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### Article

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# Cross-correlating *Planck* tSZ with RCSLenS weak lensing: implications for cosmology and AGN feedback

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## ABSTRACT

We present measurements of the spatial mapping between (hot) baryons and the total matter in the Universe, via the cross-correlation between the thermal Sunyaev–Zeldovich (tSZ) map from *Planck* and the weak gravitational lensing maps from the Red Cluster Sequence Lensing Survey (RCSLenS). The cross-correlations are performed on the map level where all the sources (including diffuse intergalactic gas) contribute to the signal. We consider two configuration-space correlation function estimators,  $\xi^{y-\kappa}$  and  $\xi^{y-\gamma_t}$ , and a Fourier-space estimator,  $C_\ell^{y-\kappa}$ , in our analysis. We detect a significant correlation out to  $3^\circ$  of angular separation on the sky. Based on statistical noise only, we can report  $13\sigma$  and  $17\sigma$  detections of the cross-correlation using the configuration-space  $y-\kappa$  and  $y-\gamma_t$  estimators, respectively. Including a heuristic estimate of the sampling variance yields a detection significance of  $7\sigma$  and  $8\sigma$ , respectively. A similar level of detection is obtained from the Fourier-space estimator,  $C_\ell^{y-\kappa}$ . As each estimator probes different dynamical ranges, their combination improves the significance of the detection. We compare our measurements with predictions from the cosmo-Overwhelmingly Large Simulations suite of cosmological hydrodynamical simulations, where different galactic feedback models are implemented. We find that a model with considerable active galactic nuclei (AGN) feedback that removes large quantities of hot gas from galaxy groups and *Wilkinson Microwave Anisotropy Probe* 7-yr best-fitting cosmological parameters provides the best match to the measurements. All baryonic models in the context of a *Planck* cosmology overpredict the observed signal. Similar cosmological conclusions are drawn when we employ a halo model with the observed ‘universal’ pressure profile.

**Key words:** gravitational lensing: weak – dark matter – large-scale structure of Universe.

## 1 INTRODUCTION

Weak gravitational lensing has matured into a precision tool. The fact that it is insensitive to galaxy bias has made lensing a power-

ful probe of large-scale structure. However, our lack of a complete understanding of small-scale astrophysical processes has been identified as a major source of uncertainty for the interpretation of the lensing signal. For example, baryonic physics has a significant impact on the matter power spectrum at intermediate and small scales with  $k \gtrsim 1 h \text{Mpc}^{-1}$  (van Daalen et al. 2011) and ignoring such effects can lead to significant biases in our cosmological inference (Semboloni et al. 2011; Harnois-Déraps et al. 2015). On the other

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hand, if modelled accurately, these effects can be used as a powerful way to probe the role of baryons in structure formation without affecting the ability of lensing to probe cosmological parameters and the dark matter distribution.

One can gain insights into the effects of baryons on the total mass distribution by studying the cross-correlation of weak lensing with baryonic probes. In this way, one can acquire information that is otherwise inaccessible, or very difficult to obtain, from the lensing or baryon probes individually. Cross-correlation measurements also have the advantage that they are immune to residual systematics that do not correlate with the respective signals. This enables the clean extraction of information from different probes.

Recent detections of the cross-correlation between the thermal Sunyaev–Zeldovich (tSZ) signal and gravitational lensing have already revealed interesting insights about the evolution of the density and temperature of baryons around galaxies and clusters. van Waerbeke, Hinshaw & Murray (2014) found a  $6\sigma$  detection of the cross-correlation between the galaxy lensing convergence,  $\kappa$ , from the Canada–France–Hawaii Telescope Lensing Survey (CFHTLenS) and the tSZ signal ( $y$ ) from *Planck*. Further theoretical investigations using the halo model (Ma et al. 2015) and hydrodynamical simulations (Battaglia, Hill & Murray 2015; Hojjati et al. 2015) demonstrated that  $\sim 20$  per cent of the cross-correlation signal arises from low-mass haloes  $M_{\text{halo}} \leq 10^{14} M_{\odot}$ , and that about a third of the signal originates from the diffuse gas beyond the virial radius of haloes. While the majority of the signal comes from a small fraction of baryons within haloes, about half of all baryons reside outside haloes and are too cool ( $T \sim 10^5$  K) to contribute to the measured signal significantly. We also note that Hill & Spergel (2014) presented a correlation between weak lensing of the cosmic microwave background (CMB; as opposed to background galaxies) and the tSZ with a similar significance of detection, whose signal is dominated by higher redshift ( $z > 2$ ) sources than the galaxy lensing–tSZ signal.

The galaxy lensing–tSZ cross-correlation studies described above were limited. In van Waerbeke et al. (2014), for example, statistical uncertainty dominates due to the relatively small area of the CFHTLenS survey ( $\sim 150 \text{ deg}^2$ ). The tSZ maps were constructed from the first release of the *Planck* data. And finally, the theoretical modelling of the cross-correlation signal was not as reliable for comparison with data as it is today.

In this paper, we use the Red Cluster Sequence Lensing Survey (RCSLenS) data (Hildebrandt et al. 2016) and the recently released tSZ maps by the *Planck* team (Planck Collaboration XXII 2016). RCSLenS covers an effective area of approximately  $560 \text{ deg}^2$ , which is roughly four times the area covered by CFHTLenS (although the RCSLenS data are somewhat shallower). Combined with the high-quality tSZ maps from *Planck*, we demonstrate a significant improvement in our measurement uncertainties compared to the previous measurements in van Waerbeke et al. (2014). In this paper, we also utilize an estimator of lensing mass–tSZ correlations where the tangential shear is used in place of the convergence. As discussed in Section 2.1.1, this estimator avoids introducing potential systematic errors to the measurements during the mass map making process and we also show that it leads to an improvement in the detection significance.

We compare our measurements to the predictions from the cosmo-OverWhelmingly Large Simulations (OWLS) suite of cosmological hydrodynamical simulations for a wide range of baryon feedback models. We show that models with considerable active galactic nuclei (AGN) feedback reproduce our measurements best when a *Wilkinson Microwave Anisotropy Probe* (WMAP) 7-yr cos-

mology is employed. Interestingly, we find that all of the models overpredict the observed signal when a *Planck* cosmology is adopted. In addition, we also compare our measurements to predictions from the halo model with the baryonic gas pressure modelled using the so-called ‘universal pressure profile’ (UPP). We find consistency in the cosmological conclusions drawn from the halo model approach with that deduced from comparisons to the hydrodynamical simulations.

The organization of the paper is as follows. We present the theoretical background and the data in Section 2. The measurements are presented in Section 3, and the covariance matrix reconstruction is described in Section 4. The implication of our measurements for cosmology and baryonic physics is described in Section 5 and we summarize in Section 6.

## 2 OBSERVATIONAL DATA AND THEORETICAL MODELS

### 2.1 Cross-correlation

#### 2.1.1 Formalism

We work with two lensing quantities in this paper, the gravitational lensing convergence,  $\kappa$ , and the tangential shear,  $\gamma_{\perp}$ . The convergence,  $\kappa(\boldsymbol{\theta})$ , is given by

$$\kappa(\boldsymbol{\theta}) = \int_0^{w_{\text{H}}} dw W^{\kappa}(w) \delta_{\text{m}}(\boldsymbol{\theta} f_K(w), w), \quad (1)$$

where  $\boldsymbol{\theta}$  is the position on the sky,  $w(z)$  is the comoving radial distance to redshift  $z$ ,  $w_{\text{H}}$  is the distance to the horizon and  $w^{\kappa}(w)$  is the lensing kernel (van Waerbeke et al. 2014),

$$W^{\kappa}(w) = \frac{3}{2} \Omega_{\text{m}} \left( \frac{H_0}{c} \right)^2 g(w) \frac{f_K(w)}{a}, \quad (2)$$

with  $\delta_{\text{m}}(\boldsymbol{\theta} f_K(w), w)$  representing the 3D mass density contrast,  $f_K(w)$  is the angular diameter distance at comoving distance  $w$  and the function  $g(w)$  depends on the source redshift distribution  $n(w)$  as

$$g(w) = \int_w^{w_{\text{H}}} dw' n(w') \frac{f_K(w') - w}{f_K(w')}, \quad (3)$$

where we choose the following normalization for  $n(w)$ :

$$\int_0^{\infty} dw' n(w') = 1. \quad (4)$$

The tSZ signal is due to the inverse Compton scattering of CMB photons off hot electrons along the line-of-sight (LoS) that results in a frequency-dependent variation in the CMB temperature (Sunyaev & Zeldovich 1970),

$$\frac{\Delta T}{T_0} = y S_{\text{SZ}}(x), \quad (5)$$

where  $S_{\text{SZ}}(x) = x \coth(x/2) - 4$  is the tSZ spectral dependence, given in terms of  $x = hv/k_{\text{B}}T_0$ ,  $h$  is the Planck constant,  $k_{\text{B}}$  is the Boltzmann constant and  $T_0 = 2.725$  K is the CMB temperature. The quantity of interest in the calculations here is the Comptonization parameter,  $y$ , given by the LoS integral of the electron pressure:

$$y(\boldsymbol{\theta}) = \int_0^{w_{\text{H}}} a dw \frac{k_{\text{B}} \sigma_{\text{T}}}{m_e c^2} n_e T_e, \quad (6)$$

where  $\sigma_{\text{T}}$  is the Thomson cross-section,  $k_{\text{B}}$  is the Boltzmann constant and  $n_e[\boldsymbol{\theta} f_K(w), w]$  and  $T_e[\boldsymbol{\theta} f_K(w), w]$  are the 3D electron number density and temperature, respectively.

The first estimator of the tSZ–lensing cross-correlation that we use for the analysis in this paper is the configuration-space two-point cross-correlation function,  $\xi^{y-\kappa}(\vartheta)$ :

$$\xi^{y-\kappa}(\vartheta) = \sum_{\ell} \left( \frac{2\ell + 1}{4\pi} \right) C_{\ell}^{y-\kappa} P_{\ell}(\cos(\vartheta)) b_{\ell}^y b_{\ell}^{\kappa}, \quad (7)$$

where  $P_{\ell}$  are the Legendre polynomials. Note that  $\vartheta$  represents the angular separation and should not be confused with the sky coordinate  $\theta$ . The  $y$ – $\kappa$  angular cross-power spectrum is

$$C_{\ell}^{y-\kappa} = \frac{1}{2\ell + 1} \sum_m y_{\ell m} \kappa_{\ell m}^*, \quad (8)$$

where  $y_{\ell m}$  and  $\kappa_{\ell m}$  are the spherical harmonic transforms of the  $y$  and  $\kappa$  maps, respectively (see Ma et al. 2015 for details), and  $b_{\ell}^y$  and  $b_{\ell}^{\kappa}$  are the smoothing kernels of the  $y$  and  $\kappa$  maps, respectively. Note that we ignore higher order lensing corrections to our cross-correlation estimator. It was shown in Tröster & Van Waerbeke (2014) that corrections due to the Born approximation, lens–lens coupling and higher order reduced shear estimations have a negligible contribution to our measurement signal. We also ignore relativistic corrections to the tSZ signal.

Another estimator of lensing–tSZ correlations is constructed using the tangential shear,  $\gamma_t$ , which is defined as

$$\gamma_t(\theta) = -\gamma_1 \cos(2\phi) - \gamma_2 \sin(2\phi), \quad (9)$$

where  $(\gamma_1, \gamma_2)$  are the shear components relative to Cartesian coordinates,  $\theta = [\vartheta \cos(\phi), \vartheta \sin(\phi)]$ , where  $\phi$  is the polar angle of  $\theta$  with respect to the coordinate system. In the flat sky approximation, the Fourier transform of  $\gamma_t$  can be written in terms of the Fourier transform of the convergence as (Jeong, Komatsu & Jain 2009)

$$\gamma_t(\theta) = - \int \frac{d^2\mathbf{l}}{(2\pi)^2} \kappa(\mathbf{l}) \cos[2(\phi - \varphi)] e^{i\mathbf{l}\theta \cos(\phi - \varphi)}, \quad (10)$$

where  $\varphi$  is the angle between  $\mathbf{l}$  and the Cartesian coordinate system. We use the above expression to derive the  $y$ – $\gamma_t$  cross-correlation function as

$$\begin{aligned} \xi^{y-\gamma_t}(\vartheta) &= \langle y \gamma_t \rangle(\vartheta) \\ &= \int_0^{2\pi} \frac{d\phi}{2\pi} \int \frac{d^2\mathbf{l}}{(2\pi)^2} C_{\ell}^{y\kappa} \cos[2(\phi - \varphi)] e^{i\mathbf{l}\vartheta \cos(\phi - \varphi)}. \end{aligned} \quad (11)$$

Note that the correlation function that we have introduced in equation (11) differs from what is commonly used in galaxy–galaxy lensing studies, where the average shear profile of haloes  $\langle \gamma_t \rangle$  is measured. Here, we take every point in the  $y$  map, compute the corresponding tangential shear from every galaxy at angular separation  $\vartheta$  in the shear catalogue and then take the average (instead of computing the signal around identified haloes). Working with the shear directly in this way, instead of convergence, has the advantage that we skip the mass map reconstruction process and any noise and systematic issues that might be introduced during the process. We have successfully applied similar estimators previously to compute the cross-correlation of galaxy lensing with CMB lensing in Harnois-Déraps et al. (2016). In principle, this estimator can be used for cross-correlations with any other scalar quantity.

### 2.1.2 Fourier-space versus configuration-space analysis

In addition to the configuration-space analysis described above, we also study the cross-correlation in the Fourier space. A configuration-space analysis has the advantage that there are no

complications introduced by the presence of masks, which significantly simplifies the analysis. As described in Harnois-Déraps et al. (2016), a Fourier analysis requires extra considerations to account for the impact of several factors, including the convolution of the mask power spectrum and mode mixing. On the other hand, a Fourier-space analysis can be useful in distinguishing between different physical effects at different scales (e.g. the impact of baryon physics and AGN feedback). We choose a forward modelling approach as described in Harnois-Déraps et al. (2016) and discussed further in Section 3.

## 2.2 Observational data

### 2.2.1 RCSLenS lensing maps

The RCSLenS (Hildebrandt et al. 2016) is part of the second Red-sequence Cluster Survey (RCS2; Gilbank et al. 2011).<sup>1</sup> Data were acquired from the MegaCAM camera from 14 separate fields and cover a total area of 785 deg<sup>2</sup> on the sky. The pipeline used to process RCSLenS data includes a reduction algorithm (Erben et al. 2013), followed by photometric redshift estimation (Benítez 2000; Hildebrandt et al. 2012) and a shape measurement algorithm (Miller et al. 2013). For a complete description see Heymans et al. (2012) and Hildebrandt et al. (2016).

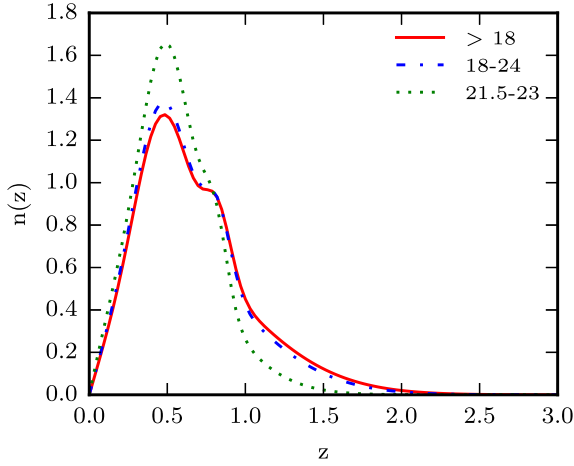
For some of the RCSLenS fields the photometric information is incomplete, so we use external data to estimate the galaxy source redshift distribution,  $n(z)$ . The CFHTLenS–VIMOS Public Extragalactic Redshift Survey (VIPERS) photometric sample is used that contains near-ultraviolet (UV) and near-infrared (IR) data combined with the CFHTLenS photometric sample and is calibrated against  $\sim 60\,000$  spectroscopic redshifts (Coupon et al. 2015). The source redshift distribution,  $n(z)$ , is then obtained by stacking the posterior distribution function of the CFHTLenS–VIPERS galaxies with predefined magnitude cuts and applying the following fitting function (following the procedure outlined in section 3.1.2 of Harnois-Déraps et al. 2016):

$$\begin{aligned} n_{\text{RCSLenS}}(z) &= a z \exp \left[ \frac{-(z-b)^2}{c^2} \right] + d z \exp \left[ \frac{-(z-e)^2}{f^2} \right] \\ &\quad + g z \exp \left[ \frac{-(z-h)^2}{i^2} \right]. \end{aligned} \quad (12)$$

As described in the Appendix A, we experimented with several different magnitude cuts to find the range where the signal-to-noise (SNR) for our measurements is maximized. We find that selecting galaxies with  $\text{mag}_r > 18$  yields the highest SNR with the best-fitting values of  $(a, b, c, d, e, f, g, h, i) = (2.94, -0.44, 1.03, 1.58, 0.40, 0.25, 0.38, 0.81, 0.12)$ . This cut leaves us with approximately 10 million galaxies from the 14 RCSLenS fields, yielding an effective galaxy number density of  $\bar{n} = 5.8$  galaxies arcmin<sup>−2</sup> and an ellipticity dispersion of  $\sigma_{\epsilon} = 0.277$  (see Heymans et al. 2012 for details).

Fig. 1 shows the source redshift distributions  $n(z)$  for the three different magnitude cuts we have examined. Note that the lensing signal is most sensitive in the redshift range approximately half way between the sources and the observer. RCSLenS is shallower than the CFHTLenS (see the analysis in van Waerbeke et al. 2013) but, as we demonstrate later, the larger area coverage of RCSLenS (more than) compensates for the lower number density of the source galaxies, in terms of the measurement of the cross-correlation with the tSZ signal.

<sup>1</sup> The RCSLenS data are public and can be found at [www.rcslens.org](http://www.rcslens.org)



**Figure 1.** Redshift distribution,  $n(z)$ , of the RCSLenS sources for different  $r$ -magnitude cuts. We work with the  $\text{mag}_r > 18$  cut (which includes all the objects in the survey).

For our analysis we use the shear data and the reconstructed projected mass maps (convergence maps) from RCSLenS. For the tSZ–tangential shear cross-correlation ( $y$ – $\gamma_t$ ), we work at the catalogue level where each pixel in the  $y$  map is correlated with the average tangential shear from the corresponding shear data in an annular bin around that point, as described in Section 3.1. To construct the convergence maps, we follow the method described in van Waerbeke et al. (2013). In Appendix A we study the impact of map smoothing on the SNR we determine for the  $y$ – $\kappa$  cross-correlation analysis. We demonstrate that the best SNR is obtained when the maps are smoothed with a kernel that roughly matches the beam scale of the corresponding  $y$  maps from *Planck* survey [full width at half-maximum (FWHM) = 10 arcmin].

The noise properties of the constructed maps are studied in detail in Appendix B.

### 2.2.2 *Planck tSZ y maps*

For the cross-correlation with the tSZ signal, we use the full sky maps provided in the *Planck* 2015 public data release (Planck Collaboration XXII 2016). We use the *milca* map that has been constructed from multiple frequency channels of the survey. Since we are using the public data from the *Planck* collaboration, there is no significant processing involved. Our map preparation procedure is limited to masking the map and cutting the patches matching the RCSLenS footprint.

Note that in performing the cross-correlations we are limited by the footprint area of the lensing surveys. In the case of RCSLenS, we have 14 separate compact patches with different sizes. In contrast, the tSZ  $y$  maps are full-sky (except for masked regions). We therefore have the flexibility to cut out larger regions around the RCSLenS fields, in order to provide a larger cross-correlation area that helps suppress the statistical noise, leading to an improvement in the SNR. We cut out  $y$  maps so that there is complete overlap with RCSLenS up to the largest angular separation in our cross-correlation measurements.

Templates have also been released by the *Planck* collaboration to remove various contaminating sources. We use their templates to mask galactic emission and point sources, which amounts to removing  $\sim 40$  per cent of the sky. We have compared our cross-correlation measurements with and without the templates and checked that our

signal is robust. We have also separately checked that the masking of point sources has a negligible impact on our cross-correlation signal (see Appendix A). These sources of contamination do not bias our cross-correlation signal and contribute only to the noise level.

In addition to using the tSZ map from the *Planck* collaboration, we have also tested our cross-correlation results with the maps made independently following the procedure described in van Waerbeke et al. (2014), where several full-sky  $y$  maps were constructed from the second release of *Planck* CMB band maps. To construct the maps, a linear combination of the four High Frequency Instrument (HFI) band maps (100, 143, 217 and 353 GHz) was used and smoothed with a Gaussian beam profile with  $\theta_{\text{SZ, FWHM}} = 10$  arcmin. To combine the band maps, band coefficients were chosen such that the primary CMB signal is removed, and the dust emission with a spectral index  $\beta_d$  is nulled. A range of models with different  $\beta_d$  values were employed to construct a set of  $y$  maps that were used as diagnostics of residual contamination. The resulting cross-correlation measurements vary by roughly 10 per cent between the different  $y$  maps, but are consistent within the errors with the measurements from the public *Planck* map.

## 2.3 Theoretical models

We compare our measurements with theoretical predictions based on the halo model and from full cosmological hydrodynamical simulations. Below we describe the important aspects of these models.

### 2.3.1 Halo model

We use the halo model description for the tSZ–lensing cross-correlation developed in Ma et al. (2015). In the framework of the halo model, the  $y$ – $\kappa$  cross-correlation power spectrum is

$$C_\ell^{y-\kappa} = C_\ell^{y-\kappa, 1h} + C_\ell^{y-\kappa, 2h}, \quad (13)$$

where the 1-halo and 2-halo terms are defined as

$$\begin{aligned} C_\ell^{y-\kappa, 1h} &= \int_0^{z_{\text{max}}} dz \frac{dV}{dz d\Omega} \int_{M_{\text{min}}}^{M_{\text{max}}} dM \frac{dn}{dM} y_\ell(M, z) \kappa_\ell(M, z), \\ C_\ell^{y-\kappa, 2h} &= \int_0^{z_{\text{max}}} dz \frac{dV}{dz d\Omega} P_m^{\text{lin}}(k = \ell/\chi, z) \\ &\quad \times \left[ \int_{M_{\text{min}}}^{M_{\text{max}}} dM \frac{dn}{dM} b(M, z) \kappa_\ell(M, z) \right] \\ &\quad \times \left[ \int_{M_{\text{min}}}^{M_{\text{max}}} dM \frac{dn}{dM} b(M, z) y_\ell(M, z) \right]. \end{aligned} \quad (14)$$

In the above equations  $P_m^{\text{lin}}(k, z)$  is the 3D linear matter power spectrum at redshift  $z$ ,  $\kappa_\ell(M, z)$  is the Fourier transform of the convergence profile of a single halo of mass  $M$  at redshift  $z$  with the Navarro–Frenk–White (NFW) profile,

$$\kappa_\ell = \frac{W^\kappa(z)}{\chi^2(z)} \frac{1}{\bar{\rho}_m} \int_0^{r_{\text{vir}}} dr (4\pi r^2) \frac{\sin(\ell r/\chi)}{\ell r/\chi} \rho(r; M, z), \quad (15)$$

and  $y_\ell(M, z)$  is the Fourier transform of the projected gas pressure profile of a single halo,

$$y_\ell = \frac{4\pi r_s}{\ell_s^2} \frac{\sigma_T}{m_e c^2} \int_0^\infty dx x^2 \frac{\sin(\ell x/\ell_s)}{\ell x/\ell_s} P_e(x; M, z). \quad (16)$$

Here  $x \equiv a(z)r/r_s$  and  $\ell_s = a\chi/r_s$ , where  $r_s$  is the scale radius of the 3D pressure profile, and  $P_e$  is the 3D electron pressure. The ratio  $r_{\text{vir}}/r_s$  is the concentration parameter (see e.g. Ma et al. 2015 for details).

**Table 1.** Subgrid physics of the baryon feedback models in the cosmo-OWLS runs. Each model has been run adopting both the *WMAP* 7-yr and *Planck* cosmologies.

| Simulation | UV/X-ray background | Cooling | Star formation | SN feedback | AGN feedback | $\Delta T_{\text{heat}}$ |
|------------|---------------------|---------|----------------|-------------|--------------|--------------------------|
| NOCOOL     | Yes                 | No      | No             | No          | No           | ...                      |
| REF        | Yes                 | Yes     | Yes            | Yes         | No           | ...                      |
| AGN 8.0    | Yes                 | Yes     | Yes            | Yes         | Yes          | $10^{8.0}$ K             |
| AGN 8.5    | Yes                 | Yes     | Yes            | Yes         | Yes          | $10^{8.5}$ K             |
| AGN 8.7    | Yes                 | Yes     | Yes            | Yes         | Yes          | $10^{8.7}$ K             |

For the electron pressure of the gas in haloes, we adopt the so-called ‘universal pressure profile’ (UPP; Arnaud et al. 2010):

$$P(x \equiv r/R_{500}) = 1.65 \times 10^{-3} E(z)^{\frac{8}{3}} \left( \frac{M_{500}}{3 \times 10^{14} h_{70}^{-1} M_{\odot}} \right)^{\frac{2}{3} + 0.12} \times \mathbb{P}(x) h_{70}^2 (\text{keV cm}^{-3}), \quad (17)$$

where  $\mathbb{P}(x)$  is the generalized NFW model (Nagai, Kravtsov & Vikhlinin 2007):

$$\mathbb{P}(x) = \frac{P_0}{(c_{500}x)^{\gamma} [1 + (c_{500}x)^{\alpha}]^{(\beta-\gamma)/\alpha}}. \quad (18)$$

We use the best-fitting parameter values from Planck Collaboration V (2013):  $\{P_0, c_{500}, \alpha, \beta, \gamma\} = \{6.41, 1.81, 1.33, 4.13, 0.31\}$ . To compute the configuration-space correlation functions, we use equations (7) and (11) for  $\xi^{y-\kappa}$  and  $\xi^{y-\nu}$ , respectively. We present the halo model predictions for two sets of cosmological parameters: the maximum likelihood *Planck* 2013 cosmology (Planck Collaboration XVI 2014) and the maximum likelihood *WMAP* 7-yr cosmology (Komatsu et al. 2011) with  $\{\Omega_m, \Omega_b, \Omega_{\Lambda}, \sigma_8, n_s, h\} = \{0.3175, 0.0490, 0.6825, 0.834, 0.9624, 0.6711\}$  and  $\{0.272, 0.0455, 0.728, 0.81, 0.967, 0.704\}$ , respectively.

There are several factors that have an impact on these predictions: the choice of the gas pressure profile, the adopted cosmological parameters and the  $n(z)$  distribution of sources in the lensing survey. In addition, the hydrostatic mass bias parameter,  $b$  (defined as  $M_{\text{obs},500} = (1 - b)M_{\text{true},500}$ ), alters the relation between the adopted pressure profile and the true halo mass. Typically, it has been suggested that  $1 - b \approx 0.8$ . Note that the impact of the hydrostatic mass bias in real groups and clusters will be absorbed into our amplitude fitting parameter  $A_{\text{tSZ}}$  (defined in equation 24).

## 2.4 The cosmo-OWLS hydrodynamical simulations

We also compare our measurements to predictions from the cosmo-OWLS suite of hydrodynamical simulations. In Hojjati et al. (2015) we compared these simulations to measurements using CFHTLenS data and we also demonstrated that high-resolution tSZ–lensing cross-correlations have the potential to simultaneously constrain cosmological parameters and baryon physics. Here we build on our previous work and employ the cosmo-OWLS simulations in the modelling of RCSLenS data.

The cosmo-OWLS suite is an extension of the Overwhelmingly Large Simulations (OWLS) project (Schaye et al. 2010). The suite consists of box-periodic hydrodynamical simulations with volumes of  $(400 h^{-1} \text{Mpc})^3$  and  $1024^3$  baryon and dark matter particles. The initial conditions are based on either the *WMAP* 7-yr or *Planck* 2013 cosmologies. We quantify the agreement of our measurements with the predictions from each cosmology in Section 5.

We use five different baryon models from the suite as summarized in Table 1 and described in detail in Le Brun et al. (2014) and McCarthy et al. (2014) and references therein. NOCOOL is a

standard non-radiative (‘adiabatic’) model. REF is the OWLS reference model and includes subgrid prescriptions for star formation (Schaye & Dalla Vecchia 2008), metal-dependent radiative cooling (Wiersma, Schaye & Smith 2009a), stellar evolution, mass loss, chemical enrichment (Wiersma et al. 2009b) and a kinetic supernova feedback prescription (Dalla Vecchia & Schaye 2008). The AGN models are built on the REF model and additionally include a prescription for black hole growth and feedback from AGN (Booth & Schaye 2009). The three AGN models differ only in their choice of the key parameter of the AGN feedback model  $\Delta T_{\text{heat}}$ , which is the temperature by which neighbouring gas is raised due to feedback. Increasing the value of  $\Delta T_{\text{heat}}$  results in more energetic feedback events, and also leads to more bursty feedback, since the black holes must accrete more matter in order to heat neighbouring gas to a higher adiabat.

Following McCarthy et al. (2014), we produce light cones of the simulations by stacking randomly rotated and translated simulation snapshots (redshift slices) along the LoS back to  $z = 3$ . Note that we use 15 snapshots at fixed redshift intervals between  $z = 0$  and  $z = 3$  in the construction of the light cones. This ensures a good comoving distance resolution, which is required to capture the evolution of the halo mass function and the tSZ signal. The light cones are used to produce  $5^\circ \times 5^\circ$  maps of the  $y$ , shear ( $\gamma_1, \gamma_2$ ) and convergence ( $\kappa$ ) fields. We construct 10 different light cone realizations for each feedback model and for the two background cosmologies. Note that in the production of the lensing maps we adopt the source redshift distribution,  $n(z)$ , from the RCSLenS survey to produce a consistent comparison with the observations.

From our previous comparisons to the cross-correlation of CFHTLenS weak lensing data with the initial public *Planck* data in Hojjati et al. (2015), we found that the data mildly preferred a *WMAP* 7-yr cosmology to the *Planck* 2013 cosmology. We will revisit this in Section 5 in the context of the new RCSLenS data.

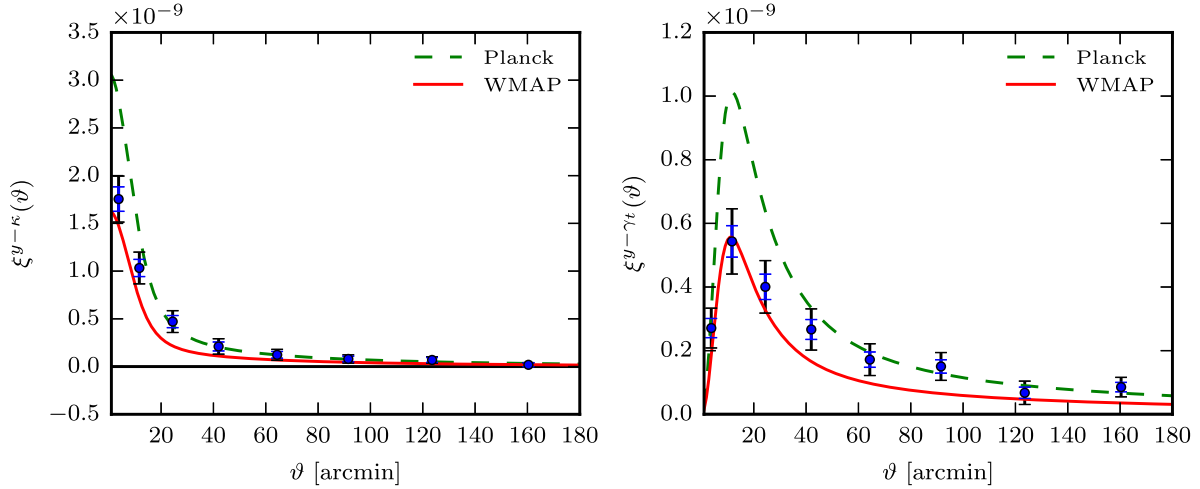
## 3 OBSERVED CROSS-CORRELATION

Below we describe our cross-correlation measurements between tSZ  $y$  and galaxy lensing quantities using the configuration-space and Fourier-space estimators described in Section 2.1.1.

### 3.1 Configuration-space analysis

We perform the cross-correlations on the 14 RCSLenS fields. The measurements from the fields converge around the mean values at each bin of angular separation with a scatter that is due to statistical noise and sampling variance. To combine the fields, we take the weighted mean of the field measurements, where the weights are determined by the total *lensfit* weight (see Miller et al. 2013 for technical definitions).

As described earlier, to improve the SNR and suppress statistical noise, we use ‘extended’  $y$  maps around each RCSLenS field to



**Figure 2.** Cross-correlation measurements of  $y-\kappa$  (left) and  $y-\gamma_t$  (right) from RCSLenS. The larger (smaller) error bars represent uncertainties after (before) including our estimate of the sampling variance contribution (see Section 4). Halo model predictions using UPP with *WMAP* 7-yr and *Planck* cosmologies are also overplotted for comparison.

increase the cross-correlation area. For RCSLenS, we extend our measurements to an angular separation of  $3^\circ$ , and hence include  $4^\circ$  wide bands around the RCSLenS fields.

We compute our configuration-space estimators as described below. For  $y-\gamma_t$ , we work at the catalogue level and compute the two-point correlation function as

$$\xi^{y-\gamma_t}(\vartheta) = \frac{\sum_{ij} y^i e_t^{ij} w^j \Delta_{ij}(\vartheta)}{\sum_{ij} w^j \Delta_{ij}(\vartheta)} \frac{1}{1 + K(\vartheta)}, \quad (19)$$

where  $y^i$  is the value of pixel  $i$  of the tSZ map,  $e_t^{ij}$  is the tangential ellipticity of galaxy  $j$  in the catalogue with respect to pixel  $i$  and  $w^j$  is the *lensfit* weight. The  $(1 + K(\vartheta))^{-1}$  factor accounts for the multiplicative calibration correction (see Hildebrandt et al. 2016 for details):

$$\frac{1}{1 + K(\vartheta)} = \frac{\sum_{ij} w^j \Delta_{ij}(\vartheta)}{\sum_{ij} w^j (1 + m^j) \Delta_{ij}(\vartheta)}. \quad (20)$$

Finally,  $\Delta_{ij}(\vartheta)$  is imposed by our binning scheme and is 1 if the angular separation is inside the bin centred at  $\vartheta$  and 0 otherwise.

For the  $y-\kappa$  cross-correlation, we use the corresponding mass maps for each field and compute the correlation function as

$$\xi^{y-\kappa}(\vartheta) = \frac{\sum_{ij} y^i \kappa^j \Delta_{ij}(\vartheta)}{\sum_{ij} \Delta_{ij}(\vartheta)}, \quad (21)$$

where  $\kappa^j$  is the convergence value at pixel  $j$  and includes the necessary weighting,  $w^j$ .

Fig. 2 presents our configuration-space measurement of the RCSLenS cross-correlation with *Planck* tSZ. Our measurements are performed within eight bins of angular separation, square-root-spaced between 1 and 180 arcmin. That is, the bins are uniformly spaced between  $\sqrt{1}$  and  $\sqrt{180}$ . The filled circle data points show the  $y-\kappa$  (left) and  $y-\gamma_t$  (right) cross-correlations. To guide the eye, the solid red curves and dashed green curves represent the predictions of the halo model for *WMAP* 7-yr and *Planck* 2013 cosmologies, respectively.

### 3.2 Fourier-space measurements

In the Fourier-space analysis, we work with the convergence and tSZ maps. As detailed in Harnois-Déraps et al. (2016), it is

important to account for a number of numerical and observational effects when performing the Fourier-space analysis. These effects include data binning, map smoothing, masking, zero-padding and apodization. Failing to take such effects into account will bias the cross-correlation measurements significantly.

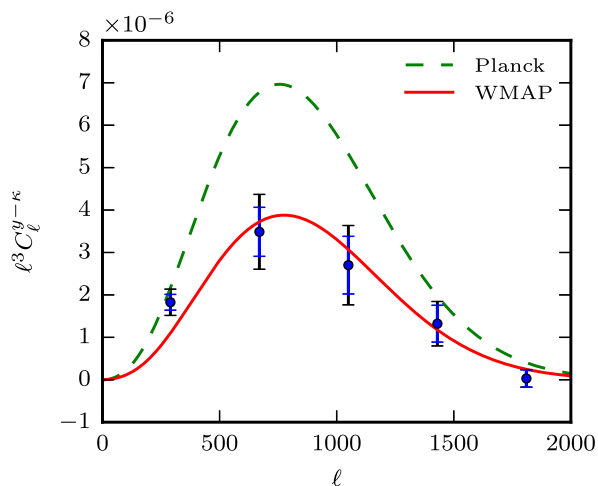
Here we adopt the forward modelling approach described in Harnois-Déraps et al. (2016), where theoretical predictions are turned into a ‘pseudo- $C_\ell$ ’, as summarized below. First, we obtain the theoretical  $C_\ell$  predictions from equations (13) and (14) as described in Section 2.3.1. We then multiply the predictions by a Gaussian smoothing kernel that matches the Gaussian filter used in constructing the  $\kappa$  maps in the mass map making process, and another smoothing kernel that accounts for the beam effect of the *Planck* satellite.

Next we include the effects of observational masks on our power spectra that break down into three components (see Harnois-Déraps et al. 2016 for details): (i) an overall downward shift of power due to the masked pixels that can be corrected for with a rescaling by the number of masked pixels; (ii) an optional apodization scheme that we apply to the masks to smooth the sharp features introduced in the power spectrum of the masked map that enhance the high- $\ell$  power spectrum measurements and (iii) a mode mixing matrix that propagates the effect of mode coupling due to the observational window.

As shown in Harnois-Déraps et al. (2016), steps (ii) and (iii) are not always necessary in the context of cross-correlation when the masks from both maps do not strongly correlate with the data. We have checked that this is indeed the case by measuring the cross-correlation signal from the cosmo-OWLS simulations with and without applying different sections of the RCSLenS masks, with and without apodization and observed that changes in the results were minor. We therefore choose to remove the steps (ii) and (iii) from the analysis pipeline. As the last step in our forward modelling, we re-bin the modelled pseudo- $C_\ell$  so that it matches the binning scheme of the data. Note that these steps have to be calculated separately for each individual field due to their distinct masks.

Fig. 3 shows our Fourier-space measurement for the  $y-\kappa$  cross-correlation, where halo model predictions for the *WMAP* 7-yr and *Planck* cosmologies are also overplotted. Our Fourier-space measurement is consistent with the configuration-space measurement





**Figure 3.** Similar to Fig. 2 but for Fourier-space estimator,  $C_\ell^{y-\kappa}$ .

overall. Namely, the data points provide a better match to *WMAP* 7-yr cosmology prediction on small physical scales (large  $\ell$  modes) and tend to move towards the *Planck* prediction on large physical scales (small  $\ell$  modes). A more detailed comparison is non-trivial as different scales ( $\ell$  modes) are mixed in the configuration-space measurements.

The details of error estimation and the significance of the detection are described in Section 4.

## 4 ESTIMATION OF COVARIANCE MATRICES AND SIGNIFICANCE OF DETECTION

In this section, we describe the procedure for constructing the covariance matrix and the statistical analysis that we perform to estimate the significance of our measurements. We have investigated several methods for estimating the covariance matrix for the type of cross-correlations performed in this paper.

### 4.1 Configuration-space covariance

To estimate the covariance matrix we follow the method of van Waerbeke et al. (2013). We first produce 300 random shear catalogues from each of the RCSLenS fields. We create these catalogues by randomly rotating the individual galaxies. This procedure will destroy the underlying lensing signal and create catalogues with pure statistical lensing noise. We then construct the  $y-\gamma_t$  covariance matrix,  $C^{y-\gamma_t}$ , by cross-correlating the randomized shear maps for each field with the  $y$  map.

To construct the  $y-\kappa$  covariance matrix, we perform our standard mass reconstruction procedure on each of the 300 random shear catalogues to get a set of convergence noise maps. We then compute the covariance matrix by cross-correlating the  $y$  maps with these random convergence maps. We follow the same procedure of map making (masking, smoothing, etc.) in the measurements from random maps as we did for the actual measurement. This ensures that our error estimation is representative of the underlying covariance matrix.

Note that we also need to ‘debias’ the inverse covariance matrix by a debiasing factor as described in Hartlap, Simon & Schneider (2007):

$$\alpha = (n - p - 2)/(n - 1), \quad (22)$$

where  $p$  is the number of data bins and  $n$  is the number of random maps used in the covariance estimation.<sup>2</sup>

The correlation coefficients are shown in Fig. 4 for  $y-\kappa$  (left) and  $y-\gamma_t$  (right). As a characteristic of configuration space, there is a high level of correlation between pairs of data points within each estimator. This is more pronounced for  $y-\kappa$  since the mass map construction is a non-local operation, and also that the maps are smoothed that creates correlation by definition. Having a lower level of bin-to-bin correlations is another reason why one might want to work with tangential shear measurements rather than mass maps in such cross-correlation studies.

### 4.2 Fourier-space covariance

For the covariance matrix estimation in Fourier space, we follow a similar procedure as in configuration space. We first Fourier transform the random convergence maps, and then follow the same analysis for the measurements (see Section 3). The resulting cross-correlation measurements create a large sample that can be used to construct the covariance matrix. Similar to the configuration-space analysis, we also debias the computed covariance matrix.

Fig. 4, right-hand panel, shows the cross-correlation coefficients for the  $\ell$  bins (Note that we chose to work with five linearly spaced bins between  $\ell = 100$  and  $\ell = 2000$ .) As expected, there is not much bin-to-bin correlation and the off-diagonal elements are small.

### 4.3 Estimating the contribution from the sampling variance

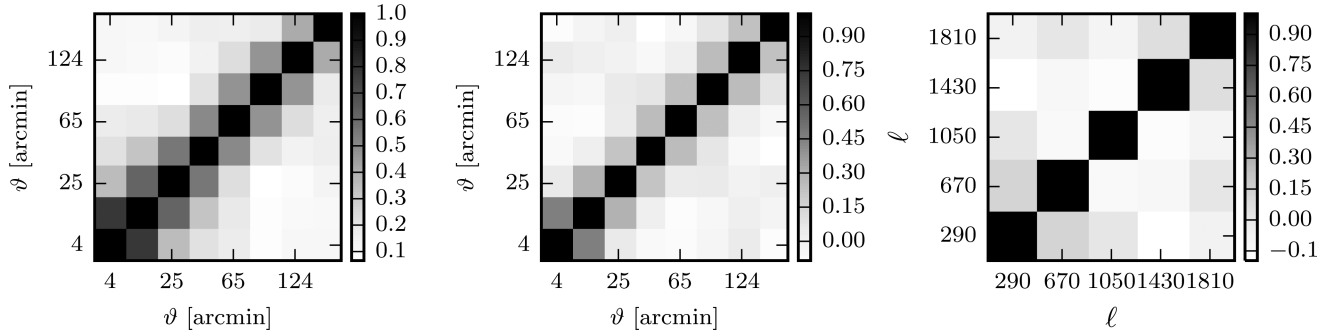
Constructing the covariance matrix as described above includes the statistical noise contribution only. There is, however, a considerable scatter in the cross-correlation signal between the individual fields. A comparison of the observed scatter to that among different LoS of the (noise-free) simulations shows that the sampling variance contribution is non-negligible. We therefore need to include the contribution to the covariance matrix from sampling variance.

We are not able, however, to estimate a reliable covariance matrix that includes sampling variance since the number of samples we have access to is very limited and the resulting covariance matrix will be noisy and non-invertible. We only have a small number of fields from the lensing surveys (14 fields from RCSLenS is not nearly enough) and the same is true for the number of LoS maps from hydrodynamical simulations (10 LoS). Instead, we can estimate the sampling variance contribution by quantifying by how much we need to ‘inflate’ our errors to account for the impact of sampling variance.

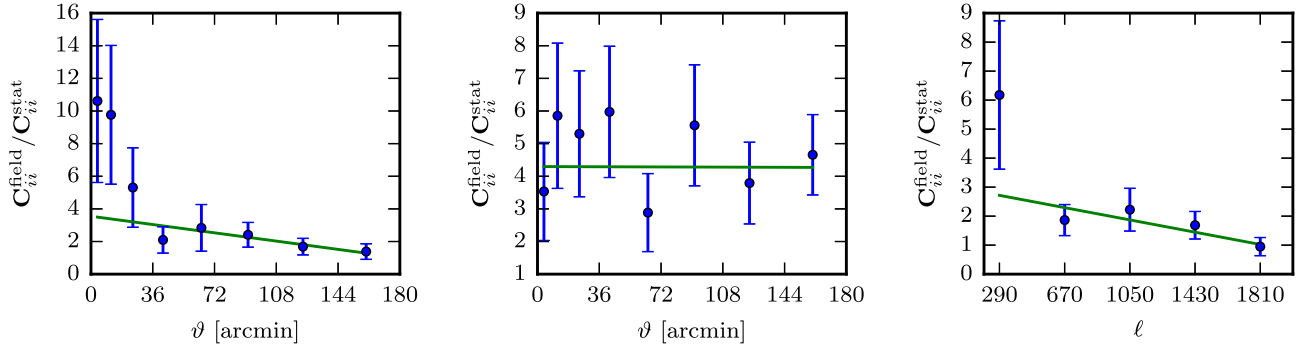
Note that the scatter in the cross-correlation signal from the individual fields is due to both statistical noise and sampling variance. We compare the scatter (or variance) in each angular bin to that of the diagonal elements of the reconstructed covariance matrix that we obtained from the previous section (which quantifies the statistical uncertainty alone). We estimate the scaling factor by which we should inflate the computed covariance matrix to match the observed scatter.

The ratio between the variance between the fields and the statistical covariance is scale independent for the tangential shear but shows some scale dependence for the other two estimators. We therefore wish to find a simple description of the ratio  $r_i$  at some

<sup>2</sup> In principle we should also implement the treatment of Sellentin & Heavens (2016), but the precision of our measurement is not high enough to worry about such errors.



**Figure 4.** Cross-correlation coefficient matrix of the angular bins for the configuration-space  $y\text{-}\kappa$  (left) and  $y\text{-}\gamma_t$  (middle), and the Fourier-space  $y\text{-}\kappa$  (right) estimators. Angular bins are more correlated for the  $y\text{-}\kappa$  estimator compared to  $y\text{-}\gamma_t$  or the Fourier-space estimator.



**Figure 5.** Ratios of the variance between the 14 RCSLenS fields and the variance estimated from random shear maps, as described in Section 4. The best-fitting linear model for the ratios is shown in green.

scale  $i$  between the field variance and statistical covariance, such that the statistical covariance  $\mathbf{C}^{\text{stat}}$  can be rescaled as

$$\mathbf{C}_{ij} = \mathbf{C}_{ij}^{\text{stat}} \sqrt{r_i r_j}. \quad (23)$$

We model the ratio  $r_i$  as a linear function of the scale. The model is then fit to the observer ratios between the field variances and statistical covariance. The errors on the observed ratios are estimated by taking 1000 bootstrap resamplings of the 14 RCSLenS fields and calculating the ratio from the variance of those resampled fields. The errors are highly correlated themselves but the error covariance is not invertible for the same reason the data covariance of the 14 fields is not invertible; the number of independent fields is too small. The observed ratios and the best-fitting models  $r_i$  are shown in Fig. 5. We use these best-fitting models to rescale the statistical covariance according to equation (23) to obtain an estimate of the full covariance.

#### 4.4 $\chi^2$ analysis and significance of detection

We quantify the significance of our measurements using the SNR estimator as described below. We assume that the RCSLenS fields are sufficiently separated such that they can be treated as independent, ignoring field-to-field covariance.

First, we introduce the cross-correlation bias factor,  $A_{\text{tSZ}}$ , through

$$\mathcal{V} = \tilde{\xi} - A_{\text{tSZ}} \hat{\xi}. \quad (24)$$

$A_{\text{tSZ}}$  quantifies the difference in amplitude between the measured ( $\tilde{\xi}$ ) and predicted ( $\hat{\xi}$ ) cross-correlation function. The prediction can be from either the halo model or from hydrodynamical simulations. Using  $\mathcal{V}$ , we define the  $\chi^2$  as

$$\chi^2 = \mathcal{V} \mathbf{C}^{-1} \mathcal{V}^T, \quad (25)$$

**Table 2.** A summary of the  $\chi^2_{\text{null}}$  values before and after including the sampling variance contribution according to the adjustment procedure of Section 4.3. There are eight angular bins, or degrees of freedom (DoF), at which the individual estimators are computed. Combining the estimators increases the DoF accordingly.

| Estimator                  | DoF | $\chi^2_{\text{null}}$ , stat. err. only | $\chi^2_{\text{null}}$ , adjusted |
|----------------------------|-----|--|-----------------------------------|
| $\xi^{y\text{-}\kappa}$    | 8   | 193.5                                    | 56.2                              |
| $\xi^{y\text{-}\gamma_t}$  | 8   | 307.4                                    | 71.6                              |
| Combined                   | 16  | 328.7                                    | 124.2                             |
| $C_\ell^{y\text{-}\kappa}$ | 5   | 156.4                                    | 64.9                              |

where  $\mathbf{C}$  is the covariance matrix.

We define  $\chi^2_{\text{null}}$  by setting  $A_{\text{tSZ}} = 0$ . In addition,  $\chi^2_{\text{min}}$  is found by minimizing equation (25) with respect to  $A_{\text{tSZ}}$ :

$$\chi^2_{\text{null}} : A_{\text{tSZ}} = 0, \quad (26)$$

$$\chi^2_{\text{min}} : A_{\text{tSZ}, \text{min}}. \quad (27)$$

In other words,  $\chi^2_{\text{min}}$  quantifies the goodness of fit between the measurements and our model prediction after marginalizing over  $A_{\text{tSZ}}$ .

Table 2 summarizes the  $\chi^2_{\text{null}}$  values from the measurements before and after including the sampling variance contribution. The values are quoted for individual estimators and when they are combined. The  $\chi^2_{\text{null}}$  is always higher for  $y\text{-}\gamma_t$  estimator, demonstrating that it is a better estimator for our cross-correlation analysis. It also improves when we combine the estimators but we should consider that  $\chi^2_{\text{null}}$  increases at the expense of adding extra degrees of freedom (DoF). Namely, we have eight angular bins for each estimator and combining the two, there are 16 DoF that introduce a redundancy

**Table 3.** A summary of the statistical analysis of the cross-correlation measurements. For the configuration-space estimators, the results are shown for each estimator independently and when they are combined. SNR quantifies the significance of detection after a fit to model predictions (halo model). SNR values are shown before (SNR, stat. err. only) and after (SNR, adjusted) adjustment for sampling variance uncertainties according to the description of Section 4.3, while  $A_{\text{tSZ}}$  values are quoted after the adjustment. The *Planck* cosmology predicts higher amplitude than *WMAP* 7-yr cosmology so that overall, the *WMAP* 7-yr cosmology predictions are in better agreement with the measurements.

| Estimator           | SNR, stat. err. only | SNR, adjusted | $A_{\text{tSZ}}$ , <i>WMAP</i> 7-yr | $A_{\text{tSZ}}$ , <i>Planck</i> |
|---------------------|----------------------|---------------|-------------------------------------|----------------------------------|
| $\xi^{y-\kappa}$    | 13.3                 | 7.1           | $1.18 \pm 0.17$                     | $0.64 \pm 0.09$                  |
| $\xi^{y-\gamma_t}$  | 16.8                 | 8.1           | $1.27 \pm 0.16$                     | $0.68 \pm 0.08$                  |
| Combined            | 17.1                 | 10.6          | $1.23 \pm 0.12$                     | $0.66 \pm 0.06$                  |
| $C_\ell^{y-\kappa}$ | 11.6                 | 7.5           | $1.07 \pm 0.14$                     | $0.60 \pm 0.08$                  |

due to the correlation between the two estimators so that  $\chi_{\text{null}}^2$  does not increase by a factor of 2.

Finally, we define the SNR as follows. We wish to quantify how strongly we can reject the null hypothesis  $H_0$ , that no correlation exists between lensing and tSZ, in favour of the alternative hypothesis  $H_1$ , that the cross-correlation is well described by our fiducial model up to a scaling by the cross-correlation bias  $A_{\text{tSZ}}$ . To this end, we employ a likelihood ratio method. The deviance  $\mathcal{D}$  is given by the logarithm of the likelihood ratio between  $H_0$  and  $H_1$ :

$$\mathcal{D} = -2 \log \frac{\mathcal{L}(\mathbf{d}|H_0)}{\mathcal{L}(\mathbf{d}|H_1)}. \quad (28)$$

For Gaussian likelihoods, the deviance can then be written as

$$\mathcal{D} = \chi_{\text{null}}^2 - \chi_{\text{min}}^2. \quad (29)$$

If  $H_1$  can be characterized by a single, linear parameter,  $\mathcal{D}$  is distributed as  $\chi^2$  with one degree of freedom (Williams 2001). The significance in units of standard deviations  $\sigma$  of the rejection of the null hypothesis, i.e. the significance of detection, is therefore given by

$$\text{SNR} = \sqrt{\chi_{\text{null}}^2 - \chi_{\text{min}}^2}. \quad (30)$$

Table 3 summarizes the significance analysis of our measurements. We show the SNR and best-fitting amplitude  $A_{\text{tSZ}}$ , for the theoretical halo model predictions with *WMAP* 7-yr and *Planck* cosmologies. The results are presented for each estimator independently and for their combination. Note that all the values in Table 3 are adjusted to account for the sampling variance, as described in Section 4.3. To estimate the combined covariance matrix, we place the covariance for individual estimators as block diagonal elements of combined matrix and compute the off-diagonal blocks (the covariance between the two estimators).

The predictions from *WMAP* 7-yr cosmology are relatively favoured in our analysis, which is consistent with the results of previous studies (e.g. McCarthy et al. 2014; Hojjati et al. 2015). We, however, find similar SNR values from both cosmologies because the effect of the different cosmologies on the halo model prediction can be largely accounted for by an overall rescaling ( $A_{\text{tSZ}}$ ). After rescaling, the remaining minor differences are due to the shape of the cross-correlation signal so that the SNR depends only weakly on the cosmology.

We obtain a  $13.3\sigma$  and  $16.8\sigma$  from  $y-\kappa$  and  $y-\gamma_t$  estimators, respectively, when we only consider the statistical noise in the covariance matrix (before the adjustment prescription of Section 4.3).<sup>3</sup>

<sup>3</sup> Note that we are quoting the detection levels from a statistical noise-only covariance matrix so that we can compare to the previous literature, including

The  $13.3\sigma$  significance from  $y-\kappa$  estimator should be compared to the  $\sim 6\sigma$  detection from the same estimator in van Waerbeke et al. (2014) where CFHTLenS data are used instead. As expected, RCSLenS yields an improvement in the SNR and  $y-\gamma_t$  improves it further. Including sampling variance in the covariance matrix decreases the detection significance from RCSLenS data to  $7.1\sigma$  and  $8.1\sigma$  for the  $y-\kappa$  and  $y-\gamma_t$  estimators, respectively.

We perform a similar analysis in Fourier space where the data vector is given by the pseudo- $C_\ell$ s and the results are included in Table 3. The SNR values are in agreement with the configuration-space analysis.<sup>4</sup> We see a similar trend as in the configuration-space analysis in that there is a better agreement with the *WMAP* 7-yr halo model predictions ( $A_{\text{tSZ}}$  is closer to 1) while the *Planck* cosmology predicts a high amplitude.

Table 3 summarizes the predictions from the halo model framework with a fixed pressure profile for gas (UPP). In Section 5, we revisit this by comparing to predictions from hydrodynamical simulations where haloes with different mass and at different redshifts have a variety of gas pressure profiles. We show that we find better agreement with models where AGN feedback is present in haloes.

#### 4.5 Impact of maximum angular separation

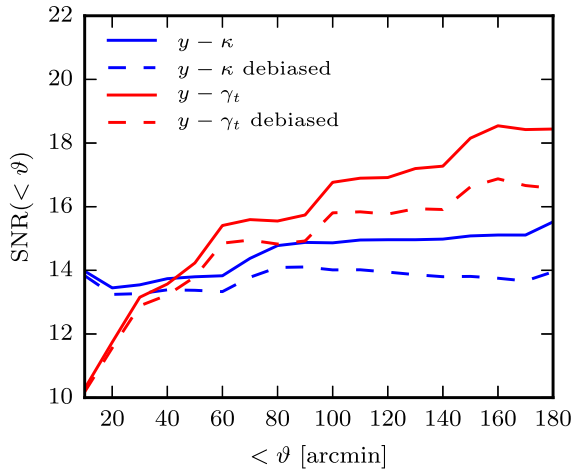
The two configuration-space estimators we use probe different dynamical scales by definition. This means that as we include cross-correlations at larger angular scales, information is captured at a different rate by the two estimators. For a survey with limited sky coverage, combining the two estimators will therefore improve the SNR of the measurements. In the following, we quantify this improvement of the SNR.

In Fig. 6, we plot the SNR values as a function of the maximum angular separation for both estimators. In addition, we also include the same quantities when debiased using equation (22) to highlight the effect of increasing DoF on the debiasing factor. Each angular bin is 10 arcmin wide and adding more bins means including cross-correlation at larger angular scales.

We observe that the  $y-\kappa$  measurement starts off with a higher SNR relative to  $y-\gamma_t$  at small angular separations. The SNR in  $y-\kappa$  levels off very quickly with little information added above  $1^\circ$  separation. The shallow SNR slope of the  $y-\kappa$  curve is partly due

the results of van Waerbeke et al. (2014), where a similar approach is taken in the construction of the covariance matrix (i.e. only statistical noise is considered).

<sup>4</sup> Note that the Fourier-space analysis is performed by pipeline 3 in Harnois-Déraps et al. (2016). Different pipelines give slightly different but consistent results.



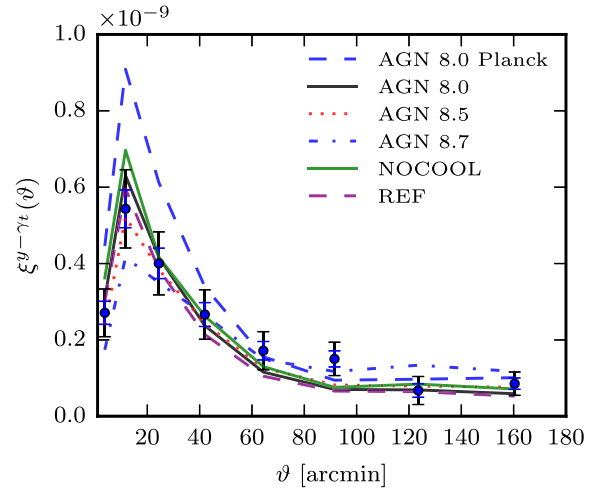
**Figure 6.** The SNR as a function of the maximum angular separation for the two configuration-space estimators, with and without debiasing (as described in Section 4.1). The slope of the lines is different for the two estimators due to the different information they capture as a function of angular separation. For  $y-\kappa$ , most of the signal is in the first few bins making it a better candidate at small scales, while  $y-\gamma_t$  has a larger slope and catches up quickly. Eventually, the two estimators approach a plateau where they contain the same amount of cross-correlation information. Note that the plots show the SNR before the ‘adjustment’ procedure of Section 4.3.

to the Gaussian smoothing kernel that is used in reconstructing the mass maps which spreads the signal within the width of the kernel. The  $y-\gamma_t$  cross-correlation, on the other hand, has a higher rate of gain in SNR and catches up with the convergence rapidly. Eventually, the two estimators approach a plateau as the cross-correlation signals drop to zero. At that point, both contain the same amount of cross-correlation information.

Note that we limit ourselves to a maximum angular separation of  $3^\circ$  in the RCSLenS measurements since the measurement is very noisy beyond that. Fig. 6 indicates that the two estimators might not have converged to the limit where the information is saturated (a plateau in the SNR curve). Since each estimator captures different information up to  $3^\circ$ , combining them improves the measurement significance (see Table 3). With surveys like the Kilo-Degree Surveys (KiDS; de Jong et al. 2013), the Dark Energy Survey (DES; Abbott et al. 2016) and the Hyper Suprime-Cam Survey (HSC; Miyazaki et al. 2012), where the coverage area is larger, we will be able to go to larger angular separations where the information from our estimators is saturated. The signal at such large scales is primarily dependent on cosmology and quite independent of the details of the astrophysical processes inside haloes (see Hojjati et al. 2015 for more details). This could, in principle, provide a new probe of cosmology based on the cross-correlation of baryons and lensing on distinct scales and redshifts.

## 5 IMPLICATIONS FOR COSMOLOGY AND ASTROPHYSICS

In Section 3, we compared our measurements to predictions from the theoretical halo model. The halo model approach, however, has limitations for the type of cross-correlation we are considering. For example, in our analysis we cross-correlate every source in the sky that produces a tSZ signal with every source that produces a lensing signal. A fundamental assumption of the halo model, however, is that all the mass in the Universe is in spherical haloes, which is not an accurate description of the large-scale structure in

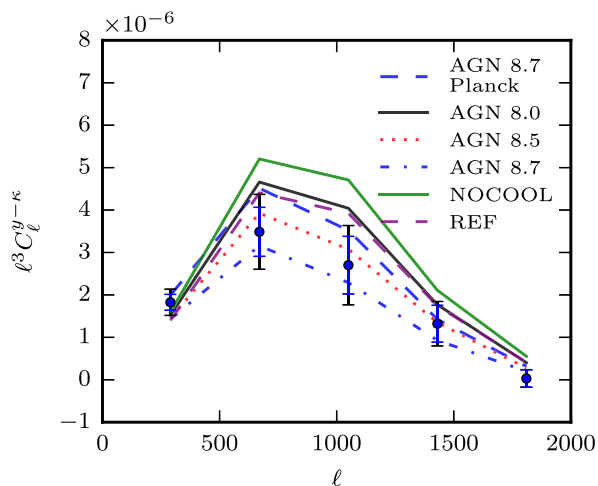


**Figure 7.** Comparisons of our cross-correlation measurement from RCSLenS to predictions from hydrodynamical simulations. The larger (smaller) error bars represent uncertainties after (before) including our estimate of the sampling variance contribution (see Section 4). Different baryon feedback models with *WMAP* 7-yr cosmology are shown for  $y-\gamma_t$  estimator (we are not showing the plots for  $y-\kappa$  as they are very similar). Baryon feedback has an impact on the cross-correlation signal at small scales.

the Universe. There are other structures such as filaments, walls or free flowing diffuse gas in the Universe, so that matching them with spherical haloes could lead to biased inference of results (see Hojjati et al. 2015). Another shortcoming is that our halo model analysis considers a fixed pressure profile for diffuse gas, while it has been demonstrated in various studies that the UPP does not necessarily describe the gas around low-mass haloes particularly well (e.g. Battaglia et al. 2012; Le Brun, McCarthy & Melin 2015).

Here we employ the cosmo-OWLS suite of cosmological hydrodynamical simulations (see Section 2.4) that includes various simulations with different baryonic feedback models. The cosmo-OWLS suite provides a wide range of tSZ and lensing (convergence and shear) maps allowing us to study the impact of baryons on the cross-correlation signal. We follow the same steps as we did with the real data to extract the cross-correlation signal from the simulated maps.

Fig. 7 compares our measured configuration-space cross-correlation signal to those from simulations with different feedback models. The plots are for the five baryon models using the *WMAP* 7-yr cosmology, and the AGN 8.0 model using the *Planck* cosmology is also plotted for comparison. Note that baryon models make the largest difference at small scales due to mechanisms that change the density and temperature of the gas inside clusters. For the (non-physical) NOCOOL model, the gas can reach very high densities near the centre of dark matter haloes and is very hot since there is no cooling mechanism in place. This leads to a high tSZ and hence a high cross-correlation signal. After including the main baryonic processes in the simulation (e.g. radiative cooling, star formation and SN winds), we see that the signal drops on small scales. Adding AGN feedback warms up the gas but also expels it to larger distances from the centre of haloes. This explains why we see a lower signal at small scales but a higher signal at intermediate scales for the AGN 8.7 model. Note that the scatter of the LoS signal varies for different models due to the details of the baryon processes so that, for example, the AGN 8.7 model creates a larger sampling variance. The mean signal of the feedback models is also affected by the cosmological parameters at all scales. Adopting a *Planck* cosmology



**Figure 8.** Same as Fig. 7 but for the Fourier-space estimator,  $C_\ell^{y-\kappa}$ .

produces a higher signal at all scales and for all models. This is mainly due to the larger values of  $\Omega_b$ ,  $\Omega_m$  and particularly  $\sigma_8$ , in the *Planck* 2013 cosmology compared to that of the *WMAP* 7-yr cosmology.

We summarize in Table 4 our  $\chi^2$  analysis for feedback model predictions relative to our measurements. We find that the data prefer a *WMAP* 7-yr cosmology to the *Planck* 2013 cosmology for all of the baryon feedback models. This is worth stressing, given the very large differences between the models in terms of the hot gas properties that they predict (Le Brun et al. 2014), which bracket all of the main observed scaling relations of groups and clusters. The best-fitting models are underlined for both cosmologies.

Our measurements are limited by the relatively low resolution of the *Planck* tSZ maps. On small scales, our signal is diluted due to the convolution of the tSZ maps with the *Planck* beam (FWHM = 10 arcmin) that makes it hard to discriminate the feedback models with our configuration-space measurements. This highlights that high-resolution tSZ measurements can be particularly useful to overcome this limitation and open up the opportunity to discriminate the feedback models from tSZ–lensing cross-correlations.

The feedback models could be better discriminated in Fourier space through their power spectra. We therefore repeat our measurements on the simulation in the Fourier space. We apply the same procedure described in Section 3.2 to the simulated maps. Fig. 8 compares our power spectrum measurements to simulation predictions, and we have summarized the  $\chi^2$  analysis in Table 4.

Our Fourier-space analysis follows a similar trend as the configuration-space analysis. Namely, there is a general overprediction of the amplitude that is worse for the *Planck* cosmology. For the best-fitting *WMAP* 7-yr models the fitted amplitude is consistent with 1. Our estimator prefers the AGN 8.7 model in all cases with a *Planck* cosmology that is different than configuration-space estimator where the AGN 8.5 was preferred.<sup>5</sup> There are a few reasons for these minor differences. For example, the binning schemes are different and give different weights to bins of angular separation. Furthermore, the Fourier-based result can change by small amounts depending on precisely which pipeline from Harnois-Déraps et al. (2016) is adopted.

<sup>5</sup> We tested that if large-scale correlations ( $\vartheta > 100$  arcmin), where uncertainties are large, are removed from the analysis, the AGN 8.7 model is also equally preferred by the configuration-space estimators.

When we fit the amplitude  $A_{\text{tSZ}}$  to obtain the  $\chi^2_{\text{min}}$  or SNR values, we are in fact factoring out the scaling of the model prediction and are left with the prediction of the shape of the cross-correlation signal. The shape depends on both the cosmological parameters (weakly) and details of the baryon model so that the values in Tables 3 and 4 are a measure of how well the model shape matches the measurement. By comparing the  $\chi^2_{\text{min}}$  values from the two cosmologies in Table 4, the general conclusion of our analysis is that significant AGN feedback in baryon models is required to match the measurements well. Note, however, that while there are differences in the amplitude (and shape) of the cross-correlation signal, the predictions from the two cosmology are not in tension with the measurements when one considers the current uncertainties in the values of the cosmological parameters (e.g.  $\sigma_8$ ).

## 6 SUMMARY AND DISCUSSION

We have performed cross-correlations of the public *Planck* 2015 tSZ map with the public weak lensing shear data from the RCSLenS. We have demonstrated that such cross-correlation measurements between two independent data sets are free from contamination by residual systematics in each data set, allowing us to make an initial assessment of the implications of the measured cross-correlations for cosmology and intracluster medium (ICM) physics.

Our cross-correlations are performed at the map level where every object is contributing to the signal. In other words, this is not a stacking analysis where measurements are done around identified haloes. Instead, we are probing all the structure in the Universe (haloes, filaments, etc.) and the associated baryon distribution including diffuse gas in the intergalactic medium.

We performed our analysis using two configuration-space estimators,  $\xi^{y-\gamma_t}$  and  $\xi^{y-\kappa}$ , and a Fourier-space analysis with  $C_\ell^{y-\kappa}$  for completeness. Configuration-space estimators have the advantage that they are less affected by the details of map making processes (masks, apodization, etc.) and the analysis is straightforward. We showed that the estimators probe different dynamical scales so that combining them can improve the SNR of the measurement.

Based only on the estimation of statistical uncertainties, the cross-correlation using RCSLenS data is detected with a significance of  $13.3\sigma$  and  $16.8\sigma$  from the  $y-\kappa$  and  $y-\gamma_t$  estimators, respectively. Including the uncertainties due to the sampling variance reduces the detection to  $7.1\sigma$  and  $8.1\sigma$ , respectively. We demonstrated that RCSLenS data improve the SNR of the measurements significantly compared to previous studies where CFHTLenS data were used.

The Fourier-space analysis, while requiring significant processing to account for masking effects, is more useful for probing the impact of physical effects at different scales. We work with  $C_\ell^{y-\kappa}$  and test for consistency of the results with the configuration-space estimators. We reach similar conclusions for the  $C_\ell^{y-\kappa}$  measurement as the configuration-space counterpart and the same level of significance of detection.

The high level of detection compared to similar measurements in van Waerbeke et al. (2014) is due to two main improvements: the larger sky coverage offered by RCSLenS has suppressed the statistical uncertainties of the measured signal, and the final tSZ map provided by the *Planck* team is also less noisy than that used in van Waerbeke et al. (2014).

We have compared our measurements against predictions from the halo model, which adopts the empirically motivated UPP to describe the pressure of the hot gas associated with haloes. We highlighted the difficulties in estimating the covariance matrix for

**Table 4.** Summary of  $\chi^2_{\min}$  analysis of the cross-correlation measurements from hydrodynamical simulations. The error on the best-fitting amplitudes is adjusted according to description of Section 4.3. The best-fitting models are underlined for both cosmologies. The *WMAP* 7-yr predictions fit data better for all baryonic models. The AGN 8.5 model is preferred by the configuration-space measurements while the Fourier-space measurements prefer the AGN 8.7 model.

|               | Model   | $\chi^2_{\min}$ , <i>WMAP</i> 7-yr | $A_{\text{tSZ}}$ , <i>WMAP</i> 7-yr | $\chi^2_{\min}$ , <i>Planck</i> | $A_{\text{tSZ}}$ , <i>Planck</i>  |
|---------------|---------|------------------------------------|-------------------------------------|---------------------------------|-----------------------------------|
| Config. space | AGN 8.0 | 5.3                                | $1.00 \pm 0.12$                     | <u>5.4</u>                      | <u><math>0.68 \pm 0.08</math></u> |
|               | AGN 8.5 | <u>3.2</u>                         | <u><math>1.10 \pm 0.13</math></u>   | 5.9                             | $0.74 \pm 0.09$                   |
|               | AGN 8.7 | 8.6                                | $1.01 \pm 0.13$                     | 8.3                             | $0.72 \pm 0.09$                   |
|               | NOCOOL  | 5.7                                | $0.89 \pm 0.11$                     | 6.1                             | $0.62 \pm 0.08$                   |
|               | REF     | 5.7                                | $1.06 \pm 0.13$                     | 5.8                             | $0.74 \pm 0.09$                   |
| Fourier space | AGN 8.0 | 6.1                                | $0.83 \pm 0.11$                     | 6.5                             | $0.57 \pm 0.07$                   |
|               | AGN 8.5 | 3.3                                | $1.01 \pm 0.13$                     | 4.0                             | $0.68 \pm 0.09$                   |
|               | AGN 8.7 | <u>1.4</u>                         | <u><math>1.20 \pm 0.15</math></u>   | <u>1.7</u>                      | <u><math>0.83 \pm 0.10</math></u> |
|               | NOCOOL  | 8.7                                | $0.72 \pm 0.10$                     | 8.2                             | $0.50 \pm 0.07$                   |
|               | REF     | 7.2                                | $0.86 \pm 0.11$                     | 7.2                             | $0.61 \pm 0.08$                   |

the type of cross-correlation measurement we consider in this paper. Our error analysis includes contributions from both statistical uncertainty and sampling variance. The large sampling variance in the cross-correlation signal originates mainly from the tSZ maps due to the dependence of the tSZ signal on the halo mass, AGN feedback and other stochastic processes. We estimated its contribution from field-to-field variance, but recognize that better estimation requires access to more data or more hydrodynamical simulations. Predictions from a *WMAP* 7-yr best-fitting cosmology match the data better than those based on the *Planck* cosmology, in agreement with previous studies (e.g. McCarthy et al. 2014).

Finally, we employed the cosmo-OWLS hydrodynamical simulations (Le Brun et al. 2014), using synthetic tSZ and weak lensing maps produced for a wide range of baryonic physics models in both the *WMAP* 7-yr and *Planck* cosmologies. In agreement with the findings of the halo model results, the comparison to the predictions of the simulations yields a preference for the *WMAP* 7-yr cosmology regardless of which feedback model is adopted. This is noteworthy, given the vast differences in the models in terms of their predictions for the ICM properties of groups and clusters (which bracket the observed hot gas properties of local groups and clusters; see Le Brun et al. 2014). The detailed shape of the measured cross-correlations tends to prefer models that invoke significant feedback from AGN, consistent with what is found from the analysis of observed scaling relations, although there is still some degeneracy between the adopted cosmological parameters and the treatment of feedback physics. Future high-resolution CMB experiments combined with large sky area from a galaxy survey can in principle break the degeneracy between feedback models and place tighter constraints on the model parameters.

We highlighted the difficulties in estimating the covariance matrix for the type of cross-correlation measurement we consider in this paper. The large sampling variance in the cross-correlation signal, which originates mainly from the tSZ maps, requires access to more data or more hydrodynamical simulations to be accurately estimated. With the limited data we have, the covariance matrix that contained the contribution from sampling variance was noisy, making it impossible to perform a robust significance analysis of the measurements. This is an area where more work is required and we will pursue this in future work.

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## APPENDIX A: EXTRA CONSIDERATIONS IN $\kappa$ -MAP RECONSTRUCTION

In the following, we describe the set of extra processing steps we have performed in our  $\kappa$ -map reconstruction pipeline to improve the SNR of our cross-correlation measurements. These include the selection function applied to the lensing shear catalogue, adjustments

in the reconstruction process and proper masking of the contamination in the tSZ  $y$  maps.

### A1 Magnitude selection

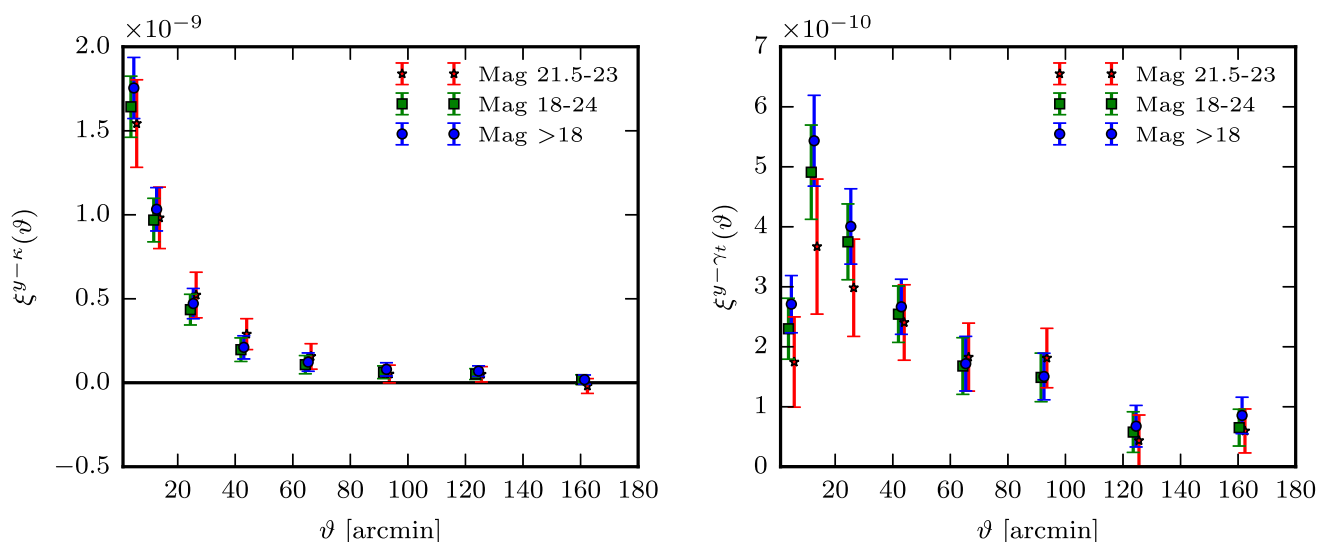
One of the parameters that we can optimize to increase the SNR is the magnitude selection function with which we select galaxies from the shear catalogue (and then make convergence maps from). This is not trivial as it is not obvious whether including faint sources with a noisy shear signal would improve our signal or not. To investigate this, we apply different magnitude cuts to our shear catalogue and compute the SNR of the correlation function measurement in each case.

In Fig. A1, we compare the correlation functions from three different  $r$ -band magnitude cuts: 21–23.5, 18–24 and  $>18$  (all of the objects). We find that the variations in the mean signal due to different magnitude cuts are relatively small. However, there is still considerable difference in the scatter around the mean signal that results in different SNR for the cuts. We consistently found that including all the objects (no cut) leads to a higher SNR.

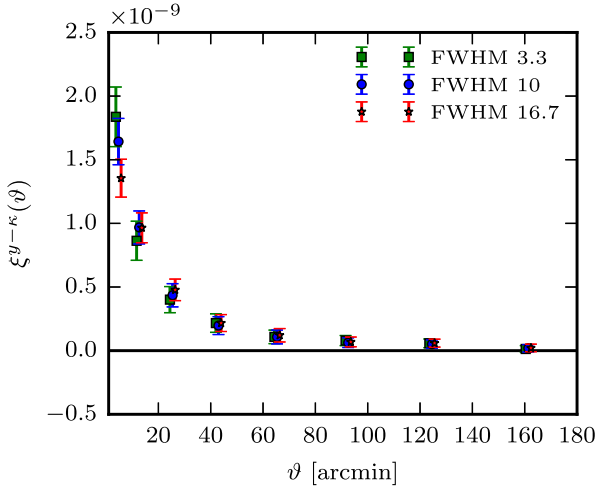
### A2 Impact of smoothing

Another factor that can change the SNR of the measurements is the smoothing kernel we apply to the lensing maps. Note that in our analysis, the resolution of the cross-correlation (the smallest angular separation) is limited by the resolution of the tSZ maps that matches the observational beam scale from the *Planck* satellite (FWHM = 10 arcmin). On the other hand, lensing maps could have a much higher resolution and the interesting question is how the smoothing scale of the lensing maps affects the SNR.

As described before, the configuration-space  $y$ - $\gamma_t$  cross-correlation works at the catalogue level without any smoothing involved. However, in making the convergence maps, we apply a smoothing kernel as described in van Waerbeke et al. (2013). One has therefore the freedom to smooth the convergence maps with an arbitrary kernel. We consider three different smoothing scales and evaluate the SNR of the cross-correlations.



**Figure A1.** Impact of different magnitude cuts on the  $y$ - $\kappa$  (left) and  $y$ - $\gamma_t$  (right) cross-correlation signals. Including all the sources in the lensing surveys yields the highest SNR.



**Figure A2.** Impact of varying the smoothing of the convergence maps on the  $y$ - $\kappa$  cross-correlation signal. We apply three different smoothing scales of  $\text{FWHM} = 3.3, 10$  and  $16.7$  arcmin during the mass map making process. While smaller scales result in a higher cross-correlation signal, the SNR is best for a smoothing scale of the same order as that of the  $y$  maps ( $\text{FWHM} = 10$  arcmin).

Fig. A2 demonstrates the impact of applying different smoothing scales ( $\text{FWHM} = 3.3, 10$  and  $16.5$  arcmin) to the convergence maps used for the  $y$ - $\kappa$  cross-correlation. Note that while narrower smoothing kernels results in a higher cross-correlation amplitude, the uncertainties also increase and it lowers the SNR. We concluded that smoothing the maps with roughly the same scale as the  $y$  maps ( $\text{FWHM} \approx 10$  arcmin) leads to the highest SNR.

### A3 Masks on the $y$ maps

Since we work with tSZ maps provided by the *Planck* collaboration, there is a minimal processing of the  $y$  maps for our analysis. We apply the masks provided by the *Planck* collaboration to remove point sources and galactic contamination. Note that the galactic mask does not significantly affect our measurements since all the RCSLenS fields are at high enough latitude. Cross-correlations are not sensitive to uncorrelated sources such as galac-

tic diffuse emissions and point sources either. We have checked that our signal is robust against the masking of the point sources (see Fig. A3).

## APPENDIX B: NULL TESTS AND OTHER EFFECTS

We have performed several consistency checks to verify our map reconstruction procedures and the robustness of the measurements. As mentioned before, an advantage of a cross-correlation analysis is that those sources of systematics that are unrelated to the measured signal will be suppressed in the measurement. This is particularly useful in the case of RCSLenS. As described below, there are residual systematics in the RCSLenS shear data (see Hildebrandt et al. 2016 for details). It is therefore important to check if these systematics contaminate our cross-correlation. We start with a description of lensing  $B$ -mode residuals in RCSLenS data.

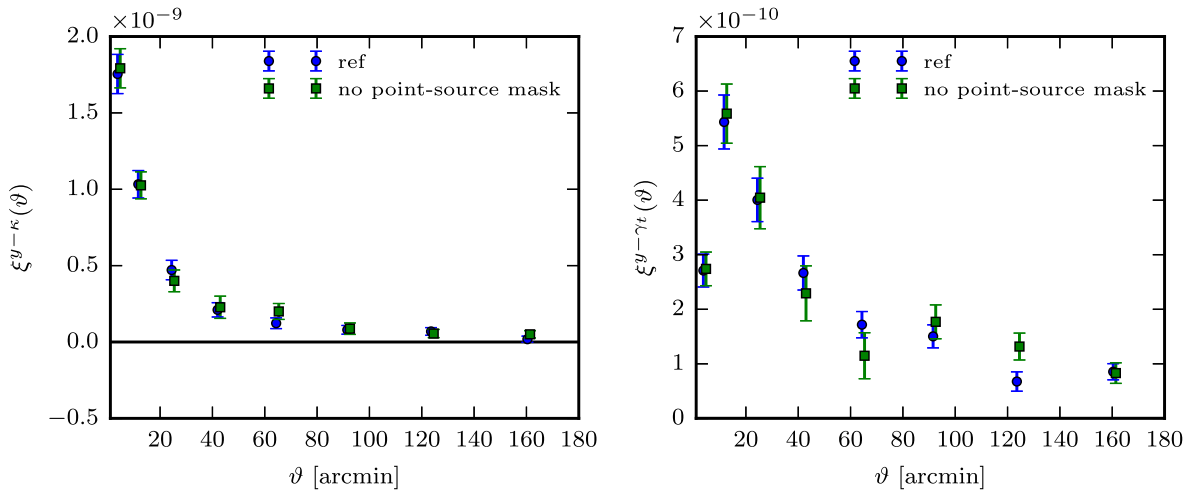
### B1 Lensing $B$ -mode residuals

In the absence of residual systematics, the scalar nature of the gravitational potential leads to a vanishing convergence  $B$ -mode signal. As one of the important systematic checks in a weak lensing survey, one should investigate the level of the  $B$ -mode present in the constructed mass maps. This is a way to check that there is not any fake lensing signal due to the equipment or analysis deficiency since a true lensing signal is curl-free.

To check for  $B$ -mode residuals in the RCSLenS data, we first create a new shear catalogue by rotating each galaxy in the original RCSLenS catalogue by  $45^\circ$  in the observation plane. This is equivalent to applying a transformation of shear components from  $(\gamma_1, \gamma_2)$  to  $(-\gamma_2, \gamma_1)$  (Schneider et al. 1998). We then follow our standard mass map making procedure to construct  $B$ -mode convergence maps,  $\kappa_B^{\text{obs}}$ , from the new catalogue. Similar to the original maps, these maps are noisy and consist of the true underlying convergence,  $\kappa_B$ , and additional statistical noise,  $\kappa_{\text{ran}}$ :

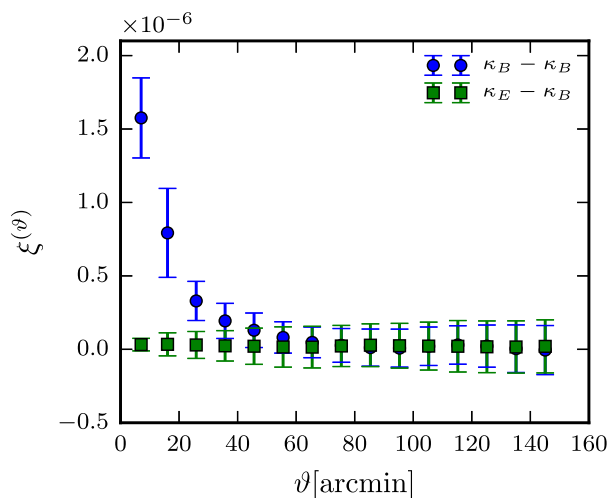
$$\kappa_B^{\text{obs}} = \kappa_B + \kappa_{\text{ran}}. \quad (\text{B1})$$

It is, therefore, necessary to distinguish between the two components when searching for residual  $B$ -modes.



**Figure A3.** The impact of masking point sources in the  $y$  map on the  $y$ - $\kappa$  (left) and  $y$ - $\gamma_t$  (right) cross-correlation analysis. The measurements are fairly robust against such contamination.





**Figure B1.** The stacked  $B$ -mode residual from the RCSLenS fields represented through the autocorrelation function, after subtracting the statistical noise contribution. The signal is not consistent with zero due to residual systematics in the shape measurements. The  $\kappa_E - \kappa_B$  cross-correlation is also shown that is consistent with zero.

To estimate  $\kappa_{\text{ran}}$ , we produce many ‘noise’ catalogue where this time the orientations of galaxies are randomly changed (these are essentially the same maps that are used to construct the covariance matrix as described in Section 4). The constructed mass maps from these catalogue would only contain statistical noise. We estimate an average statistical noise autocorrelation function,  $\bar{\xi}_{\kappa_{\text{ran}}}$ , for each RCSLenS field by averaging over the autocorrelation function from the random mass map realizations of the field. Finally, we estimate the residual  $B$ -mode signal in each of the RCSLenS fields by subtracting the statistical noise contribution computed for that field from the *observed* autocorrelation function.

Fig. B1 shows the weighted average of the residual  $B$ -mode correlation function computed from the 14 RCSLenS fields after subtracting the contribution from statistical noise. The error bars represent the error on the mean value in each angular bin. Note that there is an excess of residuals  $B$ -mode at angular separations

of  $\leq 40$  arcmin. Independent analysis of projected 3D shear power spectrum also confirms presence of excess residual  $B$ -mode signal at the corresponding scales (Hildebrandt et al. 2016), consistent with our finding. The existence of such residual systematics could be problematic for our studies and needs to be checked as we describe in the following.

In Fig. B1, we show  $E$ - and  $B$ -mode mass map cross-correlation from RCSLenS. The cross-correlation signal is consistent with zero that shows that any possible leakage of the systematic  $B$ -mode residuals to  $E$ -mode does not correlate with the true  $E$ -mode signal.

## B2 Residual tSZ–lensing systematic correlation

In the following, we demonstrate that while there is significant  $B$ -mode signal in the RCSLenS data, the lensing–tSZ cross-correlation signal is not contaminated. This serves as a good example of how cross-correlating different probes can suppress significant systematic residuals and make it useful for further studies.

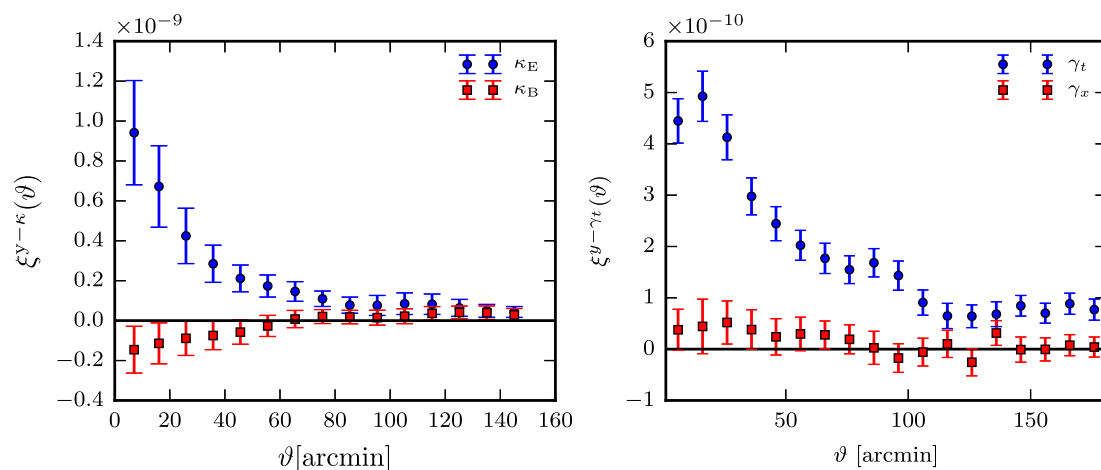
As the first step, we cross-correlate the  $y$  maps with the random noise maps constructed for each RCSLenS field. We computed the mean cross-correlation and the error on the mean from these random noise maps. Consistency with zero insures that there is not any unexpected correlation between the  $y$  signal in the absence of a true lensing signal and insures that the field masks do not create any artefacts.

As the next step, we correlate the  $y$  maps with the constructed  $\kappa_B$  maps. This cross-correlation should also be consistent with zero to ensure that there is no unexpected correlation between the tSZ signal and the systematic lensing  $B$ -mode. Note that we can perform a similar consistency check using the shear data instead. The analogue to the  $\kappa_B$  mode for shear is the cross (or radial) shear quantity,  $\gamma_{\times}$ , defined as

$$\gamma_{\times}(\theta) = -\gamma_1 \cos(2\phi) + \gamma_2 \sin(2\phi), \quad (\text{B2})$$

which can be constructed by  $45^\circ$  rotation of galaxy orientation in the shear catalogue. With this estimator, we expect the  $y$ – $\gamma_{\times}$  cross-correlations to be consistent with zero as another check of systematics in our measurements.

Fig. B2 summarizes the null tests described above. In the left-hand panel, cross-correlations of  $y$  with reconstructed  $\kappa_B$  maps are



**Figure B2.** A summary of the null tests performed on the  $y$ – $\kappa$  (left) and  $y$ – $\gamma_t$  (right) estimators. The red squares show the  $B$ -mode  $\kappa$  (right) and  $\gamma_{\times}$  cross-correlations that are consistent with zero as expected [The blue circles show the  $E$ -mode  $\kappa$  (right) and  $\gamma_t$  cross-correlations for comparison.] The null tests are validated in all cases confirming that the level of contaminating systematics is under control in the cross-correlation analysis.

shown with the  $y\text{-}\kappa_E$  curve overplotted for comparison. Correlation with  $\kappa_B$  maps slightly deviates from zero at smaller scales due to residual systematics but is still insignificant considering the high level of bin-to-bin correlation. In the right-hand panel, we show cross-correlation with  $\gamma_\times$  with the  $y\text{-}\gamma_t$  curve overplotted for comparison. We do not see any inconsistency in the  $y\text{-}\gamma_\times$  correlation.

Both estimators are also perfectly consistent with zero when cross-correlated with random maps.

We therefore conclude that the systematic residuals are well under control and do not affect our measurements.

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