



## LJMU Research Online

Jecmenica, M, Brkovic, B, Levi, E and Lazarevic, Z

**Interplane cross-saturation in multiphase machines**

<http://researchonline.ljmu.ac.uk/id/eprint/9940/>

### Article

**Citation** (please note it is advisable to refer to the publisher's version if you intend to cite from this work)

**Jecmenica, M, Brkovic, B, Levi, E and Lazarevic, Z (2019) Interplane cross-saturation in multiphase machines. IET Electric Power Applications. ISSN 1751-8679**

LJMU has developed **LJMU Research Online** for users to access the research output of the University more effectively. Copyright © and Moral Rights for the papers on this site are retained by the individual authors and/or other copyright owners. Users may download and/or print one copy of any article(s) in LJMU Research Online to facilitate their private study or for non-commercial research. You may not engage in further distribution of the material or use it for any profit-making activities or any commercial gain.

The version presented here may differ from the published version or from the version of the record. Please see the repository URL above for details on accessing the published version and note that access may require a subscription.

For more information please contact [researchonline@ljmu.ac.uk](mailto:researchonline@ljmu.ac.uk)

<http://researchonline.ljmu.ac.uk/>

# Interplane cross-saturation in multiphase machines

Milos Jecmenica<sup>1\*</sup>, Bogdan Brkovic<sup>1</sup>, Emil Levi<sup>2</sup>, Zoran Lazarevic<sup>1</sup>

<sup>1</sup> Faculty of Electrical Engineering, University of Belgrade, Bulevar Kralja Aleksandra 73, 11000 Belgrade, Serbia

<sup>2</sup> Department of Electronics and Electrical Engineering, Liverpool John Moores University, Byrom Street, Liverpool L3 3AF, UK

\* E-mail: jecmenica@etf.bg.ac.rs

**Abstract:** The use of electrical machines in electric vehicles and high-power drives frequently requires multiphase machines and multiphase inverters. While appropriate mathematical models under the linear magnetic conditions are readily available for multiphase machines, the same cannot be said for the models of the saturated multiphase machines. This paper examines the saturation in an asymmetrical six-phase induction machine under different supply conditions and addresses the applicability of the existing saturated three-phase machine models for representation of saturated multiphase machines. Specifically, the mutual coupling between different sequence planes in the vector space decomposed model under saturated conditions is analyzed. The paper relies on analytical considerations, finite element analysis and experimental results. It is shown that the saturation of the main flux path is influenced by the current components in the orthogonal (non-fundamental) sequence plane. This implies the need to develop new multiphase machine models which take this effect into account.

## 1 Introduction

During the last fifteen years or so a rapid pace of development has taken place in the area of multiphase (more than three phases) machines and drives. Such machines are suitable for numerous niche applications, due to the advantages offered by the existence of more than three phases (e.g. locomotive traction, electric ship propulsion, very high power industrial applications, electric and hybrid electric vehicles, more-electric aircraft concept, remote off-shore wind energy generation) [1–3].

The control strategies for multiphase drive applications require a good knowledge of the machine parameters to ensure a high quality of the dynamic and steady-state drive performance [4]. The performances of a machine controller, which depend on knowledge of the machine's magnetic properties, can be worsened by the phenomenon of magnetic saturation. Proper understanding and modeling of the saturation phenomenon plays a key role in determining the flux-weakening capability and better control performance of multiphase drives, since the precise estimation of controlled quantities (e.g. machine currents) and the control algorithms are all based on multiphase machine modeling. If such control systems can operate properly in the presence of magnetic saturation, a smaller machine may be used for the same purpose [5].

One of the standard assumptions of the general theory of electrical machines is that the main flux saturation can be neglected. This however proves to be inadequate in many operating regimes of three-phase machines and it is even not possible to study by simulation certain transients under this assumption (e.g. self-excitation of a three-phase stand-alone induction generator). It is for this reason that, over the years, a large research effort has been put into development of modified three-phase machine models that can account for the main flux saturation phenomenon in an accurate way. Nowadays, numerous improved models are available for both three-phase induction and synchronous machines that enable appropriate representation of the saturation within the circuit equations used to describe the machine. In general, three common approaches related to the main flux saturation modeling in three-phase machines can be identified: modeling in phase coordinates [6],  $d$ - $q$  model approach [7–12] and voltage-behind-reactance (VBR) approach [13–15]. In many ways, this research topic is now closed as far as the three-phase machinery is concerned.

Since multiphase machines are still not as common in industry as their three-phase counterparts, a huge effort has been made recently to improve multiphase machine parameter estimation techniques [16, 17]. While appropriate mathematical models under the linear magnetic conditions are readily available for multiphase machines [18, 19], the same cannot be said for the models of the saturated multiphase machines. A relatively few works have dealt with this topic [20–23] and there appears to be still a large scope for improvement.

By vector space decomposition (VSD) approach, the original phase-domain model of a multiphase machine can be decomposed into several equivalent circuits that represent the decoupled vector subspaces (planes): the fundamental ( $dq$ ) plane, identical to that of a three-phase machine, one or multiple orthogonal ( $xy$ ) planes and one or two zero-sequence components [2]. The advantages of the VSD model regarding the component decoupling become questionable if saturation and mutual leakage between stator windings is considered. The analysis of mutual coupling between the  $dq$  and  $xy$  planes carried out in [21, 23] assumes a synchronously rotating  $xy$  magnetomotive force (mmf) which contributes to air-gap flux and thus to the saturation of the main flux path. On the other hand,  $xy$  current components at fundamental frequency generate a subsynchronously rotating mmf which results in a flux density confined to leakage flux paths, due to the rotor cage reaction. Fundamental frequency currents in the  $xy$  plane are certain to occur in all post-fault scenarios that exploit fault tolerance [24], in all schemes that suggest power sharing control of the machine with multiple three-phase windings [25–28], as well as in the regenerative testing methods recently developed for multiphase machines [29, 30]. It is unknown if coupling between different orthogonal planes occurs under saturated conditions in such cases. Therefore, it is debatable whether the existing saturated  $dq$  machine models can be used to adequately take the magnetic saturation in multiphase machines into account when fundamental-frequency  $xy$  current components are present.

For the machine control purposes, it is common to take only the saturation of the main flux path into account. The leakage inductances are not affected by magnetic saturation, which is reasonable except in fault and overload conditions [9]. At low flux values, the inductances remain constant, but as the flux increases the machine starts to saturate and the inductances decrease. This is important when the machine is designed to be slightly saturated in the rated operating point in order to maximize the torque production [31, 32].

In this paper, the influence of fundamental frequency  $xy$  plane quantities on the saturation of the main flux path in an asymmetrical six-phase induction machine (6PHIM), with a  $30^\circ$  electrical shift between the two three-phase windings, will be investigated. It will be examined whether the saturation of the main flux path has an effect on the decomposition between the  $dq$  and  $xy$  planes. The influence of the  $xy$  plane on saturation will be investigated analytically, through Finite Element Analysis (FEA), and experimentally. According to the research presented in the following sections, it is concluded that the main flux path occurs mostly due to the torque-producing ( $dq$ ) plane, but an influence of the orthogonal ( $xy$ ) plane exists. This mutual influence between subspaces is termed “interplane cross-saturation”. According to the results obtained from the upcoming analyses, it is not possible to adequately include the saturation effect by considering only the currents in the  $dq$  plane, since the effect of the  $xy$  plane needs to be included as well.

This paper is organized as follows. The existing linear VSD model and a proposed approach for inclusion of magnetic saturation are described in the second section. An intuitive qualitative approach to the analysis of interplane cross-saturation will be presented in the third section. Results obtained using FEA will be given in the fourth section, whereas the experimental verification is given in the fifth section. The discussion of the results is given in the sixth section, and the conclusions are presented in the final section.

## 2 Theoretical background

In electrical machine theory, the following assumptions are frequently made when considering saturation phenomena [33]:

- the total flux linkages of each coil are the sum of the leakage and mutual flux components,
- the magnetic circuit saturation depends on the total air gap flux linkages,
- the leakage flux paths are not subject to saturation (except in transients and overload conditions), and
- hysteresis and eddy current effects (iron losses) are neglected.

Three main approaches to multiphase machine modeling exist: phase-variable, multiple  $dq$  (for multiphase machines with multiple three-phase windings) and VSD model. The phase-domain has the advantage of directly representing physical quantities, which simplifies the interfacing of the machine model with the power system network and allows more accurate representation of internal machine phenomena. The negative aspect of the phase-variable model is that it consists of nonlinear differential equations with time-varying coefficients, due to variable stator-to-rotor mutual inductances, which is not always easy to solve. The multiple  $dq$  model is based on transforming the electrical quantities of each three-phase winding into a rotating reference frame and then merging them into a unified model [18, 19]. This model allows the real behavior of the machine under asymmetrical conditions to be simulated, but is more complicated compared to the VSD model [34]. Despite its many advantages, it is difficult to interface this model with the external components or power electronics circuits modeled in the phase domain. Therefore, the voltage-behind-reactance approach was recently proposed as an alternative solution [21, 22]. The widely used VSD model is based on transforming the phase-domain variables of a multiphase machine into a fundamental (torque-producing) plane, one or more orthogonal (non-torque-producing) planes and one or two zero-sequence subspaces. The fundamental and non-fundamental subspaces are completely decoupled, which provides valuable benefits in terms of machine analysis and control [35, 36]. The VSD model equivalent circuit of a multiphase machine is identical to that of a three-phase machine, making the existing control techniques directly applicable to multiphase machines [34]. This approach can adequately describe the machine in both transient and steady-state operating conditions, both for sinusoidal and non-sinusoidal supply.

Decoupling between subspaces facilitates modeling and control of the machine. The decoupling assumption regarding the VSD model is questionable under saturated conditions. Only the coupling

between the  $dq$  and  $xy$  components will be studied, as the zero-sequence components can always be avoided by simply isolating the neutral points. The 6PHIM is commonly operated with separated neutral points, as this reduces the system dimensionality and thus simplifies the control algorithm [34]. The unsaturated VSD model of a 6PHIM will be presented, followed by an assumed extension to a model involving saturation.

### 2.1 Unsaturated VSD model

The voltage equations of a 6PHIM in the VSD domain are given as [37]:

$$\begin{aligned} \mathbf{u}_s &= \mathbf{R}_s \dot{\mathbf{i}}_s + \frac{d\boldsymbol{\psi}_s}{dt} - \omega_e [\psi_{qs} \quad -\psi_{ds} \quad 0 \quad 0 \quad 0 \quad 0]^T \\ \mathbf{0}_{6 \times 1} &= \mathbf{R}_r \dot{\mathbf{i}}_r + \frac{d\boldsymbol{\psi}_r}{dt} - (\omega_e - \omega) [\psi_{qr} \quad -\psi_{dr} \quad 0 \quad 0 \quad 0 \quad 0]^T \end{aligned} \quad (1)$$

where  $\omega$  (rad/s) is the rotor electrical angular speed,  $\omega_e$  (rad/s) is the arbitrary angular speed of the rotating reference frame, and:

$$\begin{aligned} \boldsymbol{\xi}_{s,r} &= [\xi_{ds,r} \quad \xi_{qs,r} \quad \xi_{xs,r} \quad \xi_{ys,r} \quad \xi_{0+s,r} \quad \xi_{0-s,r}]^T \\ \mathbf{R}_s &= R_s \cdot \mathbf{I}_{6 \times 6}, \quad \mathbf{R}_r = R_r \cdot \mathbf{I}_{6 \times 6} \end{aligned} \quad (2)$$

where  $\mathbf{I}_{6 \times 6}$  is an identity matrix of the sixth order and  $\xi$  stands for an arbitrary electrical quantity (voltage, current or flux linkage). The stator flux linkages are given in space vector form as (analogous expressions hold for rotor flux linkages):

$$\vec{\psi}_{dq_s} = (L_m + L_{ls}) \vec{i}_{dq_s} + L_m \vec{i}_{dq_r} \quad (3a)$$

$$\vec{\psi}_{xy_s} = L_{ls} \vec{i}_{xy_s} \quad (3b)$$

$$\psi_{0+s} = L_{ls} i_{0+s} \quad (3c)$$

$$\psi_{0-s} = L_{ls} i_{0-s}, \quad (3d)$$

where  $L_m$  is the magnetizing inductance and  $L_{ls}$  is the stator leakage inductance. Note that there is no mutual influence between the quantities of different subspaces. With no saturation involved, all inductances in (3) are constant. The remaining equations needed to complete the model are the torque equation:

$$T_e = p L_m (i_{dr} i_{qr} - i_{ds} i_{qs}) \quad (4)$$

and the electromechanical motion equation:

$$T_e - T_L = J \frac{d\Omega}{dt} + k_f \Omega, \quad (5)$$

where  $p$  is the pole pair number,  $T_L$  is the load torque,  $J$  is the moment of inertia,  $\Omega = \omega/p$  is the mechanical angular rotor speed, and  $k_f$  is the friction coefficient. The given equations are obtained when applying the power invariant decoupling transformation matrix [37]. Note that the given model is simplified as mutual leakage inductance is neglected in flux equations (3). According to [38], mutual leakage terms occur in  $dq$  and zero-sequence flux equations. This effect is not essential for the analysis in this paper, so it will be discarded for the sake of simplicity.

### 2.2 Hypothesis - saturation modeling

It is already known from [11, 39] that coupling between windings in spatial quadrature (cross-saturation) exists in saturated smooth air-gap machines. By analogy with this phenomenon, it is of interest to determine if the main flux saturation affects the mutual coupling between the  $dq$  and  $xy$  planes, that are decoupled under unsaturated conditions. This research is necessary in order to investigate if the cross-coupling effect exists between different VSD subspaces. If it is proven that the multiphase machine main flux saturation can be modeled solely in the fundamental ( $dq$ ) plane, all existing conclusions

186 regarding the modeling of saturated three-phase machines would  
 187 apply to multiphase machines as well. It will therefore be assumed  
 188 that saturation occurs solely under the influence of fundamental ( $dq$ )  
 189 plane components and that non-torque producing subspaces do not  
 190 contribute to saturation. In other words, it will be considered that  
 191 the decoupling between the orthogonal subspaces is still valid in  
 192 saturated conditions. According to this assumption, saturation inclusion  
 193 in the model requires addition of the following equation to the  
 194 unsaturated VSD model (1)–(5):

$$L_m = f(i_m), \quad i_m = \sqrt{(i_{ds} + i_{dr})^2 + (i_{qs} + i_{qr})^2}, \quad (6)$$

195 where  $i_m$  is the magnetizing current of the machine. Note that the  
 196 decoupling of subsystems is not affected by this modification, as  
 197 already stated. It is the goal of this paper to confirm or rebut this  
 198 assumption.

199 It should be noted that the machine model (1)–(6) is given here in a  
 200 generic form. Its subsequent formulation in terms of state-space vari-  
 201 ables would lead to the introduction of the dynamic cross-saturation  
 202 in the  $dq$  equations in accordance with the selected state-space  
 203 variable set, in the same manner as for a three-phase machine [7–11].  
 204 Importantly however, if (6) is sufficient to model the saturation effect  
 205 then all the three-phase machine  $dq$  models become directly appli-  
 206 cable to multiphase machines, as  $xy$  equations of the model (1)–(3)  
 207 remain fully decoupled from the  $dq$  equations.

### 208 3 Analytical approach

209 It is of interest to determine whether the  $xy$  currents affect the reluc-  
 210 tance of iron parts of the main flux path and, if so, under which  
 211 conditions. For this purpose, an appropriate magnetic equivalent  
 212 circuit of the machine is developed and examined. By solving the cir-  
 213 cuit equations under different conditions, the influence of  $xy$  current  
 214 components on the saturation of the main flux path can be studied.

#### 215 3.1 Magnetic equivalent circuit

216 Only the stator magnetic circuit will be modeled. A part of the cir-  
 217 cuit spanning an arbitrary slot is shown in Fig. 1. All dimensions  
 218 displayed in Fig. 1 are defined in Table 3 in the Appendix. The  
 219 entire model spans one pole pair, i.e.  $Q_{pp}$  slots. A similar concept is  
 220 proposed in [40] for calculating the core reluctance of an induction  
 221 machine. Given the qualitative nature of the analysis, the following  
 222 simplifying assumptions are made in this model:

- 223 (i) The fundamental air-gap flux (main flux) is sinusoidally  
 224 distributed and independent of the potential stator winding  
 225 currents in the  $xy$  subspace. The fundamental flux is gener-  
 226 ated by the  $dq$  voltage supply, and will therefore be referred  
 227 to as the  $dq$  flux component (note however that the  $dq$  currents  
 228 are zero);
- 229 (ii) Leakage flux caused by the  $dq$  current components will be  
 230 neglected, i.e. it will be considered that only the  $xy$  current  
 231 components contribute to the leakage flux. This assumption  
 232 goes in hand with (i), as the main flux can now be considered  
 233 proportional to the supply voltage (provided that the winding  
 234 resistance is also neglected);
- 235 (iii) It will be assumed that reluctances of stator slot bridges are  
 236 constant, i.e. the slot saturation in the tangential direction will  
 237 be neglected, as this flux path is dominated by air. Addition-  
 238 ally, the flux density over the length of each stator tooth will  
 239 be considered constant;
- 240 (iv) Uniform flux density distribution will be assumed in each part  
 241 of the magnetic circuit;
- 242 (v) A constant flux density will be assumed in each part of the sta-  
 243 tor yoke between the centerlines of two adjacent teeth (yoke  
 244 section of length  $l_{ys}$  in Fig. 1).

245 Since the fundamental flux density is predefined, only the non-  
 246 fundamental flux components generated by the currents in the  $xy$

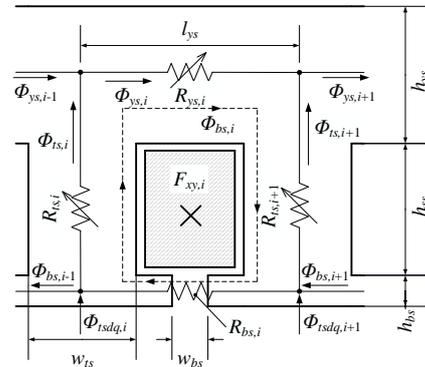


Fig. 1: Part of the developed stator magnetic circuit surrounding one slot

247 subspace, if present, are left to be determined. Therefore, an mmf  
 248 corresponding to  $xy$  current components is attributed to each slot.  
 249 The particular mmf values for each slot depend on the layout of the  
 250 particular winding. According to Fig. 1, the mmf balance equation  
 251 for an arbitrary slot is then given as:

$$F_{xy,i} = (R_{bs} + R_{ts,i} + R_{ys,i} + R_{ts,i+1}) \Phi_{bs,i}, \quad (7)$$

where  $i \in \{1, \dots, Q_{pp}\}$ , and  $\Phi_{bs,i}$  is the self flux corresponding to  
 the  $i^{\text{th}}$  slot, i.e. the flux generated solely by the slot mmf  $F_{xy,i}$ . This  
 flux component is designated by a dashed line in Fig. 1. Note that  
 $\Phi_{bs,i}$  is confined to the leakage flux path, which is in accordance  
 with the fact that the  $xy$  currents produce only leakage flux [17].  
 As stated in assumption (iii), the stator slot bridge reluctance  $R_{bs}$  is  
 considered constant and equal for each slot. Stator yoke and tooth  
 reluctances depend on the corresponding total flux densities, which  
 are defined as:

$$B_{ys,i} = \frac{\Phi_{bs,i} + \Phi_{ysdq,i}}{h_{ys} l_a}, \quad (8a)$$

$$B_{ts,i} = \frac{\Phi_{bs,i} + \Phi_{tsdq,i} - \Phi_{bs,i-1}}{w_{ts} l_a}, \quad (8b)$$

where  $l_a$  is the axial length of the machine (Table 3 in the Appendix),  
 $\Phi_{tsdq,i}$  is the main flux through one slot pitch, and  $\Phi_{ysdq,i}$  is  
 the yoke flux obtained by integrating the main flux density over  
 the perimeter of the machine. In this model, the yoke flux corre-  
 sponding to the portion of the yoke above the  $i^{\text{th}}$  slot is calculated  
 approximately as:

$$\Phi_{ysdq,i} = \sum_{n=1}^{n=i} \Phi_{tsdq,n} \quad (9)$$

The yoke, tooth, and slot bridge reluctances are given as:

$$R_{ys,i} = \frac{l_{ys}}{\mu_{ys,i} (B_{ys,i}) h_{ys} l_a} \quad (10a)$$

$$R_{ts,i} = \frac{h_{ss}}{\mu_{ts,i} (B_{ts,i}) w_{ts} l_a} \quad (10b)$$

$$R_{bs} = \frac{w_{bs}}{\mu_0 h_{bs} l_a}, \quad (10c)$$

where  $\mu_{ys,i}$  and  $\mu_{ts,i}$  are the yoke and tooth iron permeability,  
 respectively, and  $\mu_0 = 4\pi \times 10^{-7}$  (H/m) is the permeability of free  
 space. Note that the prior two are dependent on the corresponding  
 flux densities. The dependence  $\mu(B)$  is obtained from the saturation

262 characteristic of a commercial laminated steel and expressed as a  
263 piecewise linear function.

264 The unknown quantities in (7)-(10) are the fluxes  $\Phi_{bs,i}$ ,  $\Phi_{bs,i-1}$   
265 and  $\Phi_{bs,i+1}$ . Values of  $\Phi_{tsdq,i}$  and  $\Phi_{ysdq,i}$  are obtained directly  
266 from the given air-gap flux density, according to assumption (i), and  
267 therefore represent input quantities. In order to obtain a square system  
268 with a unique solution, (7) needs to be formulated for each of the  
269  $Q_{pp}$  slots under one pole pair, thereby constituting a system of  $Q_{pp}$   
270 nonlinear algebraic equations. By noting that  $\Phi_{bs,Q_{pp}+1} \equiv \Phi_{bs,1}$   
271 and  $\Phi_{bs,1-1} \equiv \Phi_{bs,Q_{pp}}$ , the number of variables reduces to  $Q_{pp}$   
272 as well and a square system of nonlinear algebraic equations is  
273 obtained. In the following section, the model of the analyzed 6PHIM  
274 will be synthesized and solved for different combinations of  $xy$  mmf  
275 and main flux density.

276 3.2 Calculation results

277 The calculations are performed using the data of the actual machine  
278 given in Table 3 in the Appendix. The main flux density distribution  
279 in the air-gap is given as:

$$B_{\delta dq}(\theta) = \hat{B}_{\delta} \cos \theta, \quad (11)$$

280 where  $\hat{B}_{\delta}$  is the magnitude of the fundamental air-gap flux density  
281 and  $\theta$  is the electrical angle, with  $\theta = 0$  corresponding to the middle  
282 of the first tooth ( $ts, 1$ ) of the developed magnetic circuit model.

283 The mmf of each slot is calculated according to the currents of the  
284 top and bottom layer and the number of conductors per layer ( $z_Q/2$ ).  
285 An mmf distribution corresponding to the  $xy$  subspace is achieved  
286 by assigning appropriate currents to each phase according to [37]:

$$\begin{aligned} i_{a1,xy} &= \hat{I}_{xy} \cdot \cos \varphi_{xy} & 317 \\ i_{b1,xy} &= \hat{I}_{xy} \cdot \cos(\varphi_{xy} - 4\pi/3) & 318 \\ i_{c1,xy} &= \hat{I}_{xy} \cdot \cos(\varphi_{xy} - 2\pi/3) & 319 \\ i_{a2,xy} &= \hat{I}_{xy} \cdot \cos(\varphi_{xy} - 5\pi/6) & 320 \\ i_{b2,xy} &= \hat{I}_{xy} \cdot \cos(\varphi_{xy} - \pi/6) & 321 \\ i_{c2,xy} &= \hat{I}_{xy} \cdot \cos(\varphi_{xy} - 3\pi/2) & 322 \end{aligned} \quad (12)$$

287 The current magnitude  $\hat{I}_{xy}$  will be held constant, whereas the  
288 phase angle  $\varphi_{xy}$  will be varied in order to change the position of  
289 the  $xy$  mmf. This angle will be referred to as the “ $xy$  phase shift”,  
290 but it should be kept in mind that it is not actually current phase  
291 angle, but rather an artificial angle which reflects the displacement  
292 of the  $xy$  mmf with respect to the  $dq$  flux density. Introduction of  
293 this quantity allows for the analysis to be performed with different  
294 angular displacements between the fundamental and  $xy$  field, which  
295 is necessary as the latter is comprised dominantly of the 5<sup>th</sup> and  
296 7<sup>th</sup> spatial harmonics. High-order space harmonics travel at lower  
297 speeds compared to the fundamental, and their mutual displacement  
298 will therefore change over time. The fundamental flux density and  
299 the 5<sup>th</sup> harmonic of the  $xy$  mmf are displayed (conveniently scaled)  
300 in Fig. 2 for several values of  $\varphi_{xy}$ . The 5<sup>th</sup> space harmonic alone is  
301 displayed to illustrate the physical meaning of the phase shift. How-  
302 ever, it should be emphasized that, since each coil side of the winding  
303 is modeled individually, all space harmonics corresponding to the  
304 given winding layout are present and their influence is accounted for  
305 by the proposed magnetic circuit model. The stator winding distribu-  
306 tion under one pole pair is displayed in Fig. 2, below the mmf  
307 waveforms.

308 The magnetic circuit model is solved for:

$$\begin{aligned} \hat{B}_{\delta} &\in \{0.4, 0.6, 0.9, 1.2\} \text{ T} \\ \varphi_{xy} &\in [0 : 30^{\circ} : 330^{\circ}] \\ \hat{I}_{xy} &= 5 \text{ A} = \text{const} \end{aligned} \quad (13)$$

309 Very low values of air-gap flux density can occur at large speeds,  
310 i.e. in the flux weakening region. The value of 1.2 T is not expected

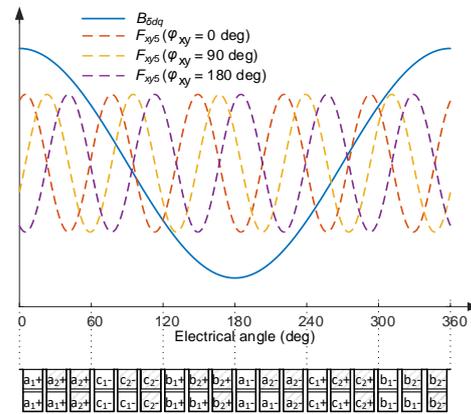


Fig. 2: Main flux density and  $xy$  mmf fifth harmonic distributions under one pole pair for different phase shifts

to ever occur and is chosen for purely theoretical reasons. After solving the model equations, yoke and tooth flux densities can be obtained according to (8), and the respective reluctances according to (10a) and (10b), respectively. Computed flux density distributions and corresponding reluctances obtained for  $\hat{B}_{\delta} = 0.9 \text{ T}$  and  $\varphi_{xy} = 90^{\circ}$ , are shown in Fig. 3. It can be noticed that the addition of the  $xy$  current component leads to an increase of flux densities and reluctances in certain parts of the magnetic circuit and its decrease in other parts. Note that the influence of the  $xy$  current component on the reluctance is the most pronounced in those parts of the magnetic circuit that are already saturated by the main ( $dq$ ) flux component.

In order to quantify the saturation of the main flux path, the magnetic voltage across the stator yoke is calculated as:

$$U_{ysdq} = \int_0^{\pi} H_{ysdq}(\theta) r_{ys} d\theta \approx \frac{1}{2} \sum_{i=1}^{Q_{pp}} R_{ys,i} |\Phi_{ysdq,i}|, \quad (14)$$

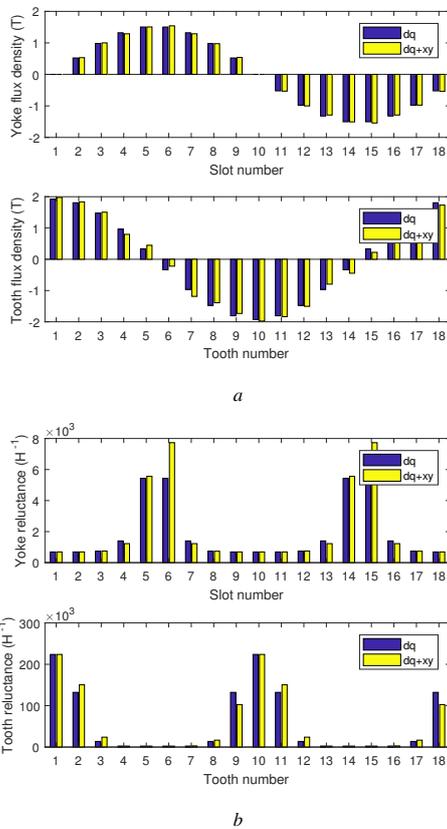
where  $H_{ysdq}$  is the  $dq$  yoke field intensity attributed to the main flux and  $r_{ys}$  is the radius of the yoke centerline. Note that only the  $dq$  flux component is used in the calculation, but the influence of the  $xy$  current (mmf) component is included in calculation of the yoke reluctance, according to (10a). The magnetic voltage values are obtained for all the combinations given by (13). In order to quantify the influence of the  $xy$  currents on the main flux saturation, the ratio of stator yoke magnetic voltage values with and without the  $xy$  current component (“relative magnetic voltage”) is calculated for each value the of main flux density and phase shift as:

$$u_{ys}^{(j,k)} = \frac{U_{ysdq}(\hat{B}_{\delta}^{(j)}, \varphi_{xy}^{(k)}, \hat{I}_{xy} = 5 \text{ A})}{U_{ysdq}(\hat{B}_{\delta}^{(j)}, \hat{I}_{xy} = 0 \text{ A})}, \quad (15)$$

where  $j$  and  $k$  denote the elements of corresponding arrays defined in (13). The relative magnetic voltage values are displayed in Fig. 4. The following conclusions can be derived from the given diagrams:

- The  $xy$  current component has a substantial effect on yoke saturation only when the main flux density is sufficiently high, in the sense that the magnetic circuit is previously saturated by the  $dq$  flux component;
- The magnetic voltage can either increase or decrease due to the  $xy$  current component, depending on the  $xy$  phase shift.

The results given in Fig. 4 clearly indicate that the  $xy$  current component has an influence on the saturation of the main flux path. Note that this influence is the most pronounced when the magnetic

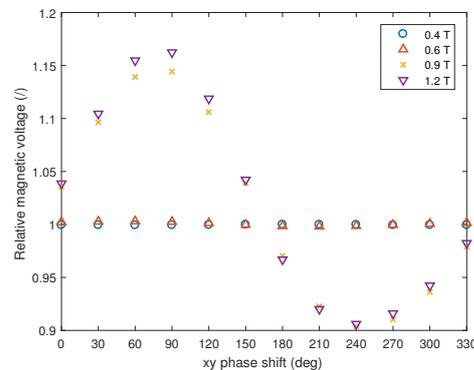


**Fig. 3:** Results obtained from the analytical model for  $\hat{B}_\delta = 0.9 \text{ T}$ ,  $\varphi_{xy} = 90^\circ$   
 a Flux densities  
 b Reluctances

346 circuit is already saturated due to the  $dq$  flux component and for  
 347 phase shifts around  $90^\circ$ . The results displayed in Fig. 3 were chosen  
 348 to illustrate such conditions. Recall that the phase shift represents  
 349 the position of the  $xy$  mmf component with respect to the main  
 350 flux density. This phase shift is time dependent, therefore, the dia-  
 351 grams displayed in Fig. 4 correspond to time waveforms of the  
 352 relative magnetic voltage. An increase of magnetic voltage means  
 353 a larger magnetizing mmf (current) requirement for the same value  
 354 of flux density, which consequently means a lower value of mag-  
 355 netizing inductance  $L_m$ . The opposite holds when the magnetic  
 356 voltage is reduced. Seeing as the  $dq$  and  $xy$  fields travel at different  
 357 angular velocities, the magnetizing inductance is expected to vary  
 358 periodically. Note that these results are contrary to the previously  
 359 adopted hypothesis (6), which indicates the presence of interplane  
 360 cross-saturation. However, in order to obtain definite conclusions  
 361 regarding the validity of the initial hypothesis, additional FEA and  
 362 experimental verification are needed and will be presented in the  
 363 following sections.

#### 364 4 Finite element analysis

365 The FEA model of the analyzed machine is formed based on the  
 366 electromagnetic design data given in Table 3. Rotor slot and yoke  
 367 dimensions could not be measured precisely, so they are assumed



**Fig. 4:** Relative stator yoke magnetic voltage values as a function of the  $xy$  phase shift for different values of the main flux density (analytical model)

368 based on common slot shapes and expected yoke flux density. The  
 369 applied FEA software takes winding currents as inputs. Therefore, as  
 370 constant air-gap flux density cannot be imposed, the concept will be  
 371 somewhat different compared to the analytical procedure. Initially,  
 372 the amplitudes of phase currents in the  $dq$  subspace that create the  
 373 air-gap flux densities given by (13) are determined by running the  
 374 model iteratively for each value. After this, the magnetics problem  
 375 is solved for the following scenarios:

- 376 1) The winding currents are set to the values determined in the  
 377 initial step ( $dq$ );
- 378 2) The winding currents are set to the values defined by (12) ( $xy$ ).  
 379 The analysis is conducted for all values of the phase angle  $\varphi_{xy}$   
 380 defined by (13). Note that  $\varphi_{xy}$  is modified according to the fun-  
 381 damental supply frequency;
- 382 3) The winding currents are set to the sum of the values corre-  
 383 sponding to scenarios 1 and 2 ( $dq + xy$ ).

384 The yoke field intensity distribution is obtained in each case.  
 385 The diagrams for the unsaturated and saturated cases are displayed  
 386 in Fig. 5. Note that, under saturated conditions ( $\hat{B}_\delta = 0.9 \text{ T}$ ), the  
 387 field intensity obtained when the  $dq$  and  $xy$  current components act  
 388 together differs significantly from the value obtained when only the  
 389  $dq$  current component is present, which indicates the presence of  
 390 interplane cross-saturation. When the magnetic circuit is unsaturated  
 391 ( $\hat{B}_\delta = 0.4 \text{ T}$ ), the influence of the  $xy$  current component is prac-  
 392 tically negligible. This confirms the conclusions of the analysis in  
 393 section 3, as the influence of the  $xy$  component on the field distribu-  
 394 tion in the stator yoke is obviously much more pronounced when the  
 395 magnetic circuit is saturated by the main flux.

396 In order to determine the influence of the  $xy$  current components  
 397 on main flux path saturation, the yoke magnetic voltages in scenarios  
 398 1 and 3 need to be compared. Only the yoke magnetic voltage caused  
 399 by the main flux is of interest. Therefore, the fundamental spatial  
 400 component of the yoke flux density is obtained for each scenario,  
 401 and the magnetic voltage is determined as:

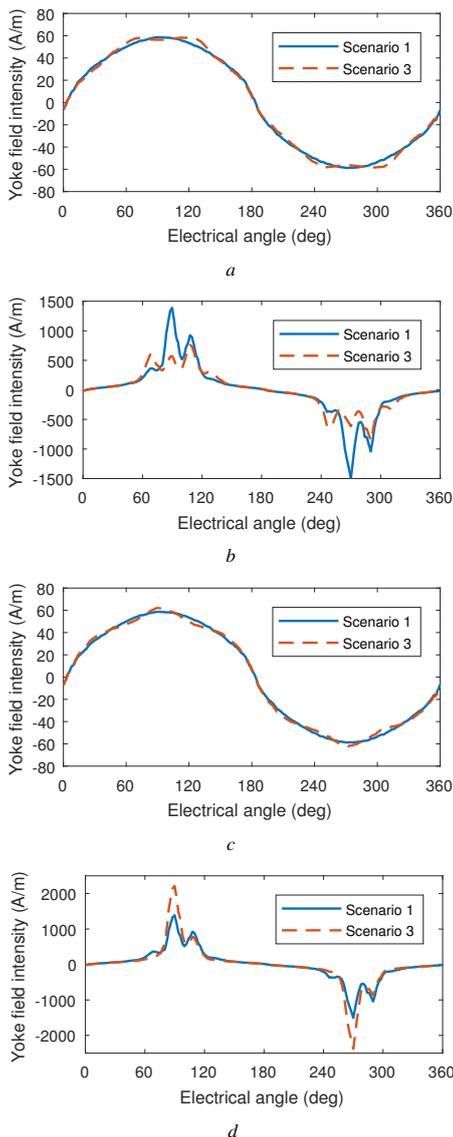
$$U_{y_s dq} = \int_0^\pi \frac{B_{y_s1}(\theta)}{\mu(\theta)} r_{y_s} d\theta, \quad (16)$$

402 where  $B_{y_s1}$  denotes the fundamental spatial component of the yoke  
 403 flux density. The magnetic material permeability is calculated as:

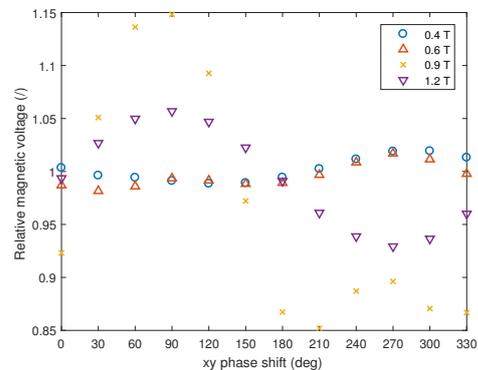
$$\mu(\theta) = \frac{B_{y_s}(\theta)}{H_{y_s}(\theta)}, \quad (17)$$

where  $B_{y_s}$  and  $H_{y_s}$  are the total flux density and field intensity at  
 the point  $(r_{y_s}, \theta)$  on the stator yoke centerline. The relative stator

406 yoke magnetic voltage values are calculated by dividing the values obtained from (16) in scenarios 1 and 3 and given in Fig. 6.  
 407 These results are very similar to those obtained from the analytical magnetic circuit model (Fig. 4). Of course, an exact match cannot be expected, as the air-gap flux density in the FEA model changes with the addition of the  $xy$  current component, and the magnetic circuit model itself is of limited accuracy. For instance, the leakage flux generated by  $dq$  currents was neglected in the magnetic circuit model. However, this flux is very pronounced in the FEA model at



**Fig. 5:** Stator yoke field intensity obtained using FEA  
 a  $\bar{B}_\delta = 0.4$  T,  $\varphi_{xy} = 270^\circ$   
 b  $\bar{B}_\delta = 0.9$  T,  $\varphi_{xy} = 270^\circ$   
 c  $\bar{B}_\delta = 0.4$  T,  $\varphi_{xy} = 90^\circ$   
 d  $\bar{B}_\delta = 0.9$  T,  $\varphi_{xy} = 90^\circ$



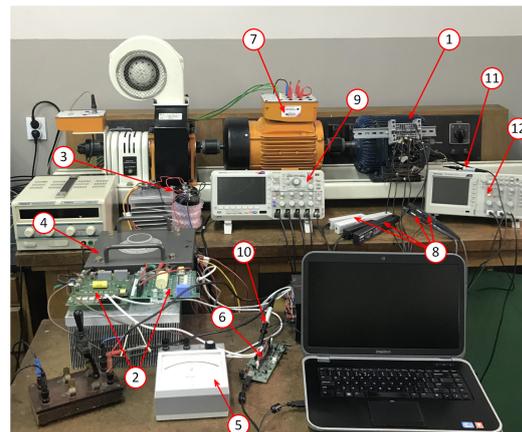
**Fig. 6:** Relative stator yoke magnetic voltage as a function of the  $xy$  phase shift for different values of the main flux density (FEA)

415 1.2 T, as the magnetic circuit is highly saturated at such a high air-gap flux density, hence the required  $dq$  current is several times larger than the rated value. Nevertheless, the FEA confirms the conclusions derived in section 3. The influence of the  $xy$  component is significant if the magnetic circuit is already saturated due to the main flux. The level of saturation, i.e. the magnetic voltage, can decrease or increase depending on the position of the  $xy$  mmf wave (phase shift  $\varphi_{xy}$ ). The results obtained from FEA confirm the presence of interplane cross-saturation indicated by the results of the analytical model.

### 5 Experimental verification

425 The influence of  $xy$  current components on the main flux saturation will be studied by observing the currents of the 6PHIM. For this purpose, measurements are performed in three operating modes characterized by the applied voltage components:

- 429 1)  $dq$  voltage supply,
- 430 2)  $xy$  voltage supply, and
- 431 3)  $dq + xy$  voltage supply.



**Fig. 7:** Experimental setup: 1–6PHIM, 2–three-phase inverter boards, 3–DC bus, 4–variatic, 5–DC bus voltage measurement, 6–microcontroller, 7–auxiliary motor, 8–current probes, 9–four-channel oscilloscope, 10–voltage probe (PWM1 signal), 11–voltage probe (air-gap voltage), 12–two-channel oscilloscope

**Table 1** Supply voltage information

DC bus voltage	Component (subspace)	Modulation index	Phase voltage fundamental
300 V	$dq$	0.84	89 Vrms
300 V	$xy$	0.16	17 Vrms
600 V	$dq$	0.92	196 Vrms
600 V	$xy$	0.08	17 Vrms

The tests are performed for different levels of saturation. The saturation level, i.e. the main flux density, is varied by changing the amplitude of the  $dq$  component of supply voltage.

The experimental setup is displayed in Fig. 7. The 6PHIM is supplied from two three-phase inverters connected to a common DC bus and controlled from a 32-bit digital signal controller with 6 PWM channels. According to [34], such a configuration is applicable when the neutral points of the two three-phase windings are separated. The DC voltage is obtained from a three-phase diode bridge rectifier supplied from a variable autotransformer. The PWM outputs are controlled in such a way that the initial phase angle corresponding to the first channel is always equal to zero, whereas the phase angles corresponding to other channels are assigned so that the required voltage components ( $dq$  or  $xy$ ) are obtained. The four-channel oscilloscope is used for the measurement of four phase currents – two in one three-phase winding, and two in the other. As the neutral point of each three-phase winding is isolated, the remaining two currents are easily calculated. The two-channel oscilloscope is used for: a) measurement of the voltage signal on the first PWM channel (PWM1 further on), which is used for time-synchronization of the current waveforms obtained in different operating modes, and b) measurement of the induced voltage of a single-turn coil placed under one pole of the 6PHIM (approximately proportional to the air-gap flux). The auxiliary motor is a four-pole induction motor used for running the 6PHIM at approximately no-load speed in operating mode 2. In operating modes 1 and 3, the auxiliary motor is disconnected from the supply and the 6PHIM is operated in no-load conditions.

The tests are conducted for two values of DC bus voltage –  $U_{dc} = 300$  V and  $U_{dc} = 600$  V. Operation with  $U_{dc} = 300$  V will be referred to as the “unsaturated case”, whereas operation with  $U_{dc} = 600$  V represents the “saturated case”. The fundamental voltage component corresponds to the rated frequency of 50 Hz (see Table 3 in the Appendix). The fundamental of  $xy$  voltage is maintained equal at both DC voltage levels by setting the appropriate values of the modulation index, so that approximately equal  $xy$  currents are obtained in both cases. The values of the modulation indices and the corresponding rms values of the supply voltage fundamental for each component and DC voltage level are given in Table 1. The fundamental component of  $dq$  voltage was set to the same value in modes 1 and 3, in order to obtain an approximately equal air-gap flux densities in these two cases. Note that the sum of the modulation indices corresponding to the  $dq$  and  $xy$  component may not exceed 1, otherwise overmodulation would occur in operating mode 3 (pure sinusoidal PWM is used, without zero-sequence injection). Obviously, the phase voltage could have been decreased by reducing the modulation index without lowering the DC bus voltage. However, this would lead to a reduction of the fundamental harmonic of current, while the ripple would remain unchanged, thereby reducing the measurement accuracy. This is a significant matter, as the oscilloscopes provide only 8-bit vertical resolution.

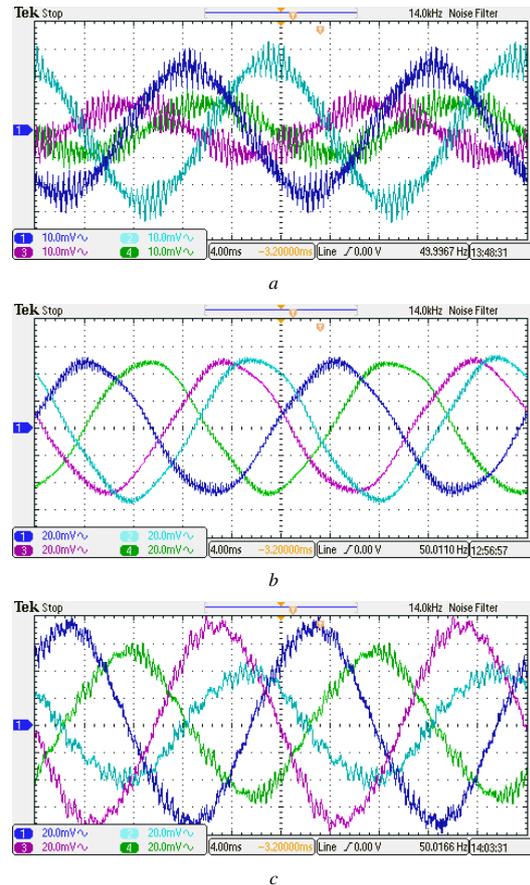
The oscilloscope screenshots of phase current waveforms corresponding to all three operating modes are shown in Figs. 8 and 9. The output/input ratio of each probe was set to 10 mV/A. The motor was operated at no-load in modes 1 and 3, and rotated at approximately no-load speed by means of the auxiliary motor in operating mode 2. It was necessary to rotate the machine under  $xy$  supply in order to achieve the same rotor cage reaction to  $xy$  current components as in mode 3. Note that the currents in mode 1 are highly unbalanced, even though the supply voltages form a balanced six-phase system. This is the consequence of the winding asymmetry, i.e. the different winding distribution of the first and second three-phase winding (see

Fig. 2). Therefore, an  $xy$  current component is present even under balanced supply. This does not represent a problem though, as the influence of the additional  $xy$  component corresponding to mode 2 can be observed regardless of the inherent  $xy$  components in mode 1. The displayed waveforms indicate that the currents corresponding to 300 Vdc are sinusoidal in all three operating modes with no notable distortion. On the other hand, the currents corresponding to 600 Vdc exhibit a certain amount of distortion, especially in operating mode 3.

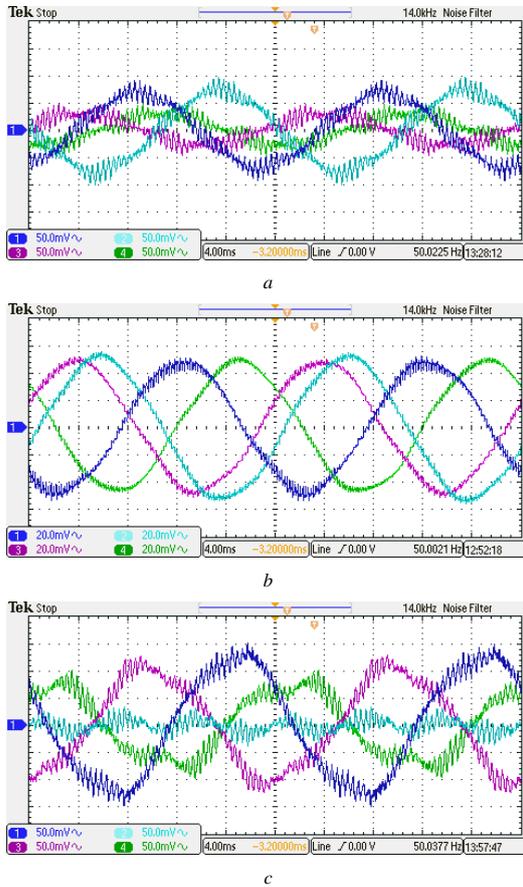
In order to better visualize the influence of the  $xy$  currents on the saturation of the magnetic circuit, the following waveforms are overlapped in Fig. 10, representing:

- the sum of currents in operating modes 1 and 2, and
- the current in operating mode 3.

All waveforms were synchronized in time with respect to the fundamental harmonic of the measured PWM1 signal. The PWM1 signal was recorded on a separate two-channel oscilloscope. In order to obtain the current and PWM1 measurements at the same time instant, a single-shot external trigger was applied to both oscilloscopes.



**Fig. 8:** Current waveforms, 300 Vdc supply  
 a Operating mode 1  
 b Operating mode 2  
 c Operating mode 3



**Fig. 9:** Current waveforms, 600 Vdc supply  
 a Operating mode 1  
 b Operating mode 2  
 c Operating mode 3

513 If the decoupling assumption were correct, the waveforms  
 514 obtained by superposition of currents in mode 1 and mode 2 should  
 515 be nearly identical to those obtained in mode 3. According to  
 516 Fig. 10a, this is true for waveforms obtained for the unsaturated case  
 517 (300 Vdc). On the other hand, the waveforms obtained in the saturated  
 518 case (600 Vdc) differ noticeably (Fig. 10b). This indicates that  
 519 the  $dq$  and  $xy$  subspaces are not decoupled when the magnetic circuit  
 520 is saturated, i.e. that interplane cross-saturation is present.

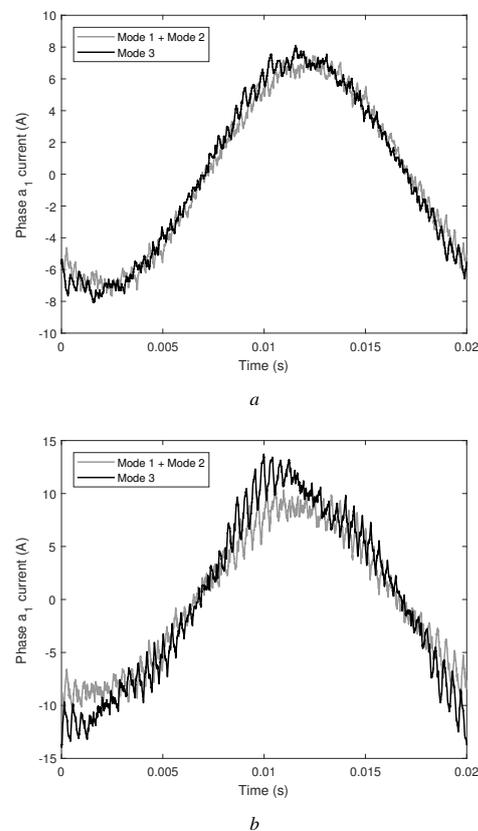
521 The second channel of the two-channel oscilloscope was used for  
 522 measuring the emf induced in a test coil placed under one pole of  
 523 the stator. This emf can be considered approximately proportional  
 524 to the air-gap flux. However, a certain amount of tooth-tip and zig-  
 525 zag leakage is inevitably present in the flux linkage of the test coil.  
 526 For purely exemplary purposes, the recorded emf waveform correspond-  
 527 ing to 600 Vdc, operating mode 1, is shown in Fig. 11. The  
 528 magnitude of the fundamental of air-gap flux density is obtained as:

$$\hat{B}_\delta = \frac{pE_1}{\sqrt{2}\pi D_{si} l_a f_1}, \quad (18)$$

529 where  $E_1$  is the rms value of the test coil emf fundamental. All  
 530 other quantities from (18) are defined in Table 3 in the Appendix.  
 531 The obtained values of fundamental air-gap flux density in operating  
 532 modes 1 and 3, in both the unsaturated and saturated case, are given

533 in Table 2. These values are very close to those selected in the analy-  
 534 tical approach and FEA, see (13). It is important to note that the flux  
 535 densities in mode 1 and 3 differ very slightly, which is most likely  
 536 the consequence of increased leakage flux due to  $xy$  current compo-  
 537 nents in mode 3. The air-gap flux density under rated operating  
 538 conditions (rated load and 180 V per phase) was determined to be  
 539 0.78 T. By observing the results of Table 2 and considering that the  
 540 magnetic circuit is moderately saturated under rated operating con-  
 541 ditions, it follows that saturation is negligible at 300 Vdc, whereas it  
 542 is highly pronounced at 600 Vdc.

543 The phase current waveforms are not sufficient to determine the  
 544 influence of the  $xy$  current components on the saturation of the main  
 545 flux path. Therefore, an additional analysis of  $dq$  current components  
 546 is necessary. The time-varying amplitude of the space vector of the



**Fig. 10:** Comparison of phase  $a_1$  current waveforms in operating  
 mode 3 and the sum of currents in operating modes 1 and 2  
 a Unsaturated case (300 Vdc)  
 b Saturated case (600 Vdc)

**Table 2** Test coil fundamental emf and air-gap flux density values

DC bus voltage (operating mode)	Emf fundamental	Air-gap flux density
300 V (1)	0.658 V	0.41 T
300 V (3)	0.672 V	0.42 T
600 V (1)	1.453 V	0.90 T
600 V (3)	1.479 V	0.92 T

547  $dq$  component is calculated as:

$$\hat{i}_{dq} = |i_{ds} + ji_{qs}| \quad (19)$$

548 Note that this value corresponds to the magnetizing current  
 549 defined by (6) if the rotor currents are equal to zero. This is  
 550 approximately true under no-load conditions. Therefore, it will be  
 551 considered that  $\hat{i}_{dq} \approx i_m$ , and the  $dq$  current vector amplitude will  
 552 be referred to as the magnetizing current further on. The magne-  
 553 tizing current waveforms corresponding to the sum of currents of  
 554 modes 1 and 2 and the currents of mode 3 are compared. The phase  
 555 current spectral components above 1 kHz were previously removed  
 556 in order to reduce the ripple and allow better visualization. The  
 557 obtained values for the unsaturated and saturated cases are shown  
 558 in Fig. 12. All waveforms indicate a presence of a backward compo-  
 559 nent (100 Hz), which can be attributed to many different factors, such  
 560 as winding asymmetry, rotor eccentricity, etc. The waveforms under  
 561 unsaturated conditions (Fig. 12a) are very similar, indicating that no  
 562 interplane cross-saturation has taken place. However, the waveforms  
 563 under saturated conditions (Fig. 12b) differ significantly. Two major  
 564 differences can be observed:

- 565 • the average value of the magnetizing current, which corresponds
- 566 to the forward component, is greater in mode 3 than in mode 1+2 by
- 567 approximately 10%, and
- 568 • the variations of the magnetizing current are greater in mode 3.

569 Both phenomena can be attributed to interplane cross-saturation.  
 570 The increase of the average of the magnetizing current indicates a  
 571 greater average reluctance of the main flux path over one period of  
 572 the fundamental frequency. Recall that the magnetic voltage, which  
 573 is proportional to the yoke reluctance, varies periodically over time,  
 574 see Figs. 4 and 6. The more pronounced oscillations of the magne-  
 575 tizing current can be attributed to the periodical variations of the  
 576 reluctance due to the  $xy$  component. This can be observed from Figs.  
 577 4 and 6.

578 The influence of interplane cross-saturation is present in the  
 579  $xy$  plane as well. This can be observed from Fig. 13, where the  
 580 waveforms of current  $i_x$  in the saturated and unsaturated cases are  
 581 displayed. A comparison is made between the current corresponding  
 582 to operating mode 3 and the sum of currents corresponding to modes  
 583 1 and 2. In the unsaturated case (Fig. 13a), the two waveforms are  
 584 nearly identical. In the saturated case (Fig. 13b) there is a significant  
 585 increase in the current magnitude. The Fourier analysis of the wave-  
 586 forms reveals that the fundamental (50 Hz) component is the most  
 587 affected, with a relative increase of nearly 40%. Higher order har-  
 588 monics are also inflicted by saturation, but are still much lower than  
 589 the fundamental.

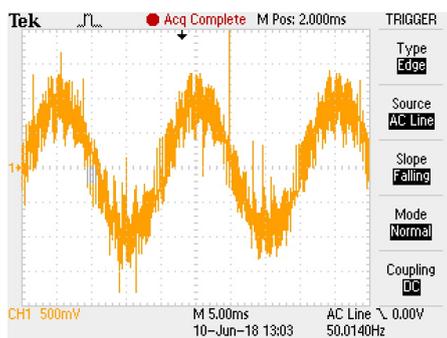


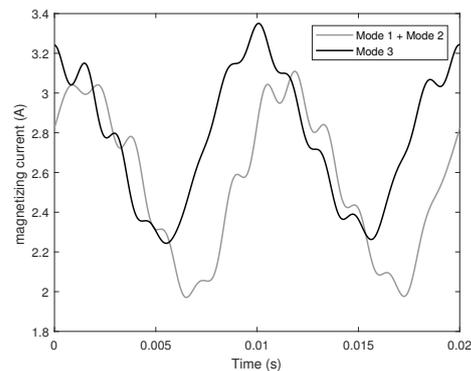
Fig. 11: Test coil induced emf waveform (operating mode 1, 600 Vdc)

## 590 6 Discussion

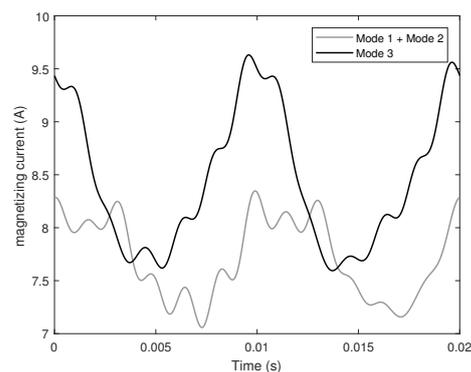
591 Results obtained from the magnetic circuit model, FE analysis and  
 592 experiment confirm the presence of mutual coupling between the  $dq$   
 593 and  $xy$  subspaces under saturated conditions. This implies a require-  
 594 ment for an improved multiphase machine model which includes this  
 595 phenomenon, termed interplane cross-saturation. A summary of the  
 596 obtained results is in order:

- 597 1) The  $dq$  and  $xy$  subspaces are decoupled under unsaturated
- 598 conditions (see Figs. 12a and 13a);
- 599 2) The addition of  $xy$  current components under saturated con-  
 600 ditions increases the magnetizing ( $dq$ ) current component (see  
 601 Fig. 12b);
- 602 3) Saturation of the magnetic circuit, i.e. the increase of magne-  
 603 tizing ( $dq$ ) current increases the  $xy$  current component (see Fig.  
 604 13b);
- 605 4) The  $xy$  current component does not affect the air-gap flux  
 606 density, regardless of the saturation level (see Table 2).

607 These observations can be used as a starting point to formulate a  
 608 model that can adequately deal with the observed saturation effects.  
 609 The intention is to retain the basic model formulation similar to  
 610 (1)-(6) and to accommodate the findings of this paper through mod-  
 611 ifications of the flux linkage equations (3). Since any such new



a

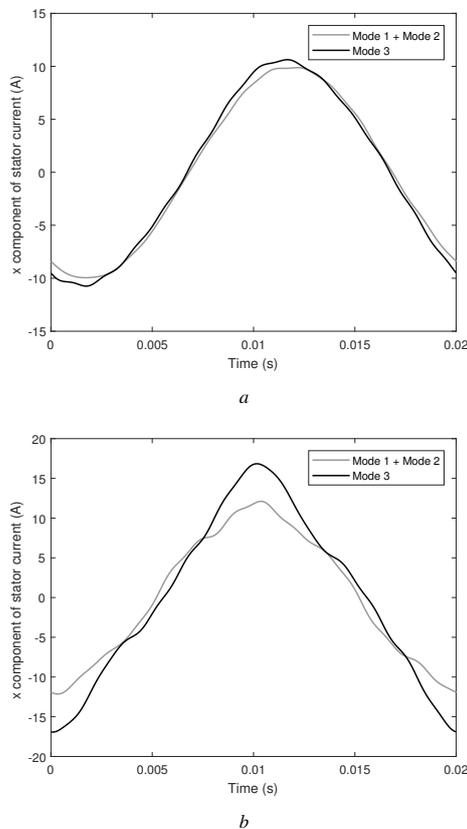


b

Fig. 12: Comparison of magnetizing current waveforms in operating mode 3 and the sum of currents in modes 1 and 2

a Unsaturated case (300 Vdc)

b Saturated case (600 Vdc)



**Fig. 13:** Comparison of  $x$  current component waveforms in operating mode 3 and the sum of currents in modes 1 and 2  
 a Unsaturated case (300 Vdc)  
 b Saturated case (600 Vdc)

model would inevitably require parameter identification and subsequent experimental verification, its exact formulation is postponed until these conditions are met.

**7 Conclusion**

Interplane cross-saturation, i.e. mutual coupling between the orthogonal subspaces in a VSD model of a saturated multiphase machine, was investigated. The fundamental frequency  $xy$  components characteristic for post-fault and power-sharing operating modes were considered. The analysis was carried out for an asymmetrical six-phase induction machine. The research was conducted through analytical considerations, finite element analysis and experimentally. Analytical and FEA results have demonstrated that the reluctances of ferromagnetic parts of the machine depend on the  $xy$  current components and the observed time instant, i.e. the displacement between the main flux density and  $xy$  mmf component. Experimental results have demonstrated that the  $dq$  current component is affected by superposition of  $xy$  supply voltage component to the preexisting  $dq$  component. However, this effect is significant only if the machine is saturated prior to the superposition of the  $xy$  component. Therefore, the initial assumption, stating that the VSD model can be expanded by simply including a variable magnetizing inductance dependent on the  $dq$  current components into the existing unsaturated model, was

shown to be incorrect. The results of all analyses indicate that interplane cross-saturation is present and needs to be taken into account for control and modeling purposes. The results obtained in this paper reveal a need to develop a new multiphase machine model or modify the existing models in order to include interplane cross-saturation. Guidelines for obtaining such a model were given in this paper. The exact formulation and verification of the model will be the focus of future research.

**8 References**

- 1 Levi, E., Bojoi, R., Profumo, F., et al.: 'Multiphase induction motor drives - a technology status review', *IET Electric Power Applications*, 2007, **1**, (4), pp. 489–516
- 2 Levi, E.: 'Multiphase electric machines for variable-speed applications', *IEEE Transactions on Industrial Electronics*, 2008, **55**, (5), pp. 1893–1909
- 3 Levi, E., Barrero, F., Duran, M.J.: 'Multiphase machines and drives-revisited', *IEEE Transactions on Industrial Electronics*, 2016, **63**, (1), pp. 429–432
- 4 Levi, E., Jones, M., Vukosavic, S., et al.: 'A novel concept of a multiphase, multimotor vector controlled drive system supplied from a single voltage source inverter', *IEEE Transactions on Power Electronics*, 2004, **19**, (2), pp. 320–335
- 5 Hofmann, H., Sanders, S.R., Sullivan, C.R.: 'Stator-flux-based vector control of induction machines in magnetic saturation', *IEEE Transactions on Industry Applications*, 1997, **33**, (4), pp. 935–942
- 6 Slemon, G.R.: 'Equivalent circuits for transformers and machines including nonlinear effects', *IEE Proceedings*, 1953, **100**, pp. 129–143
- 7 Brown, J.E., Kovacs, K.P., Vas, P.: 'A method of including the effects of main flux path saturation in the generalized equations of a.c. machines', *IEEE Transactions on Power Apparatus and Systems*, 1983, **PAS-102**, (1), pp. 96–103
- 8 Hallenius, K.E., Vas, P., Brown, J.E.: 'The analysis of a saturated self-excited asynchronous generator', *IEEE Transactions on Energy Conversion*, 1991, **6**, (2), pp. 336–345
- 9 Levi, E.: 'Applications of the current state space model in analyses of saturated induction machines', *Electric Power Systems Research*, 1994, **31**, (3), pp. 203–216
- 10 Levi, E., Krzeminski, Z.: 'Main flux-saturation modelling in d-q axis models of induction machines using mixed current-flux state-space models', *European Transactions on Electrical Power*, 1996, **6**, (3), pp. 207–215
- 11 Levi, E., Levi, V.A.: 'Impact of dynamic cross-saturation on accuracy of saturated synchronous machine models', *IEEE Transactions on Energy Conversion*, 2000, **15**, (2), pp. 224–230
- 12 Therrien, F., Wang, L., Jatskevich, J., et al.: 'Efficient explicit representation of ac machines main flux saturation in state-variable-based transient simulation packages', *IEEE Transactions on Energy Conversion*, 2013, **28**, (2), pp. 380–393
- 13 Wang, L., Jatskevich, J., Pekarek, S.D.: 'Modeling of induction machines using a voltage-behind-reactance formulation', *IEEE Transactions on Energy Conversion*, 2008, **23**, (2), pp. 382–392
- 14 Wang, L., Jatskevich, J.: 'Including magnetic saturation in voltage-behind-reactance induction machine model for emp-type solution', *IEEE Transactions on Power Systems*, 2010, **25**, (2), pp. 975–987
- 15 Therrien, F., Chapariha, M., Jatskevich, J.: 'Constant-parameter voltage-behind-reactance induction machine model including main flux saturation', *IEEE Transactions on Energy Conversion*, 2015, **30**, (1), pp. 90–102
- 16 Yepes, A.G., Riveros, J.A., Doval-Gandoy, J., et al.: 'Parameter identification of multiphase induction machines with distributed windings part 1: Sinusoidal excitation methods', *IEEE Transactions on Energy Conversion*, 2012, **27**, (4), pp. 1056–1066
- 17 Che, H.S., Abdel-Khalik, A.S., Dordevic, O., et al.: 'Parameter estimation of asymmetrical six-phase induction machines using modified standard tests', *IEEE Transactions on Industrial Electronics*, 2017, **64**, (8), pp. 6075–6085
- 18 Nelson, R.H., Krause, P.C.: 'Induction machine analysis for arbitrary displacement between multiple winding sets', *IEEE Transactions on Power Apparatus and Systems*, 1974, **PAS-93**, (3), pp. 841–848
- 19 Lipo, T.A.: 'A d-q model for six phase induction machines'. International Conf. Electrical Machines, Athens, Greece, 1980.
- 20 Singh, G.K.: 'Modeling and experimental analysis of a self-excited six-phase induction generator for stand-alone renewable energy generation', *Renewable Energy*, 2008, **33**, (7), pp. 1605–1621
- 21 Abdel-Khalik, A.S., Ahmed, S., Elserougi, A.A., et al.: 'A voltage-behind-reactance model of five-phase induction machines considering the effect of magnetic saturation', *IEEE Transactions on Energy Conversion*, 2013, **28**, (3), pp. 576–592
- 22 Amiri, N., Ebrahimi, S., Chapariha, M., et al.: 'Voltage-behind-reactance model of six-phase synchronous machines considering stator mutual leakage inductance and main flux saturation', *Electric Power Systems Research*, 2016, **138**, pp. 155–164
- 23 Pereira, L.A., Scharlau, C.C., Pereira, L.F.A., et al.: 'Influence of saturation on the airgap induction waveform of five-phase induction machines', *IEEE Transactions on Energy Conversion*, 2012, **27**, (1), pp. 29–41
- 24 Duran, M.J., Prieto, I.G., Bermudez, M., et al.: 'Optimal fault-tolerant control of six-phase induction motor drives with parallel converters', *IEEE Transactions on Industrial Electronics*, 2016, **63**, (1), pp. 629–640
- 25 Rubino, S., Bojoi, R., Cavagnino, A., et al.: 'Asymmetrical twelve-phase induction starter/generator for more electric engine in aircraft'. 2016 IEEE Energy Conversion Congress and Exposition (ECCE), 2016, pp. 1–8
- 26 Tani, A., Serra, G., Mengoni, M., et al.: 'Dynamic stator current sharing in quadruple three-phase induction motor drives'. IECON 2013 - 39th Annual Conference of the IEEE Industrial Electronics Society, 2013, pp. 5173–5178

718 27 Mengoni, M., Sala, G., Zarri, L., *et al.*: 'Control of a fault-tolerant quadruple three-  
719 phase induction machine for more electric aircrafts'. IECON 2016 - 42nd Annual  
720 Conference of the IEEE Industrial Electronics Society, 2016, pp. 5747–5753  
721 28 Zoric, I., Jones, M., Levi, E.: 'Arbitrary power sharing among three-phase winding  
722 sets of multiphase machines', *IEEE Transactions on Industrial Electronics*, 2018,  
723 65, (2), pp. 1128–1139  
724 29 Luise, F., Pieri, S., Mezzarobba, M., *et al.*: 'Regenerative testing of a concentrated-  
725 winding permanent-magnet synchronous machine for offshore wind generation -  
726 part i: Test concept and analysis', *IEEE Transactions on Industry Applications*,  
727 2012, 48, (6), pp. 1779–1790  
728 30 Zabaleta, M., Levi, E., Jones, M.: 'A novel synthetic loading method for multiple  
729 three-phase winding electric machines', *IEEE Transactions on Energy Conversion*,  
730 2018, pp. 1–9  
731 31 Slemmon, G.R.: 'Modelling of induction machines for electric drives', *IEEE Trans-  
732 actions on Industry Applications*, 1989, 25, (6), pp. 1126–1131  
733 32 Vassent, E., Meunier, G., Sabonnadiere, J.C.: 'Simulation of induction machine  
734 operation using complex magnetodynamic finite elements', *IEEE Transactions on  
735 Magnetics*, 1989, 25, (4), pp. 3064–3066  
736 33 Marti, J.R., Louie, K.W.: 'A phase-domain synchronous generator model including  
737 saturation effects', *IEEE Transactions on Power Systems*, 1997, 12, (1), pp. 222–  
738 229  
739 34 Bojoi, I.R.: 'Analysis, design and implementation of a dual three-phase vector  
740 controlled induction motor drive'. PhD thesis. Politecnico di Torino. Turin, Italy,  
741 2002  
742 35 Zhao, Y., Lipo, T.A.: 'Space vector pwm control of dual three-phase induc-  
743 tion machine using vector space decomposition', *IEEE Transactions on Industry  
744 Applications*, 1995, 31, (5), pp. 1100–1109  
745 36 Zoric, I., Jones, M., Levi, E.: 'Vector space decomposition algorithm for asymmet-  
746 rical multiphase machines'. 19th International Symposium on Power Electronics,  
747 Ee 2017, 2017, pp. 1–6  
748 37 Levi, E.: 'Multiphase ac machines', Irwin, J.D., editor. The Industrial Electronics  
749 Handbook on Power Electronics and Motor Drives. (CRC Press, 2011, pp. 1–31)  
750 38 Hadiouche, D., Razik, H., Rezzoug, A.: 'On the modeling and design of dual-stator  
751 windings to minimize circulating harmonic currents for vsi fed ac machines', *IEEE  
752 Transactions on Industry Applications*, 2004, 40, (2), pp. 506–515  
753 39 Vas, P., Brown, J.E., Hallenius, K.E.: 'Cross-saturation in smooth-air-gap electrical  
754 machines', *IEEE Transactions on Energy Conversion*, 1986, EC-1, (1), pp. 103–  
755 112  
756 40 Lipo, T.A.: 'Introduction to AC Machine Design'. (John Wiley & Sons, Inc., 2017)

757 **9 Appendix**

758 The rated data and dimensions of the analyzed 6PHIM are given in  
759 Table 3. The 6PHIM was obtained by rewinding an existing three-  
760 phase machine. Due to a limited number of stator slots and the  
761 requirement to keep the same number of poles in order to avoid  
762 excessive yoke saturation, the winding was executed with 1.5 slots  
763 per pole and phase. The given rated power corresponds to that of  
764 the original three-phase machine, which is a reasonable assumption  
765 considering that the cross-section of the conductors was retained. A  
766 thermal test would need to be conducted in order to determine the  
767 rated power of the 6PHIM.

**Table 3** Machine data

Parameter	Designation (Unit)	Value
Rated power (estimated)	$P_n$ (W)	4000
Rated frequency	$f_1$ (Hz)	50
Rated current	$I_n$ (A)	5.2
Rated voltage (per phase)	$U_{n,f}$ (V)	180
No. of poles	$2p$ ( $l$ )	4
No. of stator slots	$Q_s$ ( $l$ )	36
No. of rotor slots	$Q_r$ ( $l$ )	28
No. of turns/phase	$N_s$ ( $l$ )	264
No. of conductors/slot	$z_Q$ ( $l$ )	44
Conductor diameter	$d$ (mm)	1.0
Outer stator diameter	$D_{se}$ (mm)	184
Inner stator diameter	$D_{si}$ (mm)	116
Air gap length	$\delta$ (mm)	0.5
Stack length	$l_a$ (mm)	125
Stator slot height	$h_{ss}$ (mm)	16
Stator slot width	$w_{ss}$ (mm)	6.2
Stator slot opening height	$h_{bs}$ (mm)	1.2
Stator slot opening width	$w_{bs}$ (mm)	1.8
Stator tooth width	$w_{ts}$ (mm)	5.4
Stator yoke height	$h_{ys}$ (mm)	17