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Mass-Discrepancy Acceleration Relation: A Natural Outcome of Galaxy Formation in Cold Dark Matter Halos

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We analyze the total and baryonic acceleration profiles of a set of well-resolved galaxies identified in the EAGLE suite of hydrodynamic simulations. Our runs start from the same initial conditions but adopt different prescriptions for unresolved stellar and active galactic nuclei feedback, resulting in diverse populations of galaxies by the present day. Some of them reproduce observed galaxy scaling relations, while others do not. However, regardless of the feedback implementation, all of our galaxies follow closely a simple relationship between the total and baryonic acceleration profiles, consistent with recent observations of rotationally supported galaxies. The relation has small scatter: Different feedback implementations—which produce different galaxy populations—mainly shift galaxies along the relation rather than perpendicular to it. Furthermore, galaxies exhibit a characteristic acceleration g_{\dagger} , above which baryons dominate the mass budget, as observed. These observations, consistent with simple modified Newtonian dynamics, can be accommodated within the standard cold dark matter paradigm.

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In the cold dark matter (CDM) cosmological model, structures form hierarchically through merging and smooth accretion (e.g., [1]). The resulting “dark matter (DM) halos” trap gas which cools and forms stars, providing visible tracers of the underlying DM density field [2,3]. Understanding the connection between galaxies and their halos is therefore of fundamental importance to galaxy formation models.

Galaxy formation occurs over a broad range of scales, which hampers theoretical progress. Even the most sophisticated numerical simulations available are unable to resolve all relevant scales simultaneously and must resort to “subgrid” models that account for unresolved physical process, such as feedback from stars and black holes (e.g., [4–7]). Subgrid models are ubiquitous in areas of science that probe multiscale phenomena. They are essential ingredients in, for example, climate or atmospheric models and simulations of turbulent flows.

Traditionally, the link between galaxies and halos has been expressed in terms of scaling relations between their structural properties; the Tully-Fisher [8] and Faber-Jackson [9] relations, in particular, relate the luminosity

(or stellar mass) of a galaxy to its dynamics which, in CDM, is largely governed by its DM halo. Galaxy formation models based on CDM do not reproduce these relations unless subgrid models for unresolved feedback are calibrated to form realistic galaxies when judged according to other diagnostics (e.g., [10,11]). It comes as a surprise, then, that observations reveal an even closer coupling between the luminous mass of galaxies and their total *dynamical* mass. Perhaps most unexpected is the “mass-discrepancy acceleration relation” (MDAR) [12–14], a tight empirical relation between the radial dependence of the enclosed baryonic-to-dynamical mass ratio and the baryonic acceleration. It has small intrinsic scatter and holds for galaxies of widely varying luminosity and gas fraction. The MDAR may be expressed empirically as [15]

$$\frac{g_{\text{tot}}(r)}{g_{\text{bar}}(r)} = \frac{M_{\text{tot}}(r)}{M_{\text{bar}}(r)} = \frac{1}{1 - e^{-\sqrt{g_{\text{bar}}/g_{\dagger}}}}, \quad (1)$$

where $g_i(r)$ and $M_i(r)$ are, respectively, the acceleration and enclosed mass profiles.

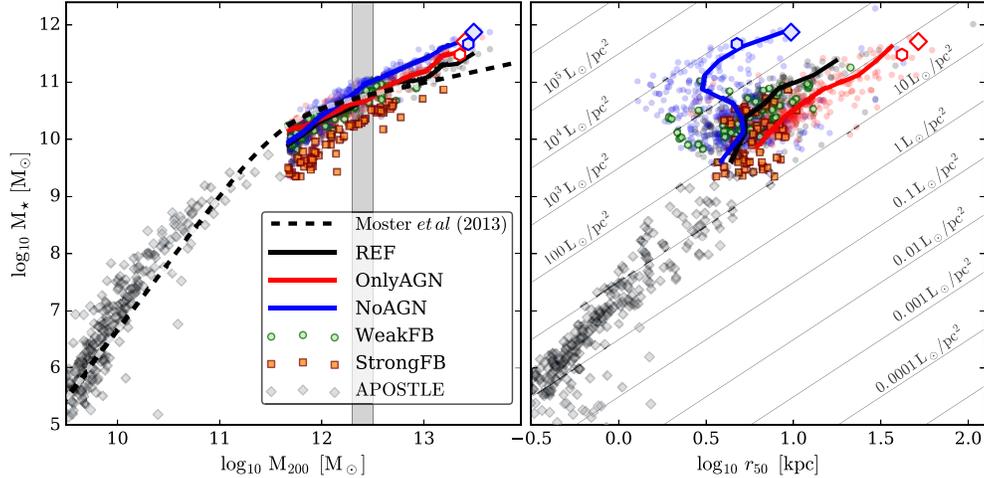


FIG. 1. Stellar mass versus halo virial mass (left) and stellar half-mass radius (right). Solid black lines show the median trends for the “REF” model; blue and red lines show, respectively, the variations if feedback is entirely limited to active galactic nuclei (AGN) (OnlyAGN) or to stars (NoAGN). Semitransparent dots of the same color show individual halos. Individual halos are also shown for runs with strong (StrongFB, orange squares) and weak (WeakFB, green circles) stellar feedback and for APOSTLE galaxies (diamonds). The dashed line in the left panel plots the $M_{\star} - M_{\text{halo}}$ relation derived from abundance matching (see [31] for details). Lines of constant effective surface brightness are plotted in the right-hand panel. The outsized blue and red symbols identify the two halos shown in Fig. 2.

It has been claimed (see [16] and the discussion therein) that the small scatter in the MDAR is inconsistent with hierarchical galaxy formation models, in which galaxies exhibit a broad range of properties even for halos of fixed mass. Furthermore, the MDAR implies a *characteristic* acceleration ($g_{\dagger} \approx 10^{-10} \text{ m s}^{-2}$), above which each galaxy’s dynamics can be determined by the observed light alone.

Why would baryons and dark matter “conspire” to produce a characteristic physical scale? One possibility is that galaxies adhere to *modified Newtonian dynamics* (although see [17,18] for an explanation within the CDM framework). However, theoretical studies suggest that the MDAR arises naturally in CDM models of galaxy formation, provided they also match observed galaxy scaling relations [19–23]. In this Letter, we address these issues using a suite of simulations drawn from the EAGLE project [6]. Our simulations vary the subgrid feedback in a way that modifies the end product of galaxy formation, enabling us to robustly assess the MDAR for a range of galaxy formation “models.”

The EAGLE simulations.—Our analysis focuses on halos and their central galaxies identified in a subset of the “intermediate resolution” EAGLE simulations [6,24]. These include periodic volumes of side length $L_{\text{cube}} = 25$ and 50 comoving Mpc sampled with, respectively, $N = 376^3$ and 752^3 particles of gas and DM. The respective particle masses are $m_g = 1.81 \times 10^6 M_{\odot}$ and $m_{\text{DM}} = 9.70 \times 10^6 M_{\odot}$; the (Plummer-equivalent) softening length is $\epsilon = 0.7$ physical kpc below $z = 2.8$ and 2.66 comoving kpc at a higher redshift. Each volume was also carried out using only DM, with $\Omega'_M = \Omega_M + \Omega_{\text{bar}}$ and $\Omega'_{\text{bar}} = 0$. In all runs, DM particles were assigned unique integer IDs; we use the same IDs for particles in runs that start from the same ICs. DM halos can then be matched across different simulations by identifying halos with common DM particles.

Cosmological parameters are those inferred by the Planck Collaboration [25].

The simulations were performed with a version of the N -body hydrodynamics code GADGET3 [26] incorporating a modified hydrodynamic scheme, time-stepping criteria, and subgrid physics modules (see [6] for details). Runs of a given box size start from the same initial conditions but adopt different values of the subgrid parameters. As a result, some accurately reproduce a diverse set of observations of the galaxy population (such as the stellar mass function, galaxy shapes, and their relationship to stellar mass), whereas others do not.

As discussed by Ref. [6], calibration of the subgrid parameters must be carried out so that simulations reproduce a diagnostic set of observational data. For EAGLE, this was achieved by calibrating the feedback models (including contributions from both AGN and stars) so that the observed galaxy stellar mass function and the mass-size relation were recovered. One such model is the “reference” model (hereafter REF [6]). Variations of REF systematically changing the subgrid parameters were also carried out [24]. These include runs with weak (WeakFB) or strong (StrongFB) stellar feedback, one with no AGN feedback (NoAGN), and another with *only* AGN feedback but none from stars (OnlyAGN). The resulting galaxy properties depend sensitively on these feedback choices.

Analysis: Halo finding and selection.—We use SUBFIND [27,28] to identify DM halos and their *central* galaxies (see [6] for details). The position of the halo particle with the minimum potential energy defines the halo and galaxy center. The halo’s virial mass M_{200} is defined as that enclosed by a sphere of mean density $200 \times \rho_{\text{crit}}$ surrounding each halo center, where $\rho_{\text{crit}} = 3H_0^2/8\pi G$ is the critical density. This implicitly defines the virial radius through

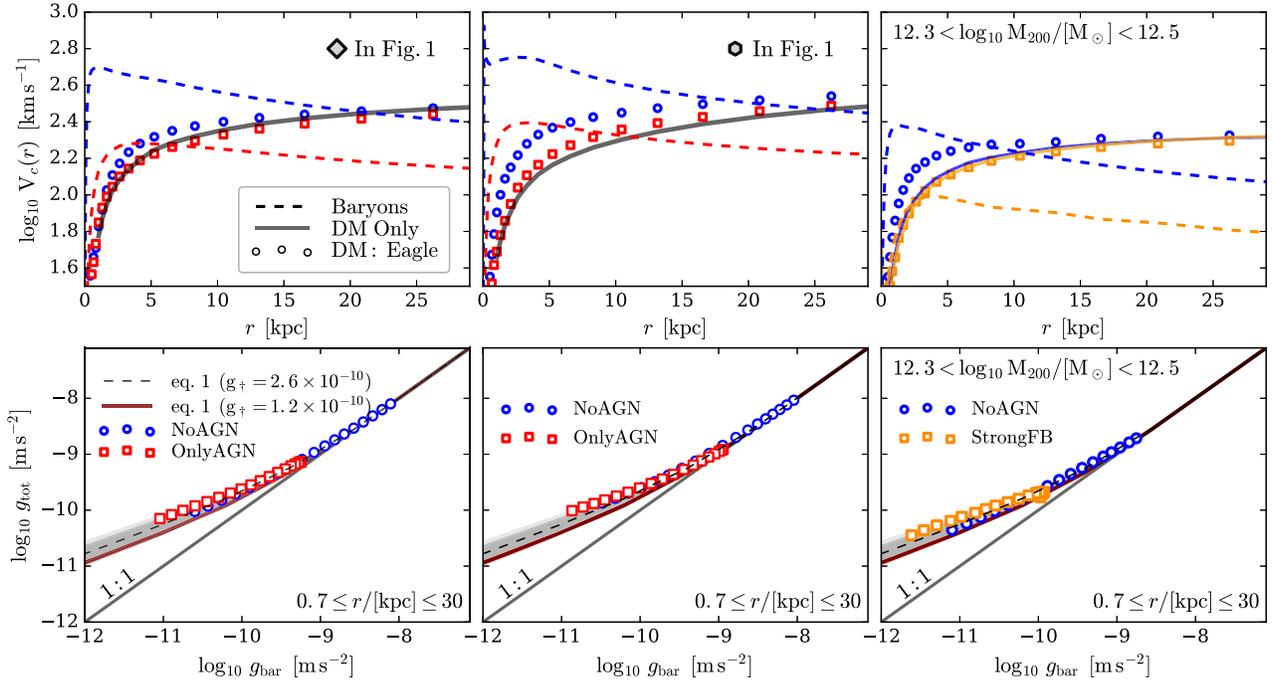


FIG. 2. Circular velocity (upper panels) and acceleration profiles (lower panels) for galaxies highlighted in Fig. 1. The left and middle panels correspond to individual halos cross-matched between the NoAGN (blue) and OnlyAGN (red) models; the rightmost panels compare the *median* profiles for halos in NoAGN (blue) and StrongFB (yellow) that fall in the narrow mass range $12.3 \leq \log_{10} M_{200}/[M_{\odot}] \leq 12.5$ (vertical shaded band in Fig. 1). The baryonic circular velocity profiles (upper panels) are shown using dashed lines; symbols indicate that of DM. [For comparison, solid black lines show the $V_c^{\text{DM}}(r)$ profiles for the same halo identified in the corresponding DM-only simulation.] Lower panels show the acceleration diagrams. The linear scaling is shown as a solid black line and Eq. (1) (using $g_{\ddagger} = 2.6 \times 10^{-10} \text{ m s}^{-2}$) as a dashed line; shaded regions indicate the scatter brought about by increasing or decreasing the enclosed baryon mass by factors of 3 (light) and 2 (dark). For comparison, we also show Eq. (1) with $g_{\ddagger} = 1.2 \times 10^{-10} \text{ m s}^{-2}$ (brown line), consistent with the observational result of Ref. [15].

$M_{200} = (800/3)\pi r_{200}^3 \rho_{\text{crit}}$. We focus our analysis on central galaxies whose DM halos are resolved with at least $N(<r_{200}) \geq 5 \times 10^4$ particles. We impose no isolation or relaxation criteria.

We also include *isolated* galaxies (that lie beyond $2 \times r_{200}$ from any halo with $M_{200} > 5 \times 10^{11} M_{\odot}$ but within 3 Mpc from their barycenter) identified in the level-1 APOSTLE simulations (see [29,30] for details of the APOSTLE project), which used the EAGLE subgrid model with REF parameters. In total, our galaxies span the (stellar) mass range $10^5 \lesssim M/M_{\odot} \lesssim 10^{12}$.

Radial mass profiles of baryons and dark matter.—The acceleration profile due to component i is computed as

$$g_i(r) = \frac{GM_i(r)}{r^2} \equiv \frac{V_c^i(r)^2}{r}, \quad (2)$$

where $V_c^i(r)$ and $M_i(r)$ are the corresponding circular velocity and enclosed mass profiles and G is Newton's constant. We compute $M_i(r)$ using logarithmically spaced radial bins with a fixed separation, $\Delta \log_{10} r = 0.1$, spanning $r_{\text{min}} = \epsilon$ (the minimum resolved spatial scale) to $r_{\text{max}} = 0.15 \times r_{200}$ (this aperture encloses, on average, $\gtrsim 95\%$ of a galaxy's stellar mass; we have verified that our results are robust to reasonable changes in r_{max}).

For each galaxy we also record a few diagnostic quantities. Its stellar mass M_{\star} is defined as the total mass of stars *gravitationally bound* to the central galaxy; the stellar half-mass radius r_{50} is defined by $M(r_{50})/M_{\star} = 1/2$.

Results.—The leftmost panel in Fig. 1 plots the galaxy stellar mass versus the halo virial mass. Solid lines show the median trends for the 50 Mpc cubes (REF, NoAGN, and OnlyAGN). Individual galaxies are shown as faint circles of corresponding color. Additional runs with strong and weak stellar feedback are also shown, along with APOSTLE galaxies (in these cases, only individual halos are plotted). The dashed line shows the relation inferred from abundance matching on data by Ref. [31]. The right-hand panel shows, using the same color scheme, the stellar mass versus half the (stellar) mass radius. The diagonals indicate lines of constant surface brightness.

Different subgrid models produce different galaxy populations. For a given halo mass, the median galaxy *stellar mass* spans a factor of ≈ 4 between the extremes (compare NoAGN and StrongFB in the leftmost panel). Galaxy sizes also differ, particularly for the runs without (NoAGN) and with *only* (OnlyAGN) AGN feedback. For $M_{\star} \gtrsim 10^{11} M_{\odot}$, for example, galaxy half-mass radii are roughly an order of magnitude smaller when AGN feedback is ignored.

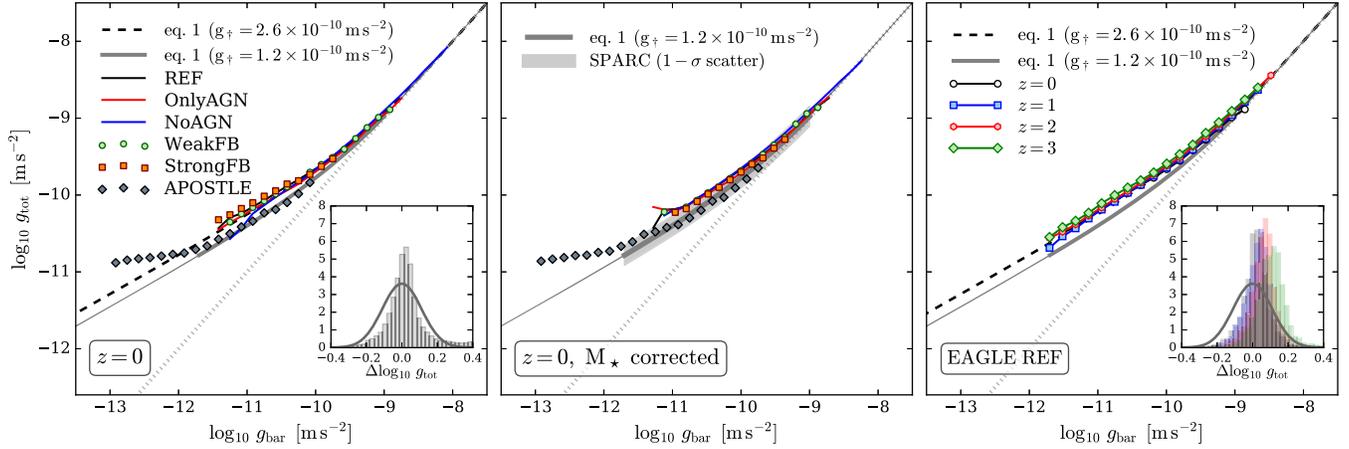


FIG. 3. Total acceleration profiles for all halos as a function of their baryonic acceleration. The left panel shows results for all halos in all simulations at $z = 0$. Lines, points, and colors have the same meaning as in Fig. 1. The right-hand panel shows (for REF) the redshift evolution for progenitor galaxies. The dashed lines in the left- and right-hand panels show Eq. (1) with $g_{\dagger} = 2.6 \times 10^{-10} \text{ m s}^{-2}$. Inset panels show the relative scatter around this curve after combining all simulations (left) and for individual redshifts (right); the solid lines represent the observational scatter in Ref. [15]. The middle panel plots the $g_{\text{obs}} - g_{\text{bar}}$ relation after rescaling galaxy stellar masses so that they fall on the abundance matching relation shown in Fig. 1 (left). The thick gray line and shaded band indicate the mean trend and scatter, respectively, obtained by Ref. [15] from observations of rotationally supported galaxies.

Figure 2 (upper panels) provides a few examples of the circular velocity profiles of baryons (dashed curves) and dark matter (open symbols) for several EAGLE galaxies. The left and middle panels show two massive galaxies that were cross-matched in the NoAGN and OnlyAGN runs (highlighted as outsized points in Fig. 1). Because they inhabit the same halo, their merger histories are similar, but their stellar masses and sizes differ noticeably as a result of differing feedback processes. Each galaxy’s DM distribution reflects its response to galaxy formation: The more massive the central galaxy, the more concentrated its DM halo. The effect is, however, weak. The dark gray line in each panel shows, for comparison, the circular velocity curve of the same halo in the corresponding DM-only simulation.

The resulting rotation curves show a clear transition from baryon- to dark-matter-dominated regimes, suggesting that careful calibration of subgrid models is needed to produce galaxies with realistic mass profiles. Despite these structural differences, all four galaxies nevertheless follow closely the same relation between the total acceleration and the acceleration due to baryons (lower panels). Galaxies in the NoAGN run, which are more massive and more compact than those in OnlyAGN, populate the high acceleration regime of the relation, indicating that they are baryon dominated over a larger radial extent. When included, AGN feedback periodically quenches star formation, resulting in less compact and lower mass central galaxies that are DM dominated over a large radial range.

The right-hand panels in Fig. 2 show another example. Here we select all halos from NoAGN and StrongFB whose masses lie in the range $12.3 \leq \log_{10} M_{200}/M_{\odot} \leq 12.5$ (vertical shaded band in the left panel in Fig. 1) and plot their *median* circular velocity and acceleration profiles. These galaxies have stellar masses that differ, on average,

by a factor of ≈ 4 depending on the feedback implementation but inhabit halos of comparable DM mass. As before, solid curves show the median dark matter mass profile for the same halos identified in the corresponding DM-only simulation; open symbols show $V_c^{\text{DM}}(r)$ measured directly in the EAGLE runs. The suppression of star formation by strong feedback results in considerably less massive galaxies that are dark matter dominated at most resolved radii. Nevertheless, both sets of galaxies follow the acceleration relation given by Eq. (1).

In all cases, *different feedback models produce galaxies that move along the MDAR rather than perpendicular to it*, resulting in small scatter. It is easy to see why. Consider an arbitrary galactic radius at which the total and baryonic accelerations are related by Eq. (1). Changing the enclosed baryon mass within this radius by a factor f shifts points horizontally to $g'_{\text{bar}} = f g_{\text{bar}}$ but also vertically to $g'_{\text{tot}} = g_{\text{tot}} + (f - 1)g_{\text{bar}}$. As a result, galaxies of different stellar mass or size that inhabit similar halos tend to move diagonally in the space of g_{bar} versus g_{tot} . The shaded regions in the lower panels in Fig. 2 indicate the scatter expected for enclosed baryon masses that differ from Eq. (1) (with $g_{\dagger} = 2.6 \times 10^{-10} \text{ m s}^{-2}$) by factors of 3 (light shaded region) and 2 (darker region).

Figure 3 (left) shows the total versus baryonic acceleration for *all* ($z = 0$) galaxies in *all* simulations. For each run, we show the *average* trends either as solid lines (REF, OnlyAGN, and NoAGN) or heavy symbols (WeakFB, StrongFB, and APOSTLE). The dashed line describes the numerical data remarkably well, even for models whose subgrid physics were *not* tuned to match observational constraints. The inset panel plots the residual scatter around this line. Despite the wide range of galaxy properties, it is smaller ($\sigma = 0.08$ dex; see also [22]) than that of the best

available observational data ($\sigma = 0.11$ dex), indicated by the solid line [15].

Note too that the acceleration relation persists at a high redshift, where galaxies are more likely to be actively merging. The right-hand panel in Fig. 3 shows the acceleration relation for $z = 0$ galaxy progenitors in our REF model at four higher redshifts. Regardless of z , the mean relations are very similar. The residuals are also small (inset panel) but show evidence of a slight but systematic redshift dependence.

Equation (1) describes all simulations remarkably well, provided $g_{\ddagger} \approx 2.6 \times 10^{-10} \text{ m s}^{-2}$ (dashed line). This is a factor of ≈ 2.2 larger than that obtained by Ref. [15] from observations of rotationally supported galaxies. This discrepancy reflects the fact that, regardless of subgrid parameters, EAGLE systematically *underpredicts* the stellar content of halos near the knee of the $M_{\star} - M_{\text{halo}}$ relation, where halos are most abundant. As a result, baryonic accelerations, at fixed g_{tot} , are smaller than observed. The middle panel in Fig. 3 shows the average MDAR for all simulations after rescaling all galaxy masses to match the $M_{\star} - M_{\text{halo}}$ derived from abundance matching [31]. All runs are now consistent with the observed relation to within the observational scatter (shown as a thick gray line and shaded region).

Discussion and summary.—We analyzed a suite of simulations from the EAGLE project that adopt widely varying subgrid parameters. Some simulations yield populations of galaxies that differ systematically from observed galaxy scaling relations. Nevertheless, all galaxies follow a simple relationship between their total and baryonic acceleration profiles, regardless of the feedback implementation. Different feedback prescriptions, which result in different galaxy populations, cause galaxies to move *along* the MDAR rather than perpendicular to it, yielding small scatter.

We note, however, that the total to baryonic acceleration relation depends *slightly but systematically* on the subgrid model. For example, the StrongFB and NoAGN models are, at a low acceleration, noticeably different: The former lies slightly above the best-fitting Eq. (1), and the latter slightly below. The differences, however, are small and within the observational scatter. The radial acceleration relation given by Eq. (1) is, therefore, very forgiving: Only *large* departures from any sensible galaxy-halo scaling relations lead to noticeable systematics. The “small” observed scatter in the MDAR is, in fact, quite large and is unlikely to provide useful constraints on subgrid models for galaxy formation.

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