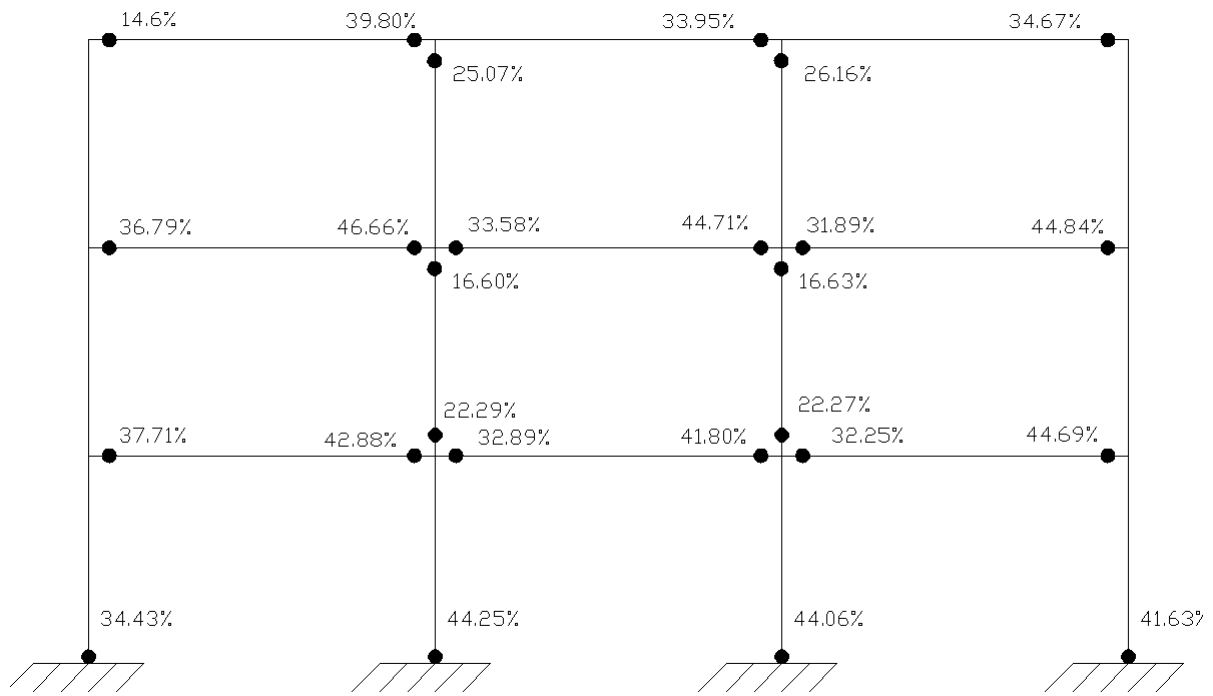


Figure 12

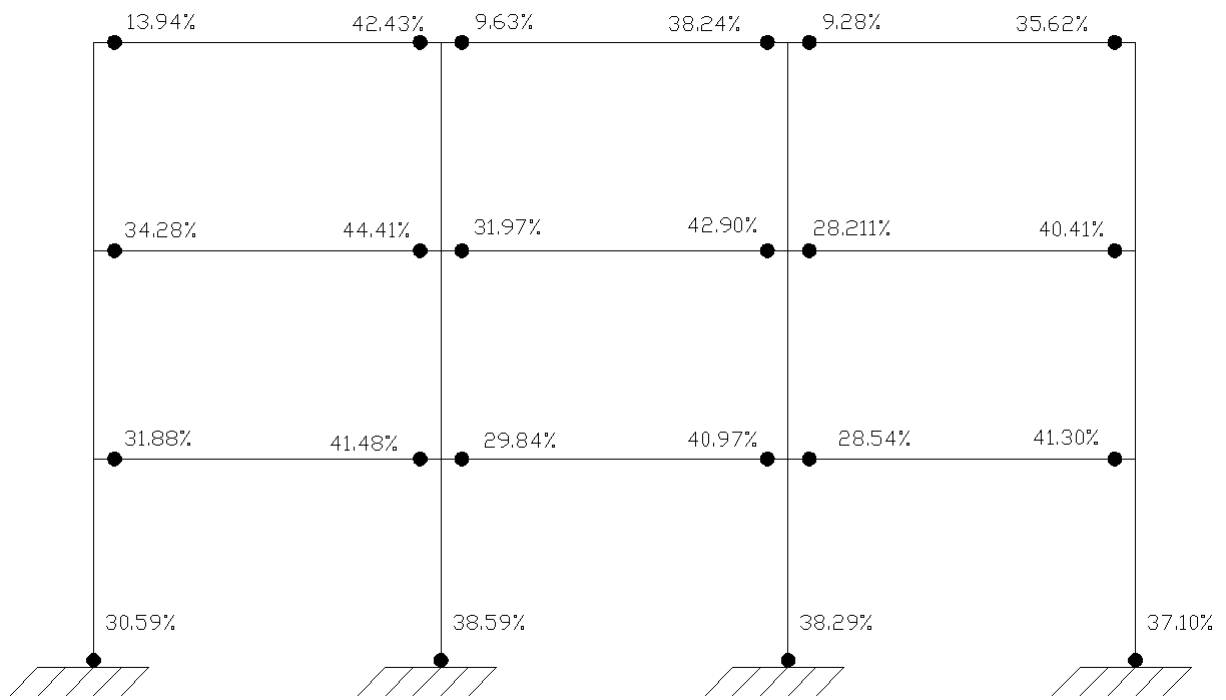


Figure 13

**TABLE 1 : Performance levels and corresponding limit response values given by several authors.**

Performance Levels	IDR	$\theta_{pl}$	$\mu_{\theta}$	Damage
I.O.	1-2% Leelataviwat et al. [1999] 1.5% SEAOC [1999] 0.5% Vasilopoulos et al. [2006] 0.7 % transient negligible permanent FEMA-273 [1997]	$\leq \theta_y$ (FEMA273) [1997]	2 (FEMA273) [1997]	$\leq 5\%$ Vasilopoulos et al.[2006] 0.1-10% ATC13[1985]
L.S.	2-3% Leelataviwat et al. [1999] 3.2 % SEAOC [1999] 1.5% Vasilopoulos et al. [2006] 2.5 % transient 1% permanent FEMA-273[1997]	$\leq 6\theta_y$ (FEMA273) [1997]	7 (FEMA273) [1997]	$\leq 20\%$ Vasilopoulos et al.[2006] 10-30% ATC13[1985]
C.P.	3-4% Leelataviwat et al. [1999] 3.8%SEAOC [1999] 3% Vasilopoulos et al.[2006] 5 % transient 5% permanent FEMA-273[1997]	$\leq 8\theta_y$ (FEMA273) [1997]	9 (FEMA273) [1997]	$\leq 50\%$ Vasilopoulos et al.[2006] 30-60% ATC13[1985]



**TABLE 2 : Steel moment resisting frames considered in parametric studies**

General data			Sections	Periods	
Frame	$n_s$	$n_b$	Columns: (HEB) & Beams: (IPE)	$T_1(\text{sec})$	$T_2(\text{sec})$
1	3	3	240-330(1-3)	0.73	0.26
2	3	3	260-330(1-3)	0.69	0.21
3	3	3	280-330(1-3)	0.65	0.19
4	3	6	240-330(1-3)	0.75	0.23
5	3	6	260-330(1-3)	0.70	0.21
6	3	6	280-330(1-3)	0.66	0.20
7	6	3	280-360(1-4)+260-330(5-6)	1.22	0.41
8	6	3	300-360(1-4)+280-330(5-6)	1.17	0.38
9	6	3	320-360(1-4)+300-330(5-6)	1.13	0.37
10	6	6	280-360(1-4)+260-330(5-6)	1.25	0.42
11	6	6	300-360(1-4)+280-330(5-6)	1.19	0.40
12	6	6	320-360(1-4)+300-330(5-6)	1.15	0.38
13	9	3	340-360(1)+340-400(2-5)+320-360(6-7)+300-330(8-9)	1.55	0.54
14	9	3	360-360(1)+360-400(2-5)+340-360(6-7)+320-330(8-9)	1.52	0.53
15	9	3	400-360(1)+400-400(2-5)+360-360(6-7)+340-330(8-9)	1.46	0.51
16	9	6	340-360(1)+340-400(2-5)+320-360(6-7)+300-330(8-9)	1.57	0.55
17	9	6	360-360(1)+360-400(2-5)+340-360(6-7)+320-330(8-9)	1.53	0.53
18	9	6	400-360(1)+400-400(2-5)+360-360(6-7)+340-330(8-9)	1.47	0.51
19	12	3	400-360(1)+400-400(2-3)+400-450(4-5)+360-400(6-7)+340-400(8-9)+340-360(10)+340-330(11-12)	1.90	0.66
20	12	3	450-360(1)+450-400(2-3)+450-450(4-5)+400-450(6-7)+360-400(8-9)+360-360(10)+360-330(11-12)	1.78	0.62
21	12	3	500-360(1)+500-400(2-3)+500-450(4-5)+450-450(6-7)+400-400(8-9)+400-360(10-11)+400-330(12)	1.72	0.60
22	12	6	400-360(1)+400-400(2-3)+400-450(4-5)+360-400(6-7)+340-400(8-9)+340-360(10)+340-330(11-12)	1.90	0.67
23	12	6	450-360(1)+450-400(2-3)+450-450(4-5)+400-450(6-7)+360-400(8-9)+360-360(10)+360-330(11-12)	1.78	0.63
24	12	6	500-360(1)+500-400(2-3)+500-450(4-5)+450-450(6-7)+400-400(8-9)+400-360(10-11)+400-330(12)	1.72	0.61
25	15	3	500-300(1)+500-400(2-3)+500-450(4-5)+450-400(6-7)+400-400(8-12)+400-360(13-14)+400-330(15)	2.29	0.78
26	15	3	550-300(1)+550-400(2-3)+550-450(4-5)+500-400(6-7)+450-400(8-12)+450-360(13-	2.22	0.75

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			14)+450-330(15)		
27	15	3	600-300(1)+600-400(2-3)+600-450(4-5)+550-450(6-7)+500-450(8-9)+500-400(10-12)+500-360(13-14)+500-330(15)	2.10	0.72
28	15	6	500-300(1)+500-400(2-3)+500-450(4-5)+450-400(6-7)+400-400(8-12)+400-360(13-14)+400-330(15)	2.30	0.78
29	15	6	550-300(1)+550-400(2-3)+550-450(4-5)+500-400(6-7)+450-400(8-12)+450-360(13-14)+450-330(15)	2.21	0.75
30	15	6	600-300(1)+600-400(2-3)+600-450(4-5)+550-450(6-7)+500-450(8-9)+500-400(10-12)+500-360(13-14)+500-330(15)	2.10	0.72
31	20	3	600-300(1)+600-400(2-3)+600-450(4-5)+550-450(6-10)+500-450(11-13)+500-400(14-16)+450-400(17)+450-360(18-19)+450-330(20)	2.82	0.97
32	20	3	650-300(1)+650-400(2-3)+650-450(4-5)+600-450(6-10)+550-450(11-13)+550-400(14-16)+500-400(17)+500-360(18-19)+500-330(20)	2.76	0.94
33	20	3	700-300(1)+700-360(2)+700-400(3)+700-450(4-5)+650-450(6-10)+600-450(11-13)+600-400(14-16)+550-400(17)+550-360(18-19)+550-330(20)	2.73	0.93
34	20	6	600-300(1)+600-400(2-3)+600-450(4-5)+550-450(6-10)+500-450(11-13)+500-400(14-16)+450-400(17)+450-360(18-19)+450-330(20)	2.75	0.96
35	20	6	650-300(1)+650-400(2-3)+650-450(4-5)+600-450(6-10)+550-450(11-13)+550-400(14-16)+500-400(17)+500-360(18-19)+500-330(20)	2.70	0.93
36	20	6	700-300(1)+700-360(2)+700-400(3)+700-450(4-5)+650-450(6-10)+600-450(11-13)+600-400(14-16)+550-400(17)+550-360(18-19)+550-330(20)	2.67	0.92

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**TABLE 3 : Performance levels and corresponding section and structural damage.**

Performance Levels	D <sub>s</sub>		D <sub>o</sub>	
	Low rise frames	High rise frames	Low rise frames	High rise frames
I.O.	≤13%	≤3%	≤3%	≤1%
L.S.	≤40%	≤15%	≤12%	≤2%
C.P.	≤50%	≤20%	≤24%	≤5%

**TABLE 4: Design of 2-D frame**

Member		EC3			Proposed method - DDCD	
		Sections	Capacity ratio	Damage	Sections	Damage
columns	(a)	HEB-180	0.742	0.0 %	HEB-160	0.0%
	(b)	HEB-140	0.821	0.0 %	HEB-140	24.3 %
beams	(c)	IPE-360	0.686	0.0 %	IPE-240	73.7 %
	(d)	IPE-330	0.842	0.0 %	IPE-270	20.0 %