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Davies, B and Beasor, ER (2020) The 'red supergiant problem': the upper luminosity boundary of Type II supernova progenitors. Monthly Notices of the Royal Astronomical Society, 493 (1). pp. 468-476. ISSN 0035-8711

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Advance Access publication 2020 January 20

The 'red supergiant problem': the upper luminosity boundary of Type II supernova progenitors

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Accepted 2020 January 16. Received 2020 January 16; in original form 2019 August 2

ABSTRACT

By comparing the properties of red supergiant (RSG) supernova (SN) progenitors to those of field RSGs, it has been claimed that there is an absence of progenitors with luminosities Labove $\log (L/L_{\odot}) > 5.2$. This is in tension with the empirical upper luminosity limit of RSGs at log (L/L_{\odot}) = 5.5, a result known as the 'RSG problem'. This has been interpreted as an evidence for an upper mass threshold for the formation of black holes. In this paper, we compare the observed luminosities of RSG SN progenitors with the observed RSG L-distribution in the Magellanic Clouds. Our results indicate that the absence of bright SN II-P/L progenitors in this sample can be explained at least in part by the steepness of the L-distribution and a small sample size, and that the statistical significance of the RSG problem is between 1σ and 2σ . Secondly, we model the luminosity distribution of II-P/L progenitors as a simple power law with an upper and lower cut-off, and find an upper luminosity limit of $\log(L_{\rm hi}/L_{\odot}) = 5.20^{+0.17}_{-0.11}$ (68 per cent confidence), though this increases to \sim 5.3 if one fixes the power-law slope to be that expected from theoretical arguments. Again, the results point to the significance of the RSG problem being within $\sim 2\sigma$. Under the assumption that all progenitors are the result of single-star evolution, this corresponds to an upper mass limit for the parent distribution of $M_{\rm hi} = 19.2 \,\mathrm{M}_{\odot}, \pm 1.3 \,\mathrm{M}_{\odot}$ (systematic), $^{+4.5}_{-2.3} \,\mathrm{M}_{\odot}$ (random; 68 per cent confidence limits).

Key words: stars: evolution - stars: massive - supergiants.

1 INTRODUCTION

Linking supernovae (SNe) to their progenitor stars is a powerful test of stellar evolutionary theory. The first SN for which this was possible, SN1987A, famously threw up the surprise of a blue progenitor (Gilmozzi et al. 1987; Sonneborn, Altner & Kirshner 1987; Walborn et al. 1987), whereas theory at the time predicted that such a star would explode as a red supergiant (RSG). Since then, it has been realized that SN1987A-like events are relatively rare, that SN1987A's progenitor likely had a complicated evolutionary history (e.g. Podsiadlowski 1992), and in fact the most common H-rich SNe (classified as either II-P or II-L) do indeed have red progenitors (Smartt et al. 2009).

Beyond simply predicting the correct colour, one can also look at the luminosity distribution of II-P/L progenitors and test theoretical predictions by comparing to the expectations from population synthesis. Exclusively until now, such comparisons have involved converting the pre-explosion luminosities L_{fin} into initial masses M_{init} using stellar models, then comparing the inferred M_{init} distribution to a Salpeter initial mass function (IMF) with an upper and lower mass cut-off (Smartt et al. 2009; Smartt 2015; Davies & Beasor 2018). In the first study of this kind, Smartt et al. (2009, hereafter S09) determined an upper mass cut-off for the progenitors of SNe II-P of $M_{\text{max}} = 16 \,\text{M}_{\odot}$. Since evolutionary models at the time had stars with initial masses of up to $30 \, M_{\odot}$ dying as RSGs, this tension – and the fate of stars with $M_{\rm init}$ between 16 and 30 ${
m M}_{\odot}$ - was termed the 'RSG problem'. The result has received a great deal of attention in the literature, due at least in part to the fact that this possible upper mass cut-off resonates with contemporaneous numerical work. Specifically, several independent authors have found that the likelihood of forming a black hole at core collapse increases dramatically above masses of 16–20 M_{\odot} (O'Connor & Ott 2011; Horiuchi et al. 2014; Ertl et al. 2016; Müller et al. 2016; Sukhbold, Woosley & Heger 2018), due to the transition from convective to radiative core carbon burning near the end of the star's life (Sukhbold & Adams 2019).

After the initial study by S09, a larger sample of progenitors was used by Smartt (2015, hereafter S15) to revise the value of M_{max} upwards to 17 M_{\odot}. Further, Davies & Beasor (2018, hereafter DB18) later revisited the complexities of converting a pre-explosion brightness to bolometric luminosity L_{fin} , and the conversion of L_{fin} to M_{init} , as well as other sources of systematic errors, and argued that

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 M_{max} was 21 M_{\odot} once systematic errors had been taken into account, but with a 1 σ upper error bar that extended up to 30 M_{\odot}. The conclusion of DB18 was therefore that the evidence for a population of 'missing' stars had only a minor statistical significance.

The studies of the RSG problem mentioned above (S09, S15, DB18) tended to work in the mass plane; that is, they infer initial masses for the progenitors, then compare these masses to the expectation of a stellar IMF and a constant star formation rate. The RSG problem itself describes the tension between the inferred value of $M_{\rm max}$ (16–21 M_{\odot}) and its expectation value, commonly quoted as being $30\,M_{\odot}$. Before continuing, it is worth emphasizing that this expected value of M_{max} is not a theoretical prediction; rather, it is the observed maximum luminosity of RSGs L_{max} , also known as the Humphreys-Davidson Limit (H-D limit; Humphreys & Davidson 1979), converted to an initial mass. The first measurements of the H–D limit placed it at log $(L_{max}/L_{\odot}) = 5.8$. This has subsequently been revised downwards to $\log (L_{\text{max}}/L_{\odot}) = 5.5$ in the Magellanic Clouds (Davies, Crowther & Beasor 2018, hereafter DCB18); and, as we will show in this paper, L_{max} appears to be the same in the Milky Way. The value of M_{max} is then simply the initial mass of the evolutionary track that terminates in the RSG phase with $L = L_{\text{max}}$. According to the STARS evolutionary tracks used in S09, this corresponds to an initial mass of $27 \, M_{\odot}$, which is the basis for the expectation value of $\sim 30 \, \text{M}_{\odot}$ quoted in reference to the RSG problem.

Alternative techniques to study progenitor masses to SN IIP have been explored, but do not yet provide any additional reliable information. SN light curves have been modelled by several authors (e.g. Bersten, Benvenuto & Hamuy 2011; Utrobin & Chugai 2017; Morozova, Piro & Valenti 2018), the shape and duration of that should yield information on the ejecta mass, which in turn should be related to the stellar initial mass. However, it has been shown that large degeneracies exist in the model parameter space that are difficult to break (Dessart & Hillier 2019; Goldberg, Bildsten & Paxton 2019). The progenitor's surface abundances, as studied from spectroscopy of the SNe at very early times, can also provide evidence as to the progenitor mass (Davies & Dessart 2019), but this work has yet to be empirically road tested. Finally, one may measure the mass of oxygen in the SN ejecta, which again should be a function of the progenitor mass (Jerkstrand et al. 2014; Valenti et al. 2016). However, when exploited on SNe that also have preexplosion imaging mass estimates, there is no apparent correlation between the two independent measurements, implying that either one or both are flawed (DB18).

When attempting to infer the properties of the progenitor distribution, working in the mass plane (i.e. beginning by converting $L_{\rm fin}$ to $M_{\rm init}$ via stellar models) serves to add in an extra layer of model dependence, and hence uncertainty, into the results. Furthermore, the use of a single set of evolutionary tracks neglects the complexity of 'real' stellar evolution. For example, stars have a broad distribution of rotation rates (Ramírez-Agudelo et al. 2013); they are often in multiples (Sana et al. 2012), and so experience loss/gain of mass and/or angular momentum (e.g. Eldridge, Izzard & Tout 2008); and stellar models still rely on highly uncertain input physics such as mass-loss rates, convective mixing/overshooting (Jones et al. 2015), plus any other form of 'weather' that prevents two stars with similar bulk properties from following the exact same evolutionary path. All of these complicating factors are naturally accounted for by employing an empirical L-distribution with which to compare the observed luminosities of the SN progenitors.

In S09, the sample of SN progenitors consisted of 20 events, with seven detections (the rest being upper limits). Of these seven

detections, the most luminous was found to be SN1999ev with $\log (L/L_{\odot}) = 5.1 \pm 0.2$.¹ The absence of progenitors within the range 5.1 < $\log (L_{I}L_{\odot}) < 5.5$, corresponding a mass range of 16–30 M_{\odot} according to the STARS models in S09, was the basis for the original claim for 'missing' progenitors. In the subsequent papers S15 and DB18, this sample size of detections grew to 14, the most luminous of which was SN2009hd with $\log (L/L_{\odot}) = 5.24 \pm 0.08$. In the following section, we will argue that much of this tension be explained as being a consequence of a small sample. Later, in Section 3 will also look at the *L*-distribution of Type-II progenitors to estimate the upper *L* cut-off, which can be directly compared to the predictions from stellar evolution. Our findings are summarized in Section 4.

2 A RE-EVALUATION OF THE 'MISSING' RSG PROGENITORS

2.1 The input sample

Our sample of II-P and II-L progenitors comes from that of DB18, which itself was based on that in S15 but with the inclusion of SN2008cn. To this sample, we have added the following more recent events:

(i) SN2017eaw: The progenitor for this SN was studied in Kilpatrick & Foley (2018) and Van Dyk et al. (2019), and was detected by Hubble Space Telescope (HST) in several bands. Both studies estimated foreground extinctions of $A_V = 1.0 \pm 0.1$, based on the strengths of the diffuse interstellar bands. Also, both attempted to obtain bolometric luminosities by modelling the spectral energy distribution (SED), though both relied upon MARCS model atmospheres that are known to struggle to fit the optical and infrared spectra simultaneously (Davies et al. 2013), and did not have enough photometry in the mid-IR to constrain the emission from circumstellar dust. As an alternative estimate of L_{bol} , we take the F160W photometry, which is closest to the intrinsic peak of the SED and is less affected by extinction, and apply a bolometric correction typical of late-type RSGs (see DB18). Though bolometric corrections (BCs) in the H band were not discussed in DB18, analysis of the same data set reveals that all RSGs in that study's sample have $BC_{F160W} = 2.6 \pm 0.1$ irrespective of spectral type. The nature of the DB18 study is such that this BC includes the effect of circumstellar extinction and mid-IR excess. Using the pre-explosion brightness of $m_{\rm F160W} = 19.36 \pm 0.01$ and a distance to the host galaxy of NGC 6946 of 7.72 ± 0.32 Mpc (see discussion in Van Dyk et al. 2019), we find a terminal luminosity of $\log L/L_{\odot} = 4.96 \pm 0.11$. This is in very good agreement with the Kilpatrick & Foley (2018) and Van Dyk et al. (2019) studies.

(ii) SN2018aoq: The detection of this SN's progenitor was presented in O'Neill et al. (2019). There were detections in the *V*, *I*, and *H* bands with *HST*. The foreground reddening was determined from comparisons to of the light curve to other similar SNe, finding a value of $E(B - V) = 0.03 \pm 0.01$. Following our methodology for SN2017eaw, using a pre-explosion brightness of $m_{F160W} = 21.89 \pm 0.02$ and a distance of 18.2 ± 1.2 kpc, we find a terminal luminosity of log L/L_{\odot} = 4.63 ± 0.12, which is somewhat lower than that of O'Neill et al.

¹The nature of the progenitor of SN1999ev, as well as others in the S09 sample, is now considered highly uncertain due to its apparent location in a star cluster (Maund, Reilly & Mattila 2014). The brightest progenitor in S09, as re-derived by DB18, is SN2006my with $\log (L_{l}L_{\odot}) = 4.97 \pm 0.18$.

In addition, we have used the revised distance to NGC 6946, measured from the tip of the red giant branch (7.72 ± 0.32 Mpc; see Van Dyk et al. 2019), for SN2002hh, SN2004et as well as SN2017eaw. We have not included the event SN2016cok (\equiv ASSASN-16fq), owing to the outstanding uncertainty over the progenitor (Kochanek et al. 2017).

The main criteria for inclusion in the sample is that it must be of type II, be located in a galaxy with pre-explosion imaging, be near enough for the progenitor to be resolved (a distance limit of \sim 30 Mpc), and have either a progenitor detection or a meaningful upper limit. The sample likely has a bias towards higher metallicities (SMC-like or higher) since it is the more massive Local Group galaxies that have the more extensive archival imaging. Finally, there is potential bias in our sample of *detections* against objects with high line-of-sight reddening. Specifically, in the case of a non-detection, we may potentially underestimate the upper limit to the progenitor's luminosity if the object is obscured. In the case of obscuration by circumstellar extinction, in DB18 we attempted to correct for this bias by adopting empirical bolometric corrections based on observations of reddened late M-type supergiants. However, this does not account for extra extinction intrinsic to the host galaxy. Jencson et al. (2017) have argued that there may be a hidden population of nearby core-collapse SNe that are hidden by large amounts of extinction intrinsic to the host galaxy, and that these objects may account for 10-20 per cent of the local SN rate. It remains to be see if these 'hidden' SNe have progenitors different to those discovered in the optical.

2.2 An empirical L-distribution of RSGs

As our basis for comparison, we take the L-distribution of RSGs, defined as those with spectral types of K0 or later (K0 +) in the Large Magellanic Cloud (LMC) as measured by DCB18. By studying the LMC rather than the Milky Way, we avoid issues such as uncertain distances and high interstellar reddening that can fatally affect the sample completeness. The LMC L-distribution in DCB18 was determined by searching, cross-matching, and combining various multiwavelength catalogues. By studying sources in the optical though mid-infrared, the authors were able to detect any sources with high circumstellar extinction that would previously have been missed in optical-only searches. Bolometric luminosities were determined by integrating under the observed SED, thus removing any dependence on uncertain bolometric corrections. The implicit assumption made was that any flux lost in the optical due to circumstellar extinction was re-radiated in the mid-IR. We found only one object where this assumption seemed to have been invalid (WOH G64), where a more detailed study of the SED by Ohnaka et al. (2008) revealed a lower luminosity. Here, we have replaced the luminosity listed by DCB18 for this star by that determined by Ohnaka et al. With this data point corrected, the luminosity cut-off at $\log (L_{\text{max}}/L_{\odot}) = 5.5$ is clear (see fig. 2 in DCB18). Furthermore, population synthesis analysis in DCB18 has shown that any RSGs above this limit (as predicted by theory) are unlikely to have been missed.

The majority of the SNe in the sample have metallicities between $12 + \log (O/H) = 8.3-8.9$, or LMC-like to slightly super-Solar (S09). Though we do not have a statistically complete *L*-distribution for the Galaxy, we will argue in Section 2.5 that there is no evidence for the HDL L_{max} being brighter in the Galaxy than in the LMC. The benefit of using an empirical *L*-distribution, as opposed to a theoretical one, is that we automatically bypass the uncertainties in stellar evolution, some of which (contribution of post-binary interaction objects, initial rotation rate distribution, magnetic fields)



Figure 1. The *L*-distribution of II-P progenitors is shown as the grey-filled histogram. Overplotted are the observed luminosity distributions of all RSGs (blue), all M supergiants (green), and all supergiants with spectral type M3 or later (red) in the Large Magellanic Cloud (LMC). Each LMC *L*-distribution has been rescaled to give the same number of objects with log ($L_{l}L_{\odot}$) > 4.8 as the SN progenitors.

are almost intractable. For example, the relation between initial mass and terminal luminosity has been shown to have a great deal of dispersion once binarity is taken into account (Zapartas et al., in prep).

In Fig. 1, we plot the luminosity function of all cool supergiants in the LMC from DCB18. It is important to note that our empirical sample of RSGs contains stars at *all stages* of RSG evolution, whereas the SN progenitors are exclusively RSGs at the very end of the phase. In DB18, we argued that these late-evolution RSGs tend to have later spectral types (M3 or later), based on two forms of evidence. First, in star clusters with large numbers of RSGs, we see the more evolved stars having later spectral types. Secondly, SNe with multicolour pre-explosion photometry invariably show that the progenitor was very red, consistent with having a spectral type of M3 or later (e.g. SN2003gd, SN2004et). Therefore, in an attempt to isolate the LMC RSGs that are closest to SN, we have made cuts on spectral type of M0 or later (which we call M0+) and M3 or later (M3 +).

In Fig. 1, we overplot the L-distributions of the master sample of RSGs in the LMC, as well as the two subsamples. Each histogram has been normalized to reproduce the total number of objects as the II-P progenitors within the range $4.8 < \log (L/L_{\odot}) < 5.6$, below which the LMC RSG sample is likely incomplete (DCB18). No matter how we slice the sample, in all cases we see a definite cut-off at $\log(L_{\text{max}}/L_{\odot}) \simeq 5.5$. In the total (K0+) sample and the M0+ subsample, we see overall luminosity distributions that are very similar in shape, and which match the observed II-P distribution rather well. In the late-type subsample (M3+), we see the distribution roll-over to smaller numbers below a brightness of $\log (L/L_{\odot}) \simeq 4.9$. This is likely an effect of incompleteness – fainter, redder objects are more likely to be missing from the DCB18 sample - though it could also be explained as being caused by fainter (i.e. lower initial mass) RSGs spending less time at later spectral types as a fraction of their overall RSG lifetime. The consequences of these two possible explanations for our conclusions are discussed in the next section.

2.3 The brightest expected supernova progenitor

Under the assumption that the *L*-distribution of late-M supergiants shown in the previous section (labelled M3 +) effectively describes



Figure 2. The expected luminosity of the brightest supernova progenitor for a range of sample sizes. The larger the sample, the higher the probability that the brightest progenitor has a luminosity close to the intrinsic L_{max} (shown by the blue-dashed line). The shaded blue regions indicate the confidence limits on L_{max} as indicated in the legend. The data points show the observed evolution of $L_{\text{max,prog}}$ as the sample size has increased over time.

that of II-P/L SN progenitors, the probability of a given SN progenitor having a luminosity L can be found simply by randomly sampling this L-distribution. Obviously, the IMF combined with the shorter lifetime of more massive stars dictate that one is more likely to find a faint progenitor than a bright one, and the probability of finding a bright progenitor increases with increasing sample size. That is, the larger the sample size, the brighter we expect the luminosity of our brightest SN progenitor $L_{\text{max,prog}}$ to be. The L-distribution in Fig. 1 allows us to quantify this.

We determine the probability distribution function (PDF) of $L_{\text{max,prog}}$ for a sample size N by performing a simple Monte Carlo (MC) experiment. We first randomly sample the luminosities of N M-supergiants in the LMC with spectral types M3 or later, where each star's luminosity is itself sampled randomly from a Gaussian distribution with a standard deviation equal to the star's 1 σ error. In each trial, we determine the brightest of the N progenitors, which we set as $L_{\text{max,prog}}$ for that trial. We then repeat 10⁴ times for each value of N to determine the PDF of $L_{\text{max,prog}}$ at that N. We perform this same experiment for a range of sample sizes.

The results of this experiment are shown as the shaded region in Fig. 2, where the different colours indicate the confidence limits in the legend. As expected, the plot demonstrates that the smaller the sample size, the fainter the $L_{\text{max,prog}}$ one expects to observe. Specifically, at sample sizes below 10 one expects to find $\log (L_{\text{max,prog}}/L_{\odot}) \simeq 5.2$, but with a large dispersion. At sample sizes greater than 80, the absence of a progenitor brighter than $\log (L_{\text{max,prog}}/L_{\odot}) \simeq 5.25$ starts to become significant at the 3σ level.

In order to compare how the observed $L_{\text{max,prog}}$ has evolved as sample size has grown, in Fig. 2 we overplot the brightest SN progenitor as a function of the sample size at the time that SN was observed. For small sample sizes (<10), the disagreement with the expectation appears to be significant. However, as the sample size grows, the observed trend (the black squares) starts to follow the results of our MC experiment more closely. Presently, the discrepancy between the luminosity of the brightest SN progenitor to date (SN2009hd) and the observed H–D limit has a significance of 1σ – 2σ . However, this does not take into account the error on SN2009hd, which had a luminosity of log (L/L_{\odot}) = 5.24 ± 0.08, or indeed that of SN2009kr (log (L/L_{\odot}) = 5.13 ± 0.23), which was less than 2σ from the H–D limit at log (L/L_{\odot}) = 5.5.

In the previous section, we noted that the luminosity distribution of the M3+ RSGs is different to that of the total RSG sample. We also offered two explanations for this – one physical, that it is caused by relatively shorter durations of the M3+ phase for lower mass RSGs; and one systematic, that it is caused by greater statistical incompleteness at lower luminosities for the M3+ subsample. If the latter explanation is correct, it would introduce a bias into our results. Specifically, by randomly sampling from a population that had too few faint objects, we would artificially increase the likelihood of selecting a bright progenitor in each MC trial. Correcting for this bias, should it exist, would effectively pull the blue shaded region in Fig. 2 down to lower luminosities, decreasing further the statistical significance of the RSG problem.

2.4 Comparisons to previous work

Our result that the statistical significance of the 'RSG problem' is below 2σ seems to contradict the conclusions of S09 and S15. These authors estimated the significance of the 'missing' RSGs to be in the region of 4σ , based on their sample size and the lack of objects with luminosities between L_{max} and that of their brightest progenitor L_{hi} . However, we note that S09/S15 did not seem to account for the uncertainties on the luminosities of the progenitors when determining this (see previous section).

We can see from Fig. 2 that when the sample size was only ~10, as it was in S09, there was the appearance that the result was significant. However, this was before the events with brighter progenitors (SN2008cn, SN2009kr, and SN2009hd). Though SN2009kr and SN2009hd were included in S15, both had their luminosities revised upwards by DB18, who tuned up the assumptions about the bolometric corrections and foreground extinctions. Indeed, in DB18 we argued that the significance of the 'missing' stars was lower than claimed in S09 and S15, due to the additional uncertainties in the theoretical $M_{init}-L_{fin}$ relation, plus the small sample size. Therefore, the conclusions of this part of our current study are consistent with those of DB18.

2.5 Is the L-distribution of RSGs different in the Milky Way?

The most obvious criticism one might make of this work is that we employ an empirical *L*-distribution measured in the LMC, whereas many of the SNe in the current sample occurred in galaxies where the metallicity is thought to be closer to Solar (S09). A statistically complete sample of RSGs in the Milky Way does not exist at the time of writing. The construction of such a sample would be extremely difficult, as it would have to overcome the obstacles of high foreground extinction beyond distances of ~3kpc, contamination by foreground red giants, and AGB stars, as well as uncertain distances. However, we *can* investigate one key feature of the Galactic RSG *L*-distribution; specifically the brightness of the H–D limit L_{max} .

In S09, the expectation value of L_{max} was determined by comparing to the brightest known Galactic RSGs in Levesque et al. (2005). These bright RSGs were some of the more famous members of the class, such as VY CMa and μ Cep. The luminosities of these stars were determined by Levesque et al. by two methods; the extrapolation of model fits to the optical SED, and from bolometrically corrected *K*-band brightnesses. Distances were inferred by assuming that the RSGs were physically associated with the nearest OB association, and adopting the appropriate distance from the literature. Here, we now re-appraise the luminosities of the brightest of these RSGs. To do this, we first re-evaluate their distances and foreground extinctions, then determine their bolometric luminosities by integrating under their observed SEDs from the optical to the mid-infrared.

2.5.1 Distances and reddenings

To determine distances to the Galactic RSGs, we employ parallax measurements. Optical parallaxes of RSGs, such as those measured by Gaia (Gaia Collaboration 2018), are extremely problematic due to the stars' inhomogeneous surfaces and the fact that their sizes are often comparable to the baseline for the parallax measurement (i.e. the size of the Earth's orbit around the Sun; see e.g. Chiavassa et al. 2011). Fortunately, there are other ways to determine RSG distances from parallaxes. First, one may employ radio parallax measurements of circumstellar masers. Secondly, one may take the average parallax of the neighbouring OB stars, under the assumption that the RSG is a part of the same association (see also Humphreys 1978; Levesque et al. 2005). Where possible, we employ both methods here to verify the accuracy of the results.

To measure reddenings, we can again look at the neighbouring OB stars, and use the colour excess to estimate the average lineof-sight extinction to the RSGs. Though there may well be extra extinction to each RSG due to circumstellar material, we can still obtain a bolometric luminosity by integrating the full SED under the assumption that any flux lost at short wavelengths is re-radiated in the infrared (see also DCB18).

For each RSG in our sample, we search the SIMBAD data base for OB stars with known spectral types within 30 arcmin of the star. Where there are a large number of OB stars, we take the nearest 50. From spectral types of the OB stars, we obtain the intrinsic B - Vcolours from Martins & Plez (2006) and Fitzgerald (1970), and use the observed colours to determine E(B - V) for each OB star. We then take the sigma-clipped mean of these reddenings, clipping at 2σ .

The parallax measurements for the OB stars were obtained from *Gaia* DR2 (Gaia Collaboration 2018). We again performed sigmaclipping with a threshold of 2σ , then took the sigma-weighted mean of the remaining stars. This mean parallax was converted to a distance following the procedure described in Davies & Beasor (2019). The comparisons of these 'OB star' distances to those obtained from maser parallaxes are illustrated in Fig. 3. The data points all follow the 1:1 line, implying that both methods are consistent with one another. Formally, analysis of the residuals reveals a mean offset of 150 ± 240 pc. The standard deviation on the offset likely represents the absolute precision on the OB star method since the OB associations and complexes that host the RSGs could easily be of order ~100pc.

2.5.2 Luminosities

Bolometric luminosities are determined by first collating broadband photometry for each RSG spanning the optical to mid-infrared. The brightnesses of these stars makes this a non-trivial task, since many are often saturated in contemporary surveys. We took optical photometry from *Gaia* DR2 (Gaia Collaboration 2018), SDSS-IV DR15 *i* band (Aguado et al. 2019; Morel & Magnenat 1978), near-IR photometry from 2MASS (Skrutskie et al. 2006; Morel & Magnenat 1978), and mid-IR photometry from IRAS and MSX (Helou & Walker 1988; Price et al. 2001). Having several survey



Figure 3. Comparison between the distances obtained from maser parallaxes (*x*-axis) and those from the *Gaia* DR2 parallaxes of neighbouring OB stars (*y*-axis). The dotted line shows the 1:1 correlation.

sources overlapping in wavelength permits the identification and rejection of spurious photometric points, due to, e.g. saturation. For each star, the good photometric data are dereddened and interpolated in the log (Flux) and log (λ) plane, then integrated to find the bolometric luminosity. Flux shortwards of *B* is assumed to contribute a negligible amount to the bolometric flux (see also DCB18).

2.5.3 Results

Our revised distances, reddenings, and bolometric luminosities of the bright Galactic RSGs are listed in Table 1. From the last column, it can be seen that no star has a luminosity greater than log $(L/L_{\odot}) = 5.5$. In terms of how these values compare to previous estimates, all are roughly consistent with the bolometrically corrected *K*-band estimates of Levesque et al. (2005). Any differences with the values listed in Mauron & Josselin (2011), who like us obtained L_{bol} by integrating under the SED, can be attributed to changes in distance and foreground reddening. The most notable change is for the star EV Car, which in Mauron & Josselin (2011) had a distance of 4.2kpc. We investigated all known OB stars with spectral types earlier than B3 in the whole Carina star-forming region, spanning 10° in Galactic longitude, and consistently found distances between 2.4–3.0 kpc.

Though we list only 12 stars in Table 1, we emphasize that these have been previously identified as the brightest optically identified RSGs in Levesque et al. (2005) and Mauron & Josselin (2011). The objects in Table 1 are therefore only a subset of optically identified Milky Way RSGs. The full sample studied by Levesque et al. (2005) contained over 80 stars, which was by no means complete. A search of SIMBAD reveals that there are over 100 stars in the Galaxy with optically identified spectral types later than K0 and luminosity classes Ib or brighter. With a sample size this large, one can expect the brightest observed RSG to be sampling close to L_{max} (cf. Fig. 2). We therefore consider the lack of any known RSGs in the Milky Way with luminosities above log (L/L_{\odot}) = 5.5 evidence that the H–

Star	RA	Dec.	D/kpc	D method	E(B - V)	$\log{(L/L_{\odot})}$
S Per	02 22 51.7	+ 58 35 11.5	$2.42^{+0.11}_{-0.09}$	Maser	$0.69^{+0.16}_{-0.51}$	$5.09^{+0.08}_{-0.15}$
VY CMa	07 22 58.3	-25 46 03.2	$1.20\substack{+0.13\\-0.10}$	Maser	$0.06\substack{+0.05\\-0.05}$	$5.25\substack{+0.09\\-0.08}$
CK Car	10 24 25.4	-60 11 29.0	$2.92^{+0.19}_{-0.15}$	OB	$0.30_{-0.18}^{+0.15}$	$5.20\substack{+0.10\\-0.10}$
RT Car	10 44 47.1	-59 24 48.1	$2.38^{+0.18}_{-0.15}$	Maser	$0.53_{-0.12}^{+0.12}$	$5.11_{-0.09}^{+0.10}$
EV Car	10 20 21.6	-60 27 15.8	$2.96^{+0.22}_{-0.20}$	OB	$0.40_{-0.29}^{+0.12}$	$5.46_{-0.14}^{+0.10}$
VX Sgr	18 08 04.0	-22 13 26.6	$1.56\substack{+0.11\\-0.10}$	Maser	$0.26_{-0.19}^{+0.40}$	$5.44_{-0.09}^{+0.15}$
BC Cyg	20 21 38.5	+ 37 31 58.9	$1.71\substack{+0.04\\-0.04}$	OB	$0.80\substack{+0.80\\-0.60}$	$5.31_{-0.14}^{+0.25}$
RW Cyg	20 28 50.6	+ 39 58 54.4	$1.62^{+0.04}_{-0.04}$	OB	$0.70_{-0.50}^{+0.40}$	$5.10\substack{+0.16 \\ -0.17}$
NML Cyg	20 46 25.5	+40.0659.4	$1.61^{+0.13}_{-0.11}$	Maser	$0.50^{+0.25}_{-0.25}$	$5.36\substack{+0.07\\-0.07}$
μ Cep	21 43 30.5	+ 58 46 48.2	$0.94^{+0.14}_{-0.04}$	OB	$0.46^{+0.09}_{-0.09}$	$5.43_{-0.07}^{+0.15}$
MY Cep	22 54 31.7	+ 60 49 39.0	$3.00^{+0.35}_{-0.29}$	OB	2.04 ± 0.07	$5.11\substack{+0.08\\-0.07}$
PZ Cas	23 44 03.3	+ 61 47 22.2	$2.81\substack{+0.22 \\ -0.19}$	Maser	$0.51\substack{+0.40 \\ -0.11}$	$5.36\substack{+0.19 \\ -0.09}$

Table 1. Observed properties of luminous Milky Way RSGs.

D limit at Solar metallicity is similar to that found in the Magellanic Clouds.

3 A RE-ANALYSIS OF THE *L*-DISTRIBUTION OF II-P/L PROGENITORS, AND THE UPPER CUT-OFF IN LUMINOSITY AND MASS

In the previous section, we discussed the statistical significance of the 'missing' RSG progenitors by comparing the luminosities of the brightest II-P progenitors with that of the RSG luminosity limit L_{max} . However, we may learn more about the properties of II-P progenitors by studying the observed progenitor sample as a whole. In this section, we analyse the observed luminosity distribution of II-P/L progenitors to evaluate the properties of the parent population. In particular, the aim is to provide the most robust measurement to date of the upper luminosity boundary L_{hi} . This in turn can be used to infer the upper mass boundary M_{hi} , allowing us to clearly separate the random errors caused by the finite sample size from the systematic errors introduced by the theoretical mass–luminosity relation.

To date, analysis of the underlying population of II-P/L progenitors has focused on the inferred masses, fitting an analytical function based on the IMF and upper/lower mass limits (S09, S15, DB18). There are two problems with this analysis, discussed earlier in this work as well as in DB18. First, it implicitly assumes that the highest mass progenitor in the sample will have a mass close to $M_{\rm hi}$, which in a finite sample causes one to underestimate $M_{\rm hi}$. Secondly, converting luminosities to masses injects all model errors and uncertainties into the analysis (see discussion in Section 1).

Here, to circumvent these problems, we present a new analysis method. First, we study the luminosity distribution, rather than the mass distribution. Secondly, we employ an MC method to randomly sample from a master population, which simulates the effects of a finite and small sample, which we now describe in more detail.

3.1 The observed cumulative luminosity distribution of SN progenitors

The first step is to create a proper description of the progenitor cumulative luminosity distribution (CLD) for our N SN progenitors. Simply plotting the observed progenitors in order of increasing luminosity (such as in fig. 6 in S15 or fig. 5 in DB18) does not take into account that the errors on L also affect the ranking. That is,



Figure 4. The cumulative luminosity distribution (CLD) of SN progenitors. The individual observations, sorted in order of increasing L, are shown in yellow. The shaded contours show the confidence limits of the underlying CLD, as determined by the Monte Carlo experiment described in the text.

perturbing the L of a progenitor to a higher value would also cause that progenitor to be higher in the ranking, and vice-versa.

We obtain a probability density distribution of the CLD by performing a simple MC procedure. In each MC trial, we randomly sample from the probability distribution of each progenitor's preexplosion brightness, distance, extinction, and bolometric correction to determine that progenitor's luminosity, then order the progenitor's luminosity $P_n(L)$ is determined from the luminosities of 30 000 MC trials. Note that *n* does *not* correspond to an individual progenitor, but is the most likely *n*th brightest out of *N* progenitors given the observational errors on all objects in the sample.

The progenitor CLD is shown as the filled contours in Fig. 4. Also, shown on the this plot are the progenitor measurements in order of increasing L, to demonstrate the subtle differences between the two. Specifically, the CLD is narrower in the mid-range than the individual errors on the data points, but extends to lower/higher L at the bottom/top, respectively.

3.2 A grid of model cumulative luminosity distributions

Next, we construct a model grid of CLDs to compare to the observed CLD. The CLD is modelled as a simple power law, and therefore has three input parameters: the lower and upper luminosity cut-offs L_{lo} and L_{hi} , and the power-law exponent Γ_L . At a given set of $\{L_{lo}, L_{hi}, \Gamma_L\}$, we again determine the CLD using MC. We randomly sample N luminosities from the distribution, and add on random noise according to the error bars of the observed L distribution. For example, for the faintest progenitor in our simulated sample, we apply the same random error as for the faintest observed progenitor. We again repeat over 30 000 MC trials to determine the posterior probability distribution for the *n*th brightest progenitor out of N objects.

3.3 Finding the best-fitting model

At each point in the grid, we evaluate the best-fitting model via a maximum-likelihood analysis. The probability P(n) that a model with parameters { L_{lo} , L_{hi} , Γ_L } reproduces the luminosity L of the *n*th progenitor is

$$P(n) = \sum_{L} \left(P_{\text{obs},n}(L) \times P_{\text{mod},n}(L) \right), \tag{1}$$

where $P_{\text{obs},n}$ is the observed probability density as a function of luminosity for the *n*th progenitor (i.e. a horizontal row in Fig. 4), and $P_{\text{mod},n}$ is the same but for the model. The likelihood \mathcal{L} that model $\{L_{\text{lo}}, L_{\text{hi}}, \Gamma_L\}$ fits the observed CLD is then

$$\ln \mathcal{L} = \sum_{n} \ln P(n). \tag{2}$$

To compare the quality of fits of neighbouring models, the likelihoods are converted to χ^2 values via, $\chi^2 = -2 \ln \mathcal{L}$. The bestfitting model is defined to be that with the lowest χ^2 value, while the models within the 68 per cent, 95 per cent, and 99.7 per cent confidence limits are those χ^2 values within 3.53, 8.02, and 14.16 of the minimum,² respectively.

3.4 Results and discussion

The probability distributions of each model parameter are illustrated in Fig. 5, while the best-fitting model CLD is shown in Fig. 6. The best-fitting model parameters, when all are allowed to be free, are

$$\log(L_{\rm lo}/{\rm L}_{\odot}) = 4.39^{+0.10}_{-0.16},$$

$$\log(L_{\rm hi}/{\rm L}_{\odot}) = 5.20^{+0.17}_{-0.11},$$

$$\Gamma_{\rm L} = -1.12^{+0.95}_{-0.81}$$

where the quoted errors are the 68 per cent confidence limits. The optimized value of $L_{\rm hi}$ is somewhat below the H–D limit (consistent with the 'RSG problem'), however, the upper error bar stretches to quite high luminosities. Specifically, the tension with the observed H–D limit at log (L/L_{\odot}) = 5.5 is within the 95 per cent confidence limit, analogous to a significance of less than 2σ . The large upper error bar on $L_{\rm hi}$ is caused in part by the the degeneracy with Γ_L – for steeper power laws, bright progenitors are expected to be rarer, meaning there is a stronger bias towards the highest observed luminosity progenitor being well below the intrinsic $L_{\rm max}$. The likelihood of the brightest progenitor in a finite sample having a

luminosity close to L_{max} is worse for steeper Γ_L (see centre panel of Fig. 5). A similar degeneracy exists between L_{lo} and Γ_L . A steeper power-law slope forces the CLD to be closer to vertical at the faint end, which pulls L_{lo} to higher values (see right-hand panel of Fig. 5).

Given these degeneracies with Γ_L , it makes sense to look further into what the expectation value of the power-law slope might be. For an IMF $dN/dM \propto M^{\Gamma}$, and an initial mass-final luminosity relation (MLR) that scales as $L \propto M_{init}^{\alpha}$, it can be shown that we would expect a luminosity function $dN/dL \propto L^{\Gamma_L}$ with $\Gamma_L = (1 - \alpha + \Gamma)/\alpha$. For a Salpeter IMF slope of $\Gamma = -2.35$, and an MLR slope of $\alpha = 2$,³ we would expect $\Gamma_L = -1.675$. Our best-fitting value of Γ_L is shallower than this, but is within the 1 σ confidence limits. If we constrain $\Gamma_L = -1.675$, we find the 2D probability density function between L_{lo} and L_{hi} shown in Fig. 7. Here, the optimal value of L_{hi} shifts to a higher value of $\log(L_{hi}/L_{\odot}) = 5.28^{+0.12}_{-0.06}$, though the tension with the H–D limit remains $\sim 2\sigma$.

3.5 Conversion of L_{hi} to M_{init}

With posterior probabilities for $L_{\rm lo}$ and $L_{\rm hi}$, we can convert these grids from luminosity-space to mass-space by simply using the MLRs of various stellar models. In Table 2, we list the best-fitting mass ranges and 68 per cent confidence intervals for several singlestar evolution models: Geneva (both rotating and non-rotating; Ekström et al. 2012), KEPLER (Woosley & Heger 2007), STARS (Eldridge et al. 2008), and MIST (Choi et al. 2016). Of these models, we note that the MIST and Geneva models are only evolved as far as the end of C-burning, and so may not accurately reproduce the properties within a few years of SN. Furthermore, we caution that we are only considering single-star evolution, and that the MLR may have a different slope and a large degree of variance once binary evolution is included (Zapartas et al., in preparation).

Using the STARS models, we find $M_{\rm lo} = 7.1^{+0.9}_{-1.2} \,\rm M_{\odot}$ and $M_{\rm hi} = 17.9^{+3.7}_{-2.1} \,\rm M_{\odot}$, again quoting 68 per cent confidence limits, consistent with the 19 $\rm M_{\odot}$ (+ 2 $\rm M_{\odot}$ systematic) that we found in DB18. Mass limits for other suites of stellar models are listed in Table 2. In general, the results show agreement for $M_{\rm hi}$ within the range 17.9–20.5 $\rm M_{\odot}$, implying that perhaps the best fit is $M_{\rm hi} = 19.2 \,\rm M_{\odot}$ with a systematic error of $\pm 1.3 \,\rm M_{\odot}$. However, the random error is much larger, with typical 68 per cent confidence limits of $+4.5/-2.5 \,\rm M_{\odot}$. Though again these numbers do not contradict the existence of the 'RSG problem', we caution that at present the significance of this result is within 2σ .

4 CONCLUSIONS

We have taken a fresh look at the RSG problem in two ways. First, we compared the observed luminosities *L* of II-P/L SN progenitors to those of late-type RSGs in the field, to assess whether we could reasonably expect to have sampled close to the upper luminosity boundary (i.e the H–D limit, at log (L/L_{\odot} = 5.5) given the current sample size of progenitors. This is in contrast to previous studies, which convert the luminosities to masses, then compare to the expected mass distribution given the stellar IMF and a theoretical estimate of the MLR. By looking at the problem in this new way, we are able to eliminate the uncertainties and model dependencies that are introduced when one first converts

³All single-star evolutionary models we investigated (Geneva/STARS/Kepler) had α between 1.9 and 2.1.

²These confidence intervals are defined for the 3 degrees of freedom of our model, following Avni (1976).



1.0

-1.5

-2 (

4.0

4.1

4.2

4.3

 $\log(L_{lo}/L_{\odot})$

4.4

4.5

Figure 5. 2D probability distributions from the CLD fitting, plotted as pairs of parameters for the three parameters in our grid. The best-fitting parameters are indicated by the cross in each panel.

-1.0

 $\Gamma_{\rm L}$

-0.5

0.0

0.5

-1.5

og(L_{hi}/L_o

5.4

5.3

5.2

5.1

5.0

-2.0



4.4

4.5

5.6

5.5

5.4

5.3

5.2

5.1

5.0

4.0 4.1

4.2 4.3

 $log(L_{lo}/L_{\odot})$

log(L_{hi}/L_O)

Figure 6. The observed CLD (the yellow points and the error bars, corresponding to the 68 per cent limits in Fig. 4) and the best-fitting model CLD (the shaded contours).

the pre-explosion luminosities to initial mass before comparing to expectation values. Our results indicate that the difference in *L* between the brightest progenitor and the H–D limit of evolved RSGs can be explained in part by the small sample size. Quantitatively, the statistical significance of the RSG problem is below 2σ .

Secondly, we model the observed *L*-distribution of II-P/L progenitors as a simple power law with a slope Γ_L , and upper/lower luminosity limits $L_{\rm hi}$ and $L_{\rm lo}$. Our best-fitting value of the upper luminosity boundary is $\log(L_{\rm hi}/L_{\odot}) = 5.20^{+0.17}_{-0.11}$, again lower than the observed H–D limit, but again with a statistical significance of less than 2σ . The lower luminosity cut-off is measured to be $\log(L_{\rm lo}/L_{\odot}) = 4.39^{+0.10}_{-0.16}$. Our best-fitting value for the slope of the power law (Γ_L) is somewhat shallower than would be expected for a Salpeter IMF and an MLR of $L_{\rm fin} \propto M_{\rm init}^2$, though again the significance of this is low (<1 σ). When forcing Γ_L to be the expected value of -1.675, we find the upper luminosity cut-off increases to $\log(L_{\rm hi}/L_{\odot}) = 5.28^{+0.12}_{-0.08}$, but the statistical significance of the tension with the H–D limit is still within $\sim 3\sigma$.

The limits on the terminal luminosities of II-P and II-L progenitors can be translated to initial masses using evolutionary models.



Figure 7. Probability density as a function of $L_{\rm lo}$ and $L_{\rm hi}$ when the powerlaw slope is constrained to $\Gamma_L = -1.675$, which is the expected value for this parameter when assuming a Salpeter IMF and an MLR of $L_{\rm fin} \propto M_{\rm init}^2$.

Table 2. Upper and lower limits to the progenitor mass ranges, with 95% confidence intervals, for three different stellar evolution models.

Model	$M_{ m lo}/{ m M}_\odot$	$M_{ m hi}/{ m M}_{\odot}$
Geneva-nr	$7.8^{+1.0}_{-1.3}$	$20.5^{+4.5}_{-2.5}$
Geneva-r	$6.4^{+0.9}_{-1.2}$	$17.9^{+4.2}_{-2.3}$
KEPLER	$7.7^{+1.0}_{-1.3}$	$20.3^{+4.5}_{-2.5}$
STARS	$7.1^{+0.9}_{-1.2}$	$17.9^{+3.7}_{-2.1}$
MIST	$7.0^{+1.0}_{-1.3}$	$19.5^{+4.6}_{-2.5}$

By comparing several single-star codes, we find a lower mass limit between of $M_{lo} = 6-8 M_{\odot}$ and an upper mass limit $M_{hi} = 18-20 M_{\odot}$. The 68 per cent confidence limits on M_{hi} are $(+4.5, -2.3) M_{\odot}$. The best-fitting value on M_{hi} is therefore very close to the prediction of various evolutionary codes that stars with initial masses greater than $20 \,\mathrm{M}_{\odot}$ form black holes at core-collapse. However, we caution that the empirical uncertainties on M_{hi} are still very large, a situation that will not change until the sample size is at least doubled.

ACKNOWLEDGEMENTS

We thank Nathan Smith for helpful discussions, and the organisers of the FOE2019 meeting that inspired this work. We used the IDL astronomy library, available at https://idlastro.gsfc.na sa.gov. EB is supported by NASA through Hubble Fellowship grant HST-HF2-51428 awarded by the Space Telescope Science Institute, which is operated by the Association of Universities for Research in Astronomy, Inc., for NASA, under contract NAS5-26555.

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