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Title Page

Inverse dynamics, joint reaction forces and loading in the musculoskeletal system: Guidelines for correct mechanical terms and recommendations for accurate reporting of results.

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1 **Abstract**

2 Inverse Dynamics is routinely used in biomechanics for the estimation of loading in the musculoskeletal
3 system but there are problems with the terms and definitions and even official recommendations
4 introduce artificial and incorrect mechanical constructs to justify arbitrary and inappropriate terms.
5 These terminology problems lead to further confusion and misinterpretations rather than to
6 standardisation of mechanically correct nomenclature and accurate interpretation of joint loading. The
7 perspective in this paper exposes some of the flawed foundational premises of these constructs and
8 makes recommendations for accurate reporting of inverse dynamics outcomes and musculoskeletal
9 loading. The inverse dynamics approach is based on free body diagrams that include the actual forces
10 as applied ('Actual Forces' approach) or the replacement of actual forces with an equivalent resultant
11 force and moment ('Resultant Moments' approach). Irrespective of the approach used to model the
12 muscle and other forces, the inverse dynamics outputs always include the joint reaction forces
13 representing the interactions with adjacent segments. The different terms suggested to distinguish the
14 calculated joint reaction forces from the two approaches such as 'net joint force', 'resultant force',
15 'intersegmental force' and 'bone-on-bone force' are inappropriate, misleading and confusing. It is
16 recommended to refer to joint reaction forces as Total or Partial when using an Actual Forces or a
17 Resultant Moments approach, respectively.

18

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19 **1. Introduction**

20 Despite remarkable progress in biomechanics, some mechanical misconceptions and inappropriate
21 or misleading terms persist, leading to confusion and misinterpretation of mechanical outputs. One of
22 the most controversial nomenclature topics relates to Inverse Dynamics and the estimation of loading
23 in the musculoskeletal system. There has been a long-standing debate and controversy on terminology
24 and interpretation of joint forces calculated through inverse dynamics in relation to musculoskeletal
25 loading. The usual suggestion in the literature including some recent standardisation and official
26 recommendation papers (Derrick et al., 2019; Vigotsky, Zelik, Lake, & Hinrichs, 2019) is to refer to
27 joint forces that are calculated without contributions from internal forces (e.g. muscle and ligament
28 forces) as net joint forces, joint intersegmental forces, or resultant forces. The recommended terms when
29 referring to joint forces that include the contributions of muscles forces in the musculoskeletal model
30 and related free body diagram (FBD) is to use terms such as joint contact forces or bone-on-bone forces
31 (Robertson, Caldwell, Hamill, Kamen, & Whittlesey, 2014; Vigotsky, et al., 2019; Winter, 2009;
32 Zatsiorsky, 2002). Although these publications clearly highlight an existing controversy and make some
33 useful recommendations, they sometimes also introduce artificial and incorrect mechanical constructs
34 to justify arbitrary and inappropriate terminology recommendations. These terminology problems lead
35 to further confusion and misinterpretations rather than to standardisation of appropriate and
36 mechanically correct terminology. For example, in a recent paper, Vigotsky et al. (2019) make some
37 excellent points about mechanical misconceptions in biomechanics and in particular joint reaction
38 forces, but they also introduce some incorrect interpretations that confuse rather than clarify the inverse
39 dynamics issues. For example, it is stated that ‘In biomechanics joint forces come in two flavors’ and
40 that one (net joint force) comes from inverse dynamics whereas the other (joint contact force that
41 includes internal force contributions) requires invasive measurements or musculoskeletal modelling.
42 These typical suggestions and recommendations present a concept of different classes or ‘flavors’ of
43 joint forces. The reality is, however, that there is only a single joint contact force output from inverse
44 dynamics, the joint reaction force (JRF), and this process always involves musculoskeletal modelling
45 irrespective of the complexity of the model and related FBD. The different terms suggested for
46 supposedly different classes or types of forces such as net joint forces, intersegmental forces, resultant

47 forces, bone-on-bone forces etc (e.g.Derrick, et al., 2019; Vigotsky, et al., 2019; Winter, 2009) are, in
48 fact, always referring to the JRF, because this is the only joint force output from an inverse dynamics
49 approach, although the forces contributing to its calculation and its magnitude and direction would vary
50 depending on the complexity and detail of the musculoskeletal model. The aim of this paper is to clarify
51 the inverse dynamics approaches in biomechanics, dispel some myths, confusions and
52 misunderstandings about JRFs and loading in the musculoskeletal system and recommend usage of
53 correct mechanical terms when describing inverse dynamics outcomes.

54 **2. Inverse Dynamics**

55 Biomechanical analysis of human motion usually involves the representation of the human body as
56 a system of interconnected rigid bodies as the mechanics of deformable bodies are too complex. Inverse
57 dynamics is the computational technique that is based on the equations of motion describing the
58 mechanics of a rigid body to calculate the forces and moments acting on the joints and other structures
59 when the kinematics of the rigid body motion and any external forces are known. We typically measure
60 the translational and rotational kinematics with motion analysis systems and measure any external
61 forces, for example the ground reaction forces, using force plates, and then utilise the equations of
62 motion in the inverse direction since the kinematics are known and we calculate the forces and moments
63 required for generating the observed motion. This requires a number of simplifications to be able to
64 represent a biological system and the complex anatomy of a human segment with a mechanical rigid
65 body model. These modelling simplifications result in a FBD for each segment which is the rigid body
66 model and the forces and moments acting on it described in a relevant reference frame linked to the
67 chosen coordinate system (Nigg and Herzog, 2007). The equations of motion for the FBD are usually
68 formulated using the Newton-Euler method (Derrick et al., 2019) and they can be used to explore the
69 dynamics of the modelled mechanical system and calculate musculoskeletal loading through inverse
70 dynamics.

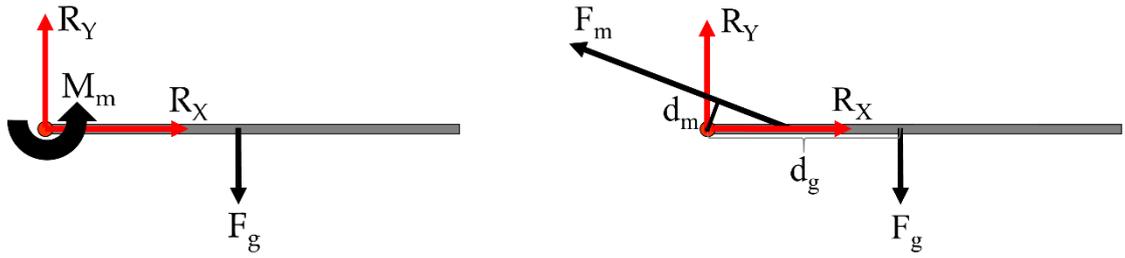
71 There are two categories of forces included in a FBD: I) Remote Forces and II) Contact Forces
72 (Andrews, 1974; Nigg and Herzog, 2007). It is important to follow the historical development of these
73 methods as the terms used originally were very simple, clear and unambiguous. The FBD is described
74 in detail, for example, by Dempster (1961) and Andrews (1974) and it is specified that the first category

75 of forces (I) are remotely applied forces on the FBD meaning without physical contact; in practice this
76 is the distributed weight force applied usually as a single gravitational force on the centre of gravity of
77 each segment. The second category of forces includes contact forces acting at the proximal and distal
78 joints due to the presence of adjacent segments (IIa) and other contact forces (IIb) acting on the segment
79 anywhere between the proximal and distal joints due to the effects of contact with the external
80 environment or other segments and external structures. These IIb forces include mainly ground contact
81 forces when in contact with the ground, muscle-tendon forces, and other external forces if there is link
82 and contact with another external body such as a dynamometer, sports implement etc. Notice that the
83 only terms used in those original papers are remote and contact forces. Although the original notations
84 for types of FBD forces used by Andrews (1974) such as I, IIa and IIb have not been adopted widely
85 and are instead used for motor unit types in muscle physiology nowadays, they will be used here simply
86 for continuity purposes and to help readers that want to refer to the original FBD papers.

87 The contact forces at the joints (IIa) are particularly important as they are applied as reactions due to
88 contact with the adjacent segments at the joint(s). The application of the other subcategory of contact
89 forces in a FBD (IIb) is more complex as we require knowledge of the contact conditions with external
90 bodies in order to apply the forces as they act in the correct sense. However, if we do not have the
91 required knowledge to apply the actual forces then an equivalent force and moment can be applied at
92 an arbitrary but appropriate point that will have the same mechanical effect, the equipollent resultant
93 force and moment (Andrews, 1974). These two approaches lead to two distinct inverse dynamics
94 formulations and one of the best and very clear descriptions of these two approaches is given by Nigg
95 and Herzog (2007) who use the terms ‘Actual Forces and Moment’ approach’ and ‘Resultant
96 Forces and Moments approach’ (simplified as ‘Actual Forces’ or ‘Resultant Moments’ here). In
97 practice, the different type IIb contact forces can be described using either approach depending on the
98 knowledge we have for their application. For this reason, we normally end up with a mixed approach
99 where the FBD usually includes some category IIb contact forces such as ground reaction forces
100 (GRFs) applied as they act (Actual Force) and other IIb contact forces, such as muscle forces,
101 replaced with equivalent resultant moments (Resultant Moment). This is normally because we do not
102 have detailed anatomical information about the geometry of their application onto the
musculoskeletal system although such information

103 exists for many situations (e.g. Tsaopoulos, Baltzopoulos, Richards, & Maganaris, 2007). We also have
104 to reduce a number of muscle forces to a single moment to avoid an indeterminate system with a single
105 moment equation and many unknown muscle forces. The important point here is that these formulations
106 (Actual Forces, Resultant Moments, or a mixed approach) are all mechanically equivalent with the same
107 system dynamics since any equipollent resultant forces and moments have exactly the same mechanical
108 effect with the actual force distributions they replace.

109 It will be easier to follow the arguments presented by considering a detailed example of a single
110 segment, two-dimensional inverse dynamics application along the lines of the model in Vigotsky, et al.
111 (2019). An isometric knee extension is assumed with a seated person holding the lower leg in a
112 horizontal position with the knee fully extended by activating the knee extensors to overcome the weight
113 of the segment. This is a static action with no movement in the knee joint and both rotational and
114 translational accelerations are zero. The two segmental axes in this position are assumed to coincide
115 with the global horizontal (X) axis (segment long axis-compressive) and vertical (Y) axis (shear segment
116 axis). There is contact at the proximal joint only (knee) with the upper leg segment. The other end of
117 the segment is free and there is no distal joint since the FBD model describes the lower leg-foot as the
118 terminal segment in the kinetic chain of the lower limb. For this reason, forces due to contact with the
119 adjacent segment are only applied at the knee (see Figure 1). We have to follow the Resultant
120 Moments approach if we do not have information about the actual application of the muscle force or
121 to reduce the number of unknown muscle forces to a single unknown parameter, the equivalent joint
122 moment they generate, and avoid an indeterminate system. In this approach we simply apply the
123 equivalent knee extension moment M_m and a total JRF resolved into components R_x and R_y along
124 the two axes as depicted in the FBD for this approach in Fig. 1 (Left Panel). In the Actual Forces
125 approach, the actual muscle force vector (F_m) is applied to the FBD instead of an equipollent moment
126 and force. This can be achieved by modelling the action of the patellar tendon based on findings from
127 the literature. In one of our previous studies, for example, we examined the orientation of the
128 patellar tendon relative to the tibia over a range of knee angles and its moment arm (d_m) *in*
129 *vivo* during maximum voluntary contractions (Tsaopoulos, et al., 2007). Based on this information
130 the resulting FBD with the Actual Forces approach is shown in the right panel of Fig. 1.



131

132 Fig. 1. Free body diagram for the isometric knee extension example using the ‘Resultant
 133 Moments’ approach (Left panel) and the ‘Actual Forces’ approach (Right panel) that also shows the
 134 moment arms of the gravitational force (d_g) and the muscle force (d_m).

135

136 In this simplified 2D approach and irrespective of the inverse dynamics approach followed, the
 137 general forms of the three equations of motion (Newton-Euler formulations of equations for rotation
 138 and translations along the two axes) are exactly the same and can be written as:

139
$$\sum_{i=1}^{M_{\max}} M_i = I\alpha$$

140
$$\sum_{i=1}^{X_{\max}} F_{x_i} = ma_x$$

141
$$\sum_{i=1}^{Y_{\max}} F_{y_i} = ma_y$$

142 where:

143 M_i the moments ($i=1 \dots M_{\max}$) acting on the FBD system, F_{x_i} the components ($i=1 \dots X_{\max}$) of all
 144 the actual forces acting along the compressive axis and F_{y_i} the components ($i=1 \dots Y_{\max}$) of any actual
 145 forces acting on or parallel to the shear axis of the FBD. The equations of motion are treated
 146 independently and sequentially so we use the same index i that takes different values in each equation.
 147 I is the moment of inertia of the segment and m the mass but since the angular (α) and linear
 148 accelerations (a_x and a_y) are zero in this isometric joint action example, the second parts of the above
 149 equations are all zero. Table 1 includes the FBDs and the general equations of motion, the expanded

150 equations of motion for rotation and translation along the two axes and the given and calculated
 151 parameters when the two different inverse dynamics approaches are implemented.

152 **Table 1.** Free body diagrams, general and expanded equations of motion, and given (input)
 153 and calculated (output) parameters when the inverse dynamics formulation is based on a FBD model
 154 using a ‘Resultant Moments’ or an ‘Actual Forces’ approach for the knee extension example. In the
 155 ‘Actual Forces’ approach the muscle force vector (F_m) can be replaced by its two components
 156 along the horizontal (F_{mx}) and vertical axis (F_{my}). Both approaches will usually have the same number
 157 of moments included in the inverse dynamics formulation so index n is common but typically $p < k$ and
 158 $q < m$

	Inverse Dynamics Approach (2D Single Segment)	
	‘Resultant Moments’	‘Actual Forces’
Free Body Diagram		
General Equations of Motion	$\sum_{i=1}^n M_i = I\alpha$ $\sum_{i=1}^p F_{x_i} = ma_x$ $\sum_{i=1}^q F_{y_i} = ma_y$	$\sum_{i=1}^n M_i = I\alpha$ $\sum_{i=1}^k F_{x_i} = ma_x$ $\sum_{i=1}^m F_{y_i} = ma_y$
Rotation	$M_m - F_g \cdot d_g = 0$	$F_m \cdot d_m - F_g \cdot d_g = 0$
Translation X Axis (Compressive)	$R_x = 0$	$R_x - F_{mx} = 0$
Translation Y Axis (Shear)	$R_y - F_g = 0$	$R_y + F_{my} - F_g = 0$
Input:	$F_g = 39.2 \text{ N}$ $d_g = 0.19 \text{ m}$	$F_g = 39.2 \text{ N}$ $d_g = 0.19 \text{ m}$ $d_m = 0.03061 \text{ m}$
Output:	$M_m = 7.45 \text{ Nm}$ $R_x = 0 \text{ N}$ $R_y = 39.2 \text{ N}$	$F_m = 243.5 \text{ N}$ $R_x = 225 \text{ N}$ $R_y = -54 \text{ N}$

159
 160 Notice that the JRF is represented in the FBD by its two components in the two different axes (R_x
 161 and R_y) and although these are drawn generically using the same vectors acting along the positive
 162 directions in both axes, the actual JRF components calculated from a Resultant Moments approach are

163 typically significantly lower and may act in different directions compared to the JRFs from the Actual
164 Forces approach. Both inverse dynamics approaches will be followed in this example to calculate the
165 loads in the musculoskeletal system, demonstrate the problems with incorrect terminology and
166 the resulting misunderstandings and confusion.

167 **2.1. Resultant Moments Approach**

168 The moments equilibrium equation for rotation in the formulation for this approach (see Table 1,
169 left panel) is:

170 $M_m - F_g \cdot d_g = I \Rightarrow \alpha \cdot M_m - F_g \cdot d_g = 0$, since $\alpha = 0$ and the moment arms of R_x and R_y are zero since, by
171 definition, they are applied on the origin of the system intersected by the axis of rotation. The muscle
172 moment M_m is the only unknown in this equation when substituting the gravitational force
173 ($F_g = 39.2$ N) and its moment arm ($d_g = 0.19$ m) so:

$$174 M_m - 39.2 \cdot 0.19 = 0 \Rightarrow M_m = 7.45 \text{ Nm}$$

175 In this formulation, the only force acting along the X axis is the compressive component of the JRF
176 (R_x) since it was not possible to model the actual muscle force and resolve it to its components along
177 the two axes:

$$178 R_x = m \cdot a_x \Rightarrow R_x = 0 \text{ N}$$

179 This inverse dynamics approach output includes the JRFs but the R_x in this case is 0 N given that this
180 is the only force that we modelled in the X direction of the FBD and we have a static condition
181 ($a_x = 0$). Solving the equation of motion for translation along the Y axis gives $R_y = 39.2$ N.

182 **2.2. Actual Forces Approach**

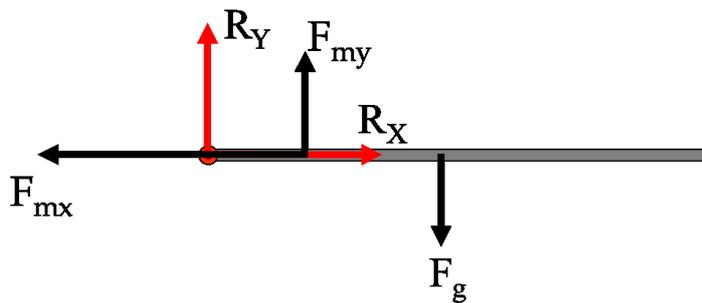
183 The moments equilibrium equation formulation for this approach under static conditions (see Table
184 1, right panel) is:

$$185 F_m \cdot d_m - F_g \cdot d_g = 0$$

186 When substituting the muscle moment arm value ($d_m = 0.03061$ m), the gravitational force ($F_g = 39.2$
187 N) and its moment arm ($d_g = 0.19$ m) to this equation, the muscle force is the only unknown so we can
188 solve for F_m :

$$189 F_m \cdot 0.03061 - 39.2 \cdot 0.19 = 0 \Rightarrow F_m = 243.5 \text{ N}$$

190 Having solved for F_m , notice that the muscle moment $M_m = F_m \cdot d_m = 7.45 \text{ Nm}$ is the same with
 191 both approaches as expected from the equations of motion for rotation in Table 1. The equations of
 192 motions for translation are applied separately in the two axes using this analytical vector
 193 approach so the calculated F_m must be resolved and replaced by its two components F_{mx} and F_{my} . It is
 194 possible to resolve F_m to its two orthogonal components and determine F_{mx} and F_{my} since the
 195 magnitude of F_m was calculated from the moments equilibrium equation and its orientation relative
 196 to the compressive axis is known (Tsaopoulos, et al., 2007). This is shown in Fig. 2 where $F_{mx} = F_m \cdot$



197
 198 **Fig. 2.** Free body diagram for the isometric knee extension example using the ‘Actual Forces’
 199 approach but with the muscle force vector replaced by the two equivalent components along the
 200 horizontal (F_{mx}) and vertical axis (F_{my}).

201
 202 We can then use the equations of motion for translation to calculate the JRF components in each
 203 axis and we obtain $R_x = 225 \text{ N}$ and $R_y = -54 \text{ N}$ as shown in Table 1 (Output row for ‘Actual Forces’).
 204 Notice that the calculated JRF in the shear direction is negative which signifies that it is actually
 205 acting in the opposite direction to the positive R_y force vector drawn in the FBD.
 206 The shear component of the JRF calculated in this approach (-54 N) is higher and in the opposite
 207 direction to the JRF shear force calculated through the Resultant Moments approach (39.2 N). Table 1
 208 contains a summary of the two different inverse dynamics modelling approaches and the resulting
 209 outputs.

210 It is important to highlight that both approaches are mechanically equivalent and the behaviour of
 211 the mechanical system would be exactly the same, that is to say, if one applied the forces and moments
 212 as described in either approach, there will be no translation in either axis and no rotation as expected in

213 this static condition. The FBD will be describing the segment in that extended static position as the
214 subject is activating the knee extensors to overcome the weight of the segment and keep the knee
215 extended with the lower leg in a static horizontal position.

216 It is also important to consider that the inverse dynamics output, irrespective of the approach
217 followed ('Actual Forces' or 'Resultant Moments'), always includes the joint reaction forces R_x and R_y .
218 It is obvious from the above example that the JRF components R_x and R_y calculated from a Resultant
219 Moments approach are significantly lower and may act in different directions compared to the JRFs
220 from the Actual Forces approach. For example, the JRFs from the Resultant Moments approach, in the
221 context of the lower leg segment and motion modelled, would indicate that there is no compressive load
222 ($R_x=0$) absorbed by the meniscus and tibia. The shear JRF ($R_y=39.2$ N) would indicate that the Posterior
223 Cruciate Ligament (PCL) is actually loaded and provides the majority of the shear force applied on the
224 tibia. However, when the actual extensor muscle force and the way it is applied is modelled (assuming
225 this knowledge exists from literature or own measurements), then the JRFs indicate that there is a
226 compressive load ($R_x=225$ N), the shear load is higher and actually applied in the posterior direction
227 ($R_y=-54$ N). This is a force that will be provided mainly by the Anterior Cruciate Ligament (ACL),
228 indicating an ACL rather than a PCL load.

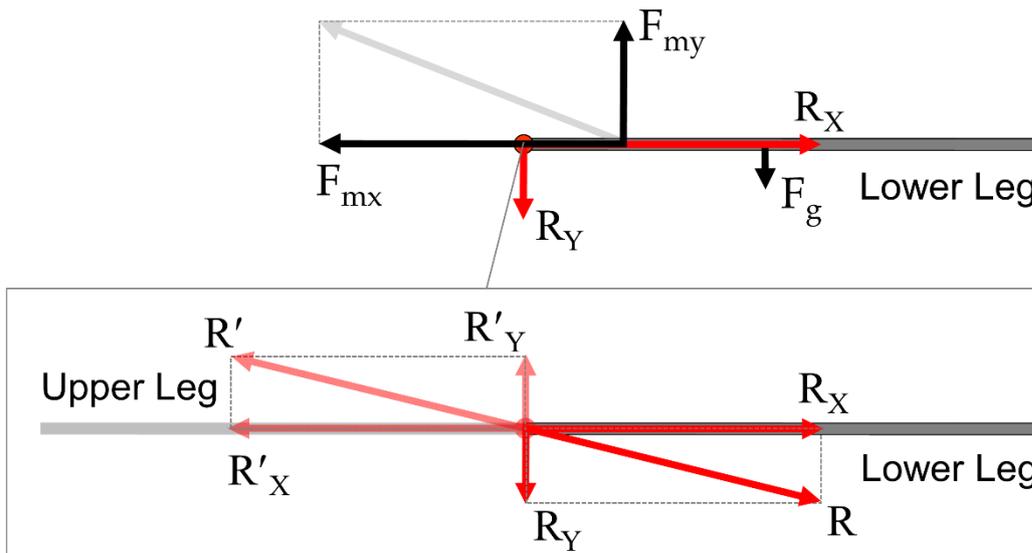
229 3. Discussion and Implications

230 The description of the inverse dynamics approaches and the worked example illustrated the problems
231 with terms and resulting misinterpretations of joint loading. The usual terminology recommendations
232 and suggested convention in the literature and recent standardisation papers is to use terms such as 'net
233 joint forces', 'resultant joint forces' or 'intersegmental joint forces' to refer to JRFs that are calculated
234 through a Resultant Moments approach and do not include the contributions of muscle forces. It is also
235 proposed that these forces should not be confused with 'bone-on-bone' or 'joint contact' forces (Derrick,
236 et al., 2019; Vigotsky, et al., 2019; Zajac, Neptune, & Kautz, 2002) that describe the loads experienced
237 across the joint surface and include muscle force contributions. Although it might be a very good
238 suggestion to have a way to differentiate JRFs when calculated through an Actual Forces or a Resultant
239 Moments approach, the fact is that they are always the calculated JRFs (category IIa contact forces in

240 the general description of forces acting in a FBD), irrespective of the inverse dynamics approach used
241 to calculate them.

242 *Why are the terms ‘net joint forces’, ‘resultant joint forces’ or ‘intersegmental joint forces’*
243 *inappropriate for differentiating JRFs?*

244 A net or a resultant force is the vector sum of a number of forces. The JRF components R_X and R_Y are
245 equal and opposite to the sum of all the forces acting on or parallel to the X and Y axes so, by definition,
246 they are net or resultant forces irrespective of the inversed dynamics approach used. For example, the
247 R_Y whether calculated through the Actual Forces ($R_Y = -54$ N) or Resultant Moments ($R_Y = 39.2$ N)
248 approach is equal and opposite to the net or resultant of all the other shear (Y axis) forces. All JRFs are
249 also, by definition, intersegmental (acting between or across segments) because they are caused as a
250 reaction to the forces (action) applied by the segment analysed to the adjacent segment, but this is
251 irrespective of the inverse dynamics approach followed. For example, the contact forces R_X and R_Y are
252 reactions (equal and opposite) to the forces applied by the lower leg to the adjacent segment (upper leg)
253 so they are equilibrant forces in structural mechanics terminology. The detailed FBD for the
254 above Actual Forces approach example is shown again in Fig. 3 but with the reaction force vectors R_X
255 and R_Y drawn to scale and pointing in the actual direction they are acting since their magnitude and
256 direction (sign) were calculated above. The joint reaction force R is thus resolved to its components
257 R_X and R_Y along the two orthogonal reference frame axes X and Y that align with the long axis of
258 the segment (compressive axis) and the shear axis, respectively, with the origin of the reference
259 frame at the joint centre.



260

261 **Fig. 3.** Free Body Diagram of the lower leg (at the top of the figure) showing the forces acting during
 262 the static knee extension example. The forces are shown as applied and resolved into components along
 263 the two axes and are drawn approximately to scale following the inverse dynamics calculations. The
 264 insert at the bottom of the figure shows the reaction forces acting at the joint between the free body
 265 diagrams of the lower and upper leg.

266

267 The insert in the bottom of Fig. 3 shows the detailed depiction of the reaction forces for the FBDs of
 268 both the lower and upper leg connected at the common joint. In the strict mechanical sense, the net or
 269 resultant of all category I and IIb forces acting on the lower leg is R' and this is applied on the upper
 270 leg segment due to contact at the joint. The equal and opposite reaction at the joint or equilibrant force
 271 R that is applied by the upper leg to the lower leg as a reaction to R' is what we include in the FBD of
 272 the lower leg since the system of interest for our mechanical analysis is the lower leg. The net force R'
 273 applied to the upper leg by the lower leg and the mechanics and motion of the adjacent segment are of
 274 no relevance for our inverse dynamics analysis of the lower leg segment. We are only concerned with
 275 the equal and opposite (equilibrant) joint reaction forces R_x and R_y (category IIa forces) that are
 276 applied as a reaction by the adjacent segment on the FBD of the segment we are currently examining.
 277 This is similar to when there is contact with the ground in which case we are interested in the ground
 reaction

278 force (GRF) as the equal and opposite reaction to the net force applied by the terminal segment to the
279 ground.

280 The terms 'net joint forces', 'resultant joint forces' or 'intersegmental joint forces' are therefore
281 inappropriate for describing JRFs calculated only through the Resultant Moments approach because the
282 JRFs calculated through an Actual Forces approach are also net or resultant and intersegmental forces.

283 *Why are the terms 'bone-on-bone forces' and 'joint contact forces' inappropriate for differentiating*
284 *JRFs?*

285 These terms are also inappropriate for differentiating JRFs because they express load on different
286 structures and not only bones and irrespective of the inverse dynamics approach followed. The
287 calculated JRFs represent forces exerted by or on different structures such as ligaments, cartilage etc
288 and not only bones. Furthermore, although a component of the JRFs will be exerted on bones, this is
289 not only the case when the Actual Forces approach is followed. For example, the shear component of
290 the JRF (R_Y) will be expressing a shear load on the tibia bone but this will be the case irrespective of
291 whether it was calculated through the Actual Forces ($R_Y=-54$ N) or Resultant Moments ($R_Y=39.2$ N)
292 approach. So it is inappropriate to restrict the term 'bone-on-bone force' only to JRFs calculated through
293 the Actual Forces approach as JRFs describe loads on bones (as well as other tissues) when using both
294 the Resultant Moments and the Actual Forces approaches. There is a typical argument used in several
295 books (Robertson, et al., 2014; Winter, 2009; Zatsiorsky, 2002) to justify the differentiation of the two
296 supposedly different forces ('joint reaction' and 'bone-on-bone') by highlighting that if there is co-
297 contraction of muscles in a static joint, for example by simultaneous activation of the main agonist and
298 antagonist muscles, then the load that will be experienced by bones will be different compared to the
299 joint load with no muscle activation, whereas the JRF will be the same in both cases. This is a fallacious
300 argument, however, because if it is known that there is co-contraction that is not modelled in the FBD
301 then of course the JRF will be miscalculated (underestimated) since there were forces acting that were
302 not included in the inverse dynamics approach. The calculated JRF is always specific to the complexity
303 of the system and constrained by the simplifications and assumptions of the musculoskeletal model used
304 in the inverse dynamics approach. If the muscle co-contraction forces acting were included in the model
305 then the correct JRF will be calculated and will be equal to the so called 'bone-on-bone' force. In both

306 cases, however, with or without co-contraction, if the muscles forces acting were included in the FBD
307 and the inverse dynamics calculations, then the JRFs will be calculated correctly and will be reflecting
308 the loads experienced by the bones and other tissues absorbing loads in the joint. Not including known
309 acting forces in the FBD is not a rational argument but a flawed foundational premise to support the
310 existence of a supposedly different category of force ('bone-on-bone force') when, in fact, what is being
311 described as a joint reaction force different from the 'bone-on bone' force is, in fact, an incorrectly
312 calculated JRF. This of course will be lower than the true JRF since there was no attempt to model and
313 include known muscle forces acting on the segment. What is termed 'bone-on-bone' force isn't a
314 separate category or type of force outside the standard inverse dynamics formulation that is different to
315 the JRF. It is in fact the correct JRF that would be calculated if all the known forces acting were included
316 in the FBD. This might be technically challenging and the restriction of only one unknown force in the
317 formulation would still apply but it is possible, for example, to predict or estimate one of the two forces,
318 the antagonist muscle force, from EMG (e.g. Kellis and Baltzopoulos, 1997; Kellis and Baltzopoulos,
319 1999). If this was applied in the above example, then the complexity of the musculoskeletal model will
320 be increased by including the EMG-estimated antagonist muscle force in the FBD model and the
321 calculated JRF will be different reducing the shear load and increasing the compressive load. Will these
322 JRFs be a different, third 'flavor' then? The answer, of course, is no because they are the same JRF
323 components R_X and R_Y but they will have different magnitude and direction as we used a more detailed
324 musculoskeletal model. There are no different 'flavors' of joint forces but a single JRF output from
325 inverse dynamics (the category IIa contact force R) although its magnitude and direction (reflected in
326 the calculated components R_X and R_Y) would depend on the complexity of the model as determined by
327 the number of other contact forces (IIb) between the proximal and distal joints included in the FBD and
328 the way they are modelled (Actual Force vs Resultant Moment).

329 It is also inappropriate to restrict the term 'joint contact force' only to JRFs calculated through the Actual
330 Forces approach when they include muscle force contributions because JRFs are joint contact forces
331 (category IIa FBD contact forces) irrespective of the inverse dynamics approach. These JRFs express
332 some of the joint contact force and joint load even when calculated without the contribution of muscle
333 forces in a Resultant Moments approach. There is also a misconception that inverse dynamics relates

334 only to the calculation of joint moments and JRFs that do not include contributions of internal forces
335 (from muscles, ligaments etc), whereas the calculation of joint contact forces that include contributions
336 of muscle and other internal forces requires musculoskeletal modelling or invasive measurement
337 (Vigotsky, et al., 2019), implying somehow that these techniques are different from inverse dynamics.
338 This is a serious misunderstanding because musculoskeletal modelling is involved in every inverse
339 dynamics approach (Nigg, 2007) as it is required in the process of constructing any FBD by making
340 simplifications and representing the segmental components and mechanics that result in a more
341 simplified (Resultant Moments approach) or more complex (Actual Forces approach) inverse dynamics
342 formulation. There is also a pejorative bias in several papers that address mechanical terminology issues
343 by targeting and criticising only sport biomechanics or sport sciences (e.g. Vigotsky, et al., 2019; Winter
344 et al., 2016) when these terminology and misinterpretation issues originate from and/or are present in
345 many other areas and applications including biomedical, clinical, rehabilitation or human movement
346 biomechanics in general.

347 *What is the appropriate terminology for JRFs in inverse dynamics?*

348 The above analysis should have clarified that the output of any inverse dynamics approach includes
349 the unknown muscle force or moment and the relevant joint contact (reaction) forces. The magnitude
350 and direction of these JRFs will obviously be different depending on the complexity of the model and
351 whether an Actual Forces or a Resultant Moments approach was followed. However, in both cases the
352 JRFs are net or resultant, intersegmental, contact forces and act on or load both bones and other
353 structures. For these reasons, the suggestion to restrict these terms to JRFs from one or the other inverse
354 dynamics approach only is arbitrary, contentious and inappropriate. An appropriate means to
355 differentiate the JRFs calculated from the two inverse dynamics approaches will be to use a term such
356 as Total JRF when referring to the JRF from the Actual Forces approach as this will include
357 contributions from all the forces acting (within the simplifications and assumptions of the FBD model)
358 and Partial JRF when using a Resultant Moments approach. The inverse dynamics approach followed
359 should also be specified (Actual Forces or Resultant Moments) when discussing musculoskeletal
360 loading rather than rely on artificial, arbitrary and sometimes incorrect or inappropriate terms. The
361 suggested term 'Total' refers to the maximum JRF calculated with the specific FBD used when all the

362 included forces (following the necessary musculoskeletal modelling simplifications) are applied on the
363 FBD as they act. If any of the forces assumed to be acting on the segment are replaced by equipollent
364 moments and forces in a Resultant Moments approach, then the calculated JRF will always be less than
365 the total JRF calculated when all the forces applied on the FBD are modelled as they act using an Actual
366 Forces approach. Therefore, the partial JRF calculated from a Resultant Moments approach must not
367 be used for estimating joint loading in inverse dynamics applications. The total JRFs from an Actual
368 Forces approach must be calculated when investigating joint loading but it must be stressed that even
369 the JRFs from an Actual Forces approach are only estimated approximations of the actual loads
370 experienced in the real joint. This is simply a consequence of the inevitable simplifications, reductions
371 and approximations of all inverse dynamics approaches that are necessary to represent the real and
372 complex musculoskeletal system with a simplified mechanical model.

373 In most biomechanics applications involving multi-segment inverse dynamics analyses, separate
374 FBDs are required for each segment and we normally start with the most distal or terminal segment
375 (usually the foot). In these multi-segment approaches, the calculated moments and forces at the proximal
376 joint (ankle) of the most distal segment (foot) have to be applied as reaction moments and forces at the
377 distal joint of the next segment (lower leg) for the inverse dynamics analysis of that segment to be
378 calculated. This process is repeated with the next segment up the kinetic chain (upper leg, pelvis etc).
379 In such multi-segment inverse dynamics analyses (Winter, 2009; Zatsiorsky, 2002), it is very convenient
380 to use the Resultant Moments approach because it eliminates the need to model the application of muscle
381 and other forces accurately at each intermediate joint, there is only one unknown parameter in the
382 moments equilibrium equation avoiding indeterminate systems and it is easier and more effective
383 computationally. This is the main reason that it is usually the inverse dynamics approach implemented
384 in motion analysis and musculoskeletal modelling software. The misinterpretation problems usually
385 start when the calculated partial JRFs from a Resultant Moments approach are used to estimate joint
386 loading with this inverse dynamics formulation. This discrepancy in the interpretation of joint loads,
387 however, is not caused because the calculated forces are not JRFs or they are not correct and it certainly
388 cannot be solved by arbitrary and inappropriate labels that are suggesting different categories or types
389 of forces but, in fact, they always refer to the JRFs. If one needs to know exact directions of the total

390 joint force in a particular direction (compressive or shear for example), then they need to make the effort
391 and obtain the information that will allow modelling of all the contributing forces as they act in both the
392 proximal and distal joints using an Actual Forces inverse dynamics approach for the last segment and
393 joint of interest. This is something that was known ever since the early applications in biomechanics
394 with Paul (1966) stating ‘To obtain the true value of the joint force components at any instant would
395 require a knowledge of the directions of pull of the muscles at that instant and the magnitude of the
396 force exerted by each’. The only possibility to use the Resultant Moments approach for joint loading
397 assessment would be to distribute the calculated joint moments at both the proximal and distal joints to
398 the contributing forces using optimisation techniques (e.g. Tsirakos, Baltzopoulos, & Bartlett, 1997),
399 and then re-calculate the total JRF. However, optimisation techniques also require knowledge or
400 estimation of various muscle parameters or variables such as moment arm/line of action, physiological
401 cross-sectional area or maximum force etc.

402 **4. Conclusions**

403 In human motion biomechanics the inverse dynamics approach is based on FBDs that include the
404 actual forces as applied or the replacement of actual forces with an equipollent resultant force and
405 moment. Irrespective of the approach used to model the muscle forces (‘Actual Forces’ or ‘Resultant
406 Moments’), the inverse dynamics outputs are always the JRFs calculated from the equations of motion
407 for translation and representing the interactions (reaction contact forces at the joints) with adjacent
408 segments. The ‘Resultant Moments’ approach is very convenient as it avoids indeterminate systems and
409 is implemented in multi-segment inverse dynamics analyses but the JRFs calculated are only the partial
410 joint contact forces since they do not contain the contributions from muscle forces that were replaced
411 by an equivalent moment. The total joint contact forces can only be calculated with the ‘Actual Forces’
412 approach and if these forces are the focus of the investigation for determining joint loading, then the
413 ‘Resultant Moments’ approach should not be used for that segment. The different terms suggested and
414 recommended to distinguish the calculated JRFs from the two different approaches are inappropriate,
415 misleading and confusing because the JRFs from either approach are always, net or resultant forces,
416 intersegmental, and represent some or all of the load on bones and other joint tissues.

417 Guidelines for accurate reporting of inverse dynamics outcomes and musculoskeletal loading using
418 mechanically correct and appropriate terms:

- 419 • Always report the approach used to model muscle force(s): ‘Actual Forces’ or ‘Resultant Moments’
- 420 • Refer to JRFs as Total or Partial depending on whether an ‘Actual Forces’ or ‘Resultant Moments’
421 approach was, respectively, used
- 422 • If accurate joint loading estimation is required then an ‘Actual Forces’ approach should be used for
423 the calculation of the total JRF, at least for the segment(s) and joint(s) of interest, by an attempt to
424 use a more detailed musculoskeletal model with the actual application of the main muscle force in
425 the FBDs of those segments
- 426 • If a ‘Resultant Moments’ approach is the only option for the inverse dynamics analysis, then this
427 should be reported and only the calculated joint moment should be used. The partial JRF calculated
428 with this inverse dynamics approach should not be used for joint loading estimation.
- 429 • The terms ‘net joint force’, ‘resultant force’, ‘intersegmental force’ and ‘bone-on-bone force’
430 should not be used to distinguish JRFs from different inverse dynamics approaches. All JRFs are
431 net or resultant, intersegmental and express some bone loading, irrespective of the inverse
432 dynamics approach used for their calculation.

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