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The FLAMINGO project: the coupling between baryonic feedback and cosmology in light of the S_8 tension

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ABSTRACT

Large-scale structure surveys have reported measurements of the density of matter, Ω_m , and the amplitude of clustering, σ_8 , that are in tension with the values inferred from observations of the cosmic microwave background. While this may be a sign of new physics that slows the growth of structure at late times, strong astrophysical feedback processes could also be responsible. In this work, we argue that astrophysical processes are not independent of cosmology and that their coupling naturally leads to stronger baryonic feedback in cosmological models with suppressed structure formation or when combined with a mechanism that removes dark matter from haloes. We illustrate this with two well-motivated extensions of the Standard Model known to suppress structure formation: massive neutrinos and decaying dark matter. Our results, based on the FLAMINGO suite of hydrodynamical simulations, show that the combined effect of baryonic and non-baryonic suppression mechanisms is greater than the sum of its parts, particularly for decaying dark matter. We also show that the dependence of baryonic feedback on cosmology can be modelled as a function of the ratio $f_b/c_v^2 \sim f_b/(\Omega_m\sigma_8)^{1/4}$ of the universal baryon fraction, f_b , to a velocity-based definition of halo concentration, c_v^2 , giving an accurate fitting formula for the baryonic suppression of the matter power spectrum. Although the combination of baryonic and non-baryonic suppression mechanisms can resolve the tension, the models with neutrinos and decaying dark matter are challenged by constraints on the expansion history.

Key words: neutrinos – galaxies: formation – quasars: general – dark matter – large-scale structure of Universe – cosmology: theory.

1 INTRODUCTION

The success of the Lambda cold dark matter (Λ CDM) model indicates that signatures of new physics are likely to manifest either as small modifications to the Λ CDM prediction or in the relatively unexplored high-redshift régime. As such, the model is under intense scrutiny at both the high-precision and high-redshift frontiers. Among a number of tensions and puzzling anomalies (e.g. Abdalla et al. 2022; Peebles 2022) is a long-standing discrepancy between measurements of the matter density and amplitude of fluctuations on $8 h^{-1}$ Mpc scales¹ obtained from large-scale structure probes, such as galaxy clustering, weak lensing, and the thermal

Sunyaev–Zeldovich (tSZ) effect, and the values extrapolated from measurements of the cosmic microwave background (CMB) (e.g. Aghanim et al. 2020; Asgari et al. 2021; Nunes & Vagnozzi 2021; Amon et al. 2022; Secco et al. 2022; Abbott et al. 2023; McCarthy et al. 2023). Further motivating the work at the high-precision frontier is the possibility to measure the sum of neutrino masses. The imprint of massive neutrinos could be detected by galaxy surveys such as the Dark Energy Spectroscopic Instrument (DESI) and *Euclid* surveys and the Legacy Survey of Space and Time (LSST), even for the minimum value allowed by oscillation data, but this requires per cent-level accuracy in large-scale structure measurements and predictions (e.g. Brinckmann et al. 2019; Chudaykin & Ivanov 2019).

Complicating these efforts is the fact that astrophysical processes, such as feedback from supernovae (SN) and active galactic nuclei (AGNs), change the distribution of matter even on relatively large scales (e.g. van Daalen et al. 2011; Chisari et al. 2019; Schneider et al. 2019; Debackere, Schaye & Hoekstra 2020). By heating and ejecting

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¹Described by the parameter combination $S_8 = (\Omega_m/0.3)^{1/2} \sigma_8$, where Ω_m is the present density of matter and σ_8 the standard deviation of the present linear matter field averaged in spheres of radius $8 h^{-1}$ Mpc.

gas into the intergalactic medium, AGN feedback can suppress the power spectrum of matter fluctuations by $\mathcal{O}(10)$ per cent on non-linear scales, $1 h \text{ Mpc}^{-1} < k < 10 h \text{ Mpc}^{-1}$. On smaller scales, the power spectrum may be boosted by star formation and gas cooling, both processes allowing matter to contract (e.g. Debackere et al. 2020; but see e.g. Forouhar Moreno et al. 2022). A crucial question for the interpretation of large-scale structure observations concerns the coupling between baryonic physics and cosmology. If the choice of cosmological model determined only the distribution of dark matter haloes, while the galaxies formed inside those haloes were identical, then the effects of baryons and cosmology might be modelled independently. On the other hand, a non-trivial coupling between galaxy formation and cosmological processes should give rise to ‘non-factorizable corrections’ to clustering statistics, introduced formally below. Note that there is a difference between the factorizability of two processes, meaning that their effects on some observable can be treated independently, and their degeneracy, meaning that their effects are indistinguishable.

A number of previous studies (e.g. van Daalen et al. 2011; Mummery et al. 2017; Pfeifer et al. 2020; Schneider et al. 2020; Stafford et al. 2020; van Daalen, McCarthy & Schaye 2020; Aricò et al. 2021; Paribelli et al. 2021; Broxterman et al. 2023; Salcido et al. 2023; Upadhye et al. 2023) have shown that the effects of cosmology and baryonic physics are indeed factorizable to a first approximation, with residual effects of up to several per cent for small variations in cosmology. There are several reasons to subject this topic to further systematic scrutiny. First of all, by modelling more precisely the non-factorizable corrections that arise from variations in cosmology in the presence of baryonic physics, we can improve existing prescriptions for baryonic feedback (e.g. Mead et al. 2015, 2021) and match the precision of Stage-IV galaxy surveys such as *Euclid* and LSST. Second, new physics introduced to account for tensions in cosmological data sets may change more significantly the strength of baryonic effects than simply varying the standard cosmological parameters. For example we will demonstrate a strong dependence of baryonic effects on the dark matter lifetime. Understanding the coupling between cosmology and baryonic feedback will shed light on the conditions under which their interaction becomes important and guide model builders towards novel solutions of cosmic tensions. Third, since baryonic feedback can itself be constrained in multiple independent ways, such as through weak lensing and X-ray or SZ measurements of cluster gas fractions (e.g. Semboloni et al. 2011; Harnois-Déraps et al. 2015; McCarthy et al. 2017; Schneider et al. 2020, 2022; Amon et al. 2022; Aricò et al. 2023; Chen et al. 2023; Grandis et al. 2023; Kugel et al. 2023; To et al. 2024), its dependence on cosmology might in principle be used as a cosmological probe if the degeneracy with astrophysical parameters and modelling uncertainty could be broken.

One could imagine different mechanisms through which baryonic processes, such as star formation and the growth of supermassive black holes, and hence baryonic feedback, could depend on cosmology. Although dark matter haloes share a universal density profile (Navarro, Eke & Frenk 1996; Navarro, Frenk & White 1997), their concentrations depend on cosmology (Eke, Navarro & Steinmetz 2001; Knollmann, Power & Knebe 2008; Prada et al. 2012; Kwan et al. 2013; Correa et al. 2015; Ragagnin et al. 2021). Cosmological model variations that slow the rate of structure formation (such as decreasing the matter density, Ω_m , or amplitude of clustering, σ_8) lead to less concentrated haloes, lowering the gravitational binding energy and altering the balance between outflows and black hole accretion (Booth & Schaye 2010; Bower et al. 2017; Chen et al. 2020). Another potential channel is the formation history of dark

matter haloes. If haloes assemble their mass more slowly, galaxy formation and the rapid growth of supermassive black holes may be delayed (Matthee et al. 2017; Davies, Pontzen & Crain 2022). A third possibility is that a change in the large-scale distribution of matter affects the halo environment, which could affect halo properties indirectly through assembly bias (Avila-Reese et al. 2005; Wechsler et al. 2006; Gao & White 2007) or affect feedback by changing the density of the halo outskirts. Finally and perhaps most crucially, variations in the baryon fraction, through shifts in Ω_b , alter the amount of gas that is available for star formation and black hole accretion.

These effects must be considered when extensions of the Λ CDM model are introduced. Consider massive neutrinos as an example. A change in the sum of neutrino masses, $\sum m_\nu$, could plausibly affect feedback through any of the four channels mentioned above. Neutrinos cluster less effectively on scales smaller than their free streaming length (for a review, see Lesgourgues & Pastor 2006), which results in less concentrated haloes, delayed structure formation, and smoother halo environments. Moreover, neutrinos also affect the baryon density, Ω_b/Ω_c , relative to the cold dark matter density, Ω_c , given that a change in neutrino mass at fixed matter density, $\Omega_m = \Omega_b + \Omega_c + \Omega_\nu$, will alter the amount of gas that is available for a halo of a given dark matter mass. Crucially, the universal baryon fraction should therefore be defined relative to the mass that clusters efficiently: $f_b \equiv \Omega_b/(\Omega_c + \Omega_b)$. These channels are not necessarily mutually exclusive. To find out which, if any, play a role in regulating baryonic feedback, we will use the new FLAMINGO suite of hydrodynamical simulations (Kugel et al. 2023; Schaye et al. 2023), which includes several feedback and cosmology variations. We will use halo properties (such as the concentration and formation epoch) as proxies for the ways in which feedback could depend on cosmology. We will then formulate a model to predict the non-factorizable corrections to the matter power spectrum in response to a shift in cosmology.

The organization of the paper is as follows. In Section 2, we discuss the FLAMINGO model and describe the simulations analysed in this paper. In Section 3, we will first demonstrate the existence of non-factorizable corrections for models that are close to a Planck-based Λ CDM model. This is followed by an analysis of possible mediating mechanisms. Using insights from that analysis, we then develop an analytical model for the dependence of baryonic feedback on cosmology and test it against the simulations. Those readers primarily interested in the S_8 tension may on first reading skip to Section 4, where we discuss the cosmological implications of these results in light of this tension and extensions of the Λ CDM model. In Section 5, we compare our results with commonly used halo model approaches. Finally, Section 6 provides the conclusion.

2 SIMULATIONS

Our analysis is based on the FLAMINGO suite of cosmological hydrodynamical simulations (Schaye et al. 2023). The FLAMINGO simulations use an updated version of the subgrid models adopted by the earlier OWLS (Schaye et al. 2010), Cosmo-OWLS (Le Brun et al. 2014), and BAHAMAS (McCarthy et al. 2017) projects. In a departure from its predecessors, the subgrid physics parameters were systematically calibrated by training emulators to predict key astrophysical quantities (the galaxy stellar mass function at $z = 0$ and cluster gas fractions at low z) and comparing directly with observations (Kugel et al. 2023). The simulations also used higher order multifluid initial conditions and a novel treatment of massive neutrinos (Hahn, Rampf & Uhlemann 2021; Elbers et al. 2021,

2022), both aimed at improving the accuracy of its large-scale structure predictions. Combined with the unprecedented volume of the simulations, these improvements make FLAMINGO ideal for precision cosmology applications.

The largest simulation contains $N_c = N_b = 5040^3$ dark matter and baryon particles and $N_\nu = 2800^3$ massive neutrino particles in a periodic $(2.8 \text{ Gpc})^3$ volume. This simulation assumes a fiducial Λ CDM cosmology with minimal neutrino masses, $\sum m_\nu = 0.06 \text{ eV}$, and parameters based on the Dark Energy Survey Year 3 analysis of 3×2 pt clustering, baryon acoustic oscillations (BAO), redshift space distortions (RSD), SNe Ia, and *Planck* CMB data (Abbott et al. 2022). In addition, the FLAMINGO suite contains many simulations with the same mass resolution in a $(1 \text{ Gpc})^3$ volume. These simulations span a range of subgrid physics and cosmological parameter variations. Among these are simulations with the fiducial cosmology, but with subgrid parameters calibrated to cluster gas fractions that are $n\sigma$ above or below the observations. For each hydrodynamical simulation, there is a gravity-only counterpart that treats dark matter and baryons as a single cold fluid, but still includes the effects of massive neutrinos (also called ‘dark matter only’ or DMO).

The hydrodynamical simulations include improved prescriptions for gas cooling (Ploekinger & Schaye 2020), star formation (Schaye & Dalla Vecchia 2008), stellar feedback (Chaikin et al. 2022), and chemical enrichment (Wiersma et al. 2009). Supermassive black holes are modelled following the approaches of Springel et al. (2005), Di Matteo et al. (2008), Booth & Schaye (2009), and Bahé et al. (2022). For some runs, AGN feedback was implemented as jets instead of thermally driven winds (Huško et al. 2022). The simulations were run with the SWIFT cosmological hydrodynamics code (Schaller et al. 2018, 2023), using the SPHENIX flavour of SPH (Borrow et al. 2022), on the COSMA-8 facility at Durham.

The initial conditions were generated with third-order Lagrangian perturbation theory (3LPT) at $z = 31$ with separate transfer functions for dark matter, baryons, and neutrinos (Hahn et al. 2021; Elbers et al. 2022), using a modified version of MONOFONIC² (Hahn et al. 2020; Michaux et al. 2021) and FASTDF (Elbers 2022b), with transfer functions computed with CLASS (Lesgourgues 2011). Halo catalogues were produced with VELOCIRAPTOR (Elahi et al. 2019) and post-processed with the spherical overdensity analysis tool SOAP.³

2.1 Model extensions

To explore the varying impact of cosmology-dependent feedback for models beyond Λ CDM, we consider two extensions of the base model. Although all simulations have neutrinos, we will consider runs that vary the massive neutrino content. In addition, we will consider models in which dark matter is unstable and decays invisibly to dark radiation (e.g. Cen 2001; Wang & Zentner 2010; Aoyama et al. 2014; Audren et al. 2014; Berezhiani, Dolgov & Tkachev 2015; Enqvist et al. 2015; Poulin, Serpico & Lesgourgues 2016; Hubert et al. 2021; Tanimura et al. 2023). Both extensions retard the growth of structure compared to Λ CDM with minimal neutrino masses, which we will show also enhances the strength of baryonic feedback.

Massive neutrinos were included in the simulations using the δf method (Elbers et al. 2021), which minimizes shot noise without neglecting the non-linear evolution of the phase-space distribution.

²<https://github.com/wullm/monofonic>

³<https://github.com/SWIFTSIM/SOAP>

The neutrino particles start from relativistic initial conditions and use a special relativistic velocity correction to produce accurate clustering on large scales. For models with $\sum m_\nu = 0.06 \text{ eV}$, one massive species and two massless species were assumed, with the latter contributing only at the background level. For larger neutrino masses, a degenerate mass spectrum was assumed. In Elbers et al. (2021, 2022), it is shown that the effects of neutrinos on the power spectrum can be modelled with 0.1 per cent-level accuracy, enabling the detailed analysis in this paper (see also Adamek et al. 2023).

In the decaying cold dark matter model (DCDM), cold dark matter is an unstable particle with mean lifetime τ that decays into a new relativistic particle, referred to as dark radiation. In general, only a fraction f of the dark matter might be unstable (e.g. Berezhiani et al. 2015; Hubert et al. 2021), but we will focus on the $f = 1$ case for simplicity. The background densities of decaying cold dark matter and dark radiation then evolve as

$$\dot{\rho}_{\text{cdm}} = -3\mathcal{H}\rho_{\text{cdm}} - a\Gamma_{\text{cdm}}\rho_{\text{cdm}}, \quad (1)$$

$$\dot{\rho}_{\text{dr}} = -4\mathcal{H}\rho_{\text{dr}} + a\Gamma_{\text{cdm}}\rho_{\text{cdm}}, \quad (2)$$

where $\Gamma_{\text{cdm}} = \tau^{-1}$ is the decay rate, dots denote conformal time derivatives, a is the scale factor, and $\mathcal{H} = \dot{a}/a$. These equations were implemented at the background level in the N -body code SWIFT, modifying the equations of motion in the expanding reference frame. At the perturbation level, dark matter decay was implemented by adjusting the particle masses in proportion to the fraction of dark matter that has decayed, following Enqvist et al. (2015) and Hubert et al. (2021). For the gravity-only (DMO) simulations, the evolving particle masses take into account the fact that Ω_b is constant. We also modified the initial conditions code MONOFONIC (Hahn et al. 2020) and backscaling code ZWINDSTROOM (Elbers 2022a) to account for dark matter decay and used the publicly available implementation of decaying dark matter in CLASS⁴ (Audren et al. 2014) for the transfer functions.

We ran two large hydrodynamical simulations with the DCDM model at the fiducial resolution in a $(1 \text{ Gpc})^3$ volume, using cosmological parameters based on the existing *Planck* simulation (Schaye et al. 2023), but adjusting Ω_Λ and the initial value of Ω_{cdm} to keep the primordial dark matter to baryon density ratio and the curvature, $\Omega_k = 0$, fixed at the *Planck* values. Our choice for the decay rate, Γ , is based on an analysis of the final data release of *Planck* CMB temperature and polarization data by Tristram et al. (2023). Using the COBAYA sampler (Torrado & Lewis 2021), we obtain a 95 per cent upper bound of $\Gamma < 12.8 \text{ km s}^{-1} \text{ Mpc}^{-1}$. This is to be compared with a recent analysis by Tanimura et al. (2023) of CMB, tSZ, BAO, and SN Ia data, which gave a 95 per cent upper bound of $\Gamma < 26 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and a preferred value of $\Gamma = 7.1 \text{ km s}^{-1} \text{ Mpc}^{-1}$. On the other hand, tighter constraints of $\Gamma < 6 \text{ km s}^{-1} \text{ Mpc}^{-1}$ have been obtained from other data combinations (Audren et al. 2014; Aubourg et al. 2015; Enqvist et al. 2020).

Based on these results, we choose for our simulations decay rates of $\Gamma = 12 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ($\tau = 81 \text{ Gyr}$) and $\Gamma = 24 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ($\tau = 41 \text{ Gyr}$). Although essentially ruled out, the second model is included to understand better the effect on baryonic feedback of extreme cosmological excursions, which must necessarily be modelled in Monte Carlo analyses. For the same reason, we also extend the main FLAMINGO suite by running an additional $(1 \text{ Gpc})^3$ simulation with a large neutrino mass of $\sum m_\nu = 0.48 \text{ eV}$, which is similarly ruled out by *Planck* (but see Di Valentino & Melchiorri

⁴https://github.com/lesgourg/class_public

2022). We refer the reader to Table 1 for an overview of the large simulations used in this paper.

2.2 Additional simulations

While the simulations listed in Table 1 have varying cosmological parameters, they are limited to specific scenarios or shifts in individual parameters. To mimic the type of parameter variations encountered in a Monte Carlo analysis, we ran seven additional simulations with the same resolution but in a smaller volume (side length $L = 200$ Mpc) with cosmological parameters (h , $\Omega_b h^2$, $\Omega_m h^2$, n_s , σ_8) sampled in a Latin hypercube with parameter ranges set by the $\pm 3\sigma$ error bars around the best-fitting Planck TTTEEE + lowE model (Aghanim et al. 2020), except in the case of the power spectrum normalization, σ_8 , for which we used the $\pm 5\sigma$ range:

$$\begin{aligned} h &\in [0.657, 0.6894], \\ \Omega_b h^2 &\in [0.021933, 0.022833], \\ \Omega_m h^2 &\in [0.13984, 0.14644], \\ n_s &\in [0.95345, 0.97865], \\ \sigma_8 &\in [0.776, 0.848]. \end{aligned} \quad (3)$$

To confirm an assumption of the model developed in Section 3, related to the scaling of the black hole mass, we ran another four simulations ($L = 200$ Mpc) identical to the fiducial FLAMINGO case but with the baryon fraction, $f_b = \Omega_b / (\Omega_b + \Omega_c)$, varied by $\Delta f_b / f_b \in \{-4 \text{ per cent}, -2 \text{ per cent}, +2 \text{ per cent}, +4 \text{ per cent}\}$. These small simulations all used the fiducial subgrid physics model and a fixed neutrino mass of $\sum m_\nu = 0.06$ eV, modelled as one massive and two massless species. Gravity-only counterparts were also run for each model.

3 THE DEPENDENCE OF FEEDBACK ON COSMOLOGY

We begin our analysis by studying the cosmology dependence of the baryonic effect on the matter power spectrum in Section 3.1, demonstrating the existence of non-factorizable corrections. The baryonic effect, which corresponds to the combined impact of the processes mentioned above (e.g. gas cooling, star formation, AGNs, and SN feedback) is measured by comparing the power spectrum in hydrodynamical simulations with that in dark matter only simulations. The essential role of the halo concentration in explaining the non-factorizable corrections is discussed in Section 3.2. We then construct a simple model for the non-factorizable correction to the power spectrum in Section 3.3, before fitting it to the simulations in Section 3.4.

3.1 Non-factorizable corrections to the matter power spectrum

We define the baryonic suppression of the matter power spectrum as the ratio

$$F_b(k) = \frac{P_m^{\text{hydro}}(k)}{P_m^{\text{DMO}}(k)}, \quad (4)$$

of the hydrodynamical matter power spectrum, $P_m^{\text{hydro}}(k)$, to the gravity-only matter power spectrum, $P_m^{\text{DMO}}(k)$. The top panel of Fig. 1 shows this suppression at $z = 0$ for a set of cosmological models that are close to the best-fitting Planck Λ CDM model (Aghanim et al. 2020). The results are based on the 11 (0.2 Gpc)³ simulations described in Section 2.2. Despite the smaller volume

of these simulations, the dependence of F_b on cosmology can be determined to within about 0.5 per cent on the scales of interest (see Appendix A).

Let us consider first the general trend. The ratio equals unity on large scales up to about $k \approx 0.5 h \text{ Mpc}^{-1}$ and then decreases to a dramatic minimum at $k \approx 10 h \text{ Mpc}^{-1}$. This happens primarily because feedback from AGNs expels gas from $10^{14} M_\odot$ haloes, which lowers their contribution to the power spectrum at these scales (Semboloni et al. 2011; van Daalen et al. 2011; Schneider et al. 2019; Debackere et al. 2020). Although we focus here on the scales $k \leq 10 h \text{ Mpc}^{-1}$ most relevant for weak lensing observations, the suppression eventually turns into an enhancement of clustering for $k \geq 30 h \text{ Mpc}^{-1}$ because gas cooling and star formation allows haloes to contract, increasing the density on small scales. Precisely characterizing this is beyond the scope of the FLAMINGO project.

Assuming that the baryonic suppression is independent of cosmology, we may factorize the change in the power spectrum from one model (1) to another (2) as

$$\frac{P_2^{\text{hydro}}}{P_1^{\text{hydro}}} = \left(\frac{P_2^{\text{DMO}}}{P_1^{\text{DMO}}} \right) \left(\frac{P_2^{\text{hydro}}/P_2^{\text{DMO}}}{P_1^{\text{hydro}}/P_1^{\text{DMO}}} \right) \approx \frac{P_2^{\text{DMO}}}{P_1^{\text{DMO}}}. \quad (5)$$

We refer to the second term in brackets as the *non-factorizable correction* to this approximation. This factor is implicitly assumed to be 1 in works that ignore the cosmological coupling. The bottom panel of Fig. 1 shows the correction for Planck-based variations in cosmology, assuming fixed astrophysical parameters and subgrid modelling. Varying the cosmological parameters by a few per cent produces corrections on scales $k > 2 h \text{ Mpc}^{-1}$ of up to 4 per cent – 5 per cent, which is relatively large compared to the total baryonic effect of 10 per cent – 15 per cent. Notice also that the deviations are mostly monotonic on these scales. This suggests that there is a systematic trend to be uncovered.

3.2 The role of halo concentration

The baryonic effect on the matter power spectrum can be understood as an aggregate of the effects on individual dark matter haloes, integrated over a range of masses, since the stars and black holes that are responsible form inside haloes. Let us therefore consider the baryonic effect on individual bound structures. The idea is that a change in cosmology alters the halo population, which subsequently leads to a change in the baryonic effect. We enumerated earlier a number of hypotheses for ways in which cosmology might affect feedback: by changing the structure of dark matter haloes, their formation histories, or their environments.⁵ We will argue that the first two mechanisms – halo structure and formation history – both play a role to some extent, but that for the range of scales most relevant for weak lensing observations, the first mechanism alone is important. Remarkably, we can neatly separate out these two mechanisms, depending on the mass of the halo. Finally, we will show that the influence of the environmental density around the halo is negligible.

To proceed, we match each halo in the hydrodynamical simulation with a halo in the gravity-only version of the same simulation by pairing the 10 most strongly bound particles,⁶ which allows us to determine the properties of the same halo with and without baryonic effects. This is done without varying the cosmological

⁵Or their baryonic contents, but we will return to that crucial factor later.

⁶Sorting halo particles according to their binding energies and using only a small number of most bound particles improves the quality of the matching.

Table 1. An overview of the large FLAMINGO simulations used in this paper. The number of baryon particles, N_b , is equal to the number of cold dark matter particles, N_c , for the simulations that have them. The number of neutrino particles is always $N_\nu = N_c/1.8^3$. For each simulation, there exists a gravity-only (DMO) counterpart with combined CDM and baryon particle mass $m_{cb} = m_c + m_g$. The columns correspond to the side length, L , the number and (initial) mass of cold dark matter particles, N_c and m_c , the initial mass of gas particles, m_g , and the cosmological parameters. The final column shows the dark matter decay rate, Γ , in units of $100 \text{ km s}^{-1} \text{ Mpc}^{-1} = H_0/h$ for the simulations with decaying cold dark matter (DCDM). For the DCDM models, the Ω_c column lists the sum of the present-day densities of decaying cold dark matter and dark radiation. The simulations with the suffix $f_{\text{gas}} \pm n\sigma$ are identical to L1_m9, but have subgrid physics parameters calibrated to cluster gas fractions that are $n\sigma$ higher or lower than the observed data. All simulations assume a flat ($\Omega_k = 0$) Universe with massive neutrinos and with an amount of radiation corresponding to $T_{\text{CMB}} = 2.7255 \text{ K}$ and $N_{\text{eff}} = 3.044$ effective relativistic neutrino species at high redshift.

Identifier	L/Gpc	N_c	m_c/M_\odot	m_g/M_\odot	h	Ω_m	Ω_c	Ω_b	$\sum m_\nu$	σ_8	$10^9 A_s$	n_s	$\Gamma h/H_0$
L2p8_m9	2.8	5040^3	5.65×10^9	1.07×10^9	0.681	0.306	0.256	0.0486	0.06 eV	0.807	2.099	0.967	–
L1_m9	1.0	1800^3	5.65×10^9	1.07×10^9	0.681	0.306	0.256	0.0486	0.06 eV	0.807	2.099	0.967	–
L1_m9- $f_{\text{gas}} - 8\sigma$	1.0	1800^3	5.65×10^9	1.07×10^9	0.681	0.306	0.256	0.0486	0.06 eV	0.807	2.099	0.967	–
L1_m9- $f_{\text{gas}} - 4\sigma$	1.0	1800^3	5.65×10^9	1.07×10^9	0.681	0.306	0.256	0.0486	0.06 eV	0.807	2.099	0.967	–
L1_m9- $f_{\text{gas}} - 2\sigma$	1.0	1800^3	5.65×10^9	1.07×10^9	0.681	0.306	0.256	0.0486	0.06 eV	0.807	2.099	0.967	–
L1_m9- $f_{\text{gas}} + 2\sigma$	1.0	1800^3	5.65×10^9	1.07×10^9	0.681	0.306	0.256	0.0486	0.06 eV	0.807	2.099	0.967	–
Planck	1.0	1800^3	5.72×10^9	1.07×10^9	0.673	0.316	0.265	0.0494	0.06 eV	0.812	2.101	0.966	–
Planck ν 0.24Var	1.0	1800^3	5.67×10^9	1.06×10^9	0.662	0.328	0.271	0.0510	0.24 eV	0.772	2.109	0.968	–
Planck ν 0.24Fix	1.0	1800^3	5.62×10^9	1.07×10^9	0.673	0.316	0.261	0.0494	0.24 eV	0.769	2.101	0.966	–
Planck ν 0.48Fix	1.0	1800^3	5.62×10^9	1.07×10^9	0.673	0.316	0.256	0.0494	0.48 eV	0.709	2.101	0.966	–
PlanckDCDM12	1.0	1800^3	5.71×10^9	1.07×10^9	0.673	0.274	0.246	0.0494	0.06 eV	0.794	2.101	0.966	0.12
PlanckDCDM24	1.0	1800^3	5.70×10^9	1.07×10^9	0.673	0.239	0.229	0.0494	0.06 eV	0.777	2.101	0.966	0.24
LS8	1.0	1800^3	5.65×10^9	1.07×10^9	0.682	0.305	0.256	0.0473	0.06 eV	0.760	1.836	0.965	–

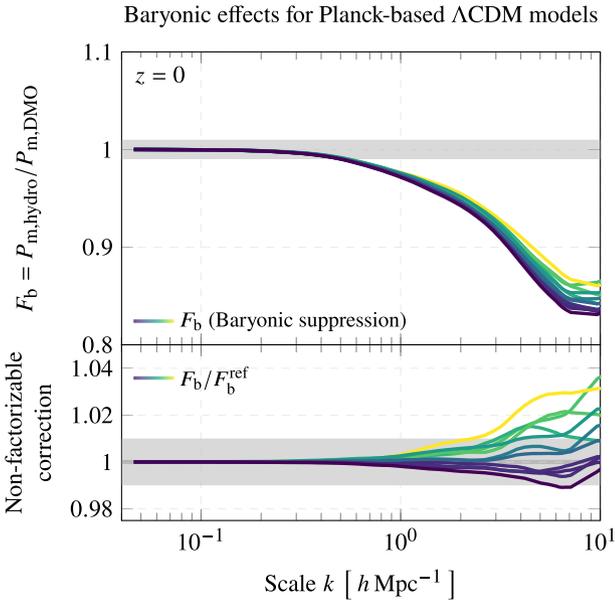


Figure 1. The baryonic effect on the matter power spectrum, P_m , in 11 Λ CDM models close to the best-fitting *Planck* model. The bottom panel shows that the non-factorizable corrections can be as large as 4 per cent – 5 per cent even for small shifts in standard cosmological parameters. The solid lines correspond to the 5-bin central moving average of the data. The grey band represents a 1 per cent error. The colours indicate the average deviation from the baseline model.

model, instead relying on the inherent scatter in halo properties in the large L2p8_m9 simulations. The hydrodynamical simulation has 30 million haloes with masses exceeding $10^{12} M_\odot$ and 0.2 million haloes with masses exceeding $10^{14} M_\odot$, providing a large enough sample to make additional cuts based on secondary and tertiary halo properties. Our matching procedure results in a successful bijective pairing for 98.4 per cent of haloes with $M_{200c} > 10^{12} M_\odot$ and 99.2 per cent of

haloes with $M_{200c} > 10^{13} M_\odot$.⁷ We are interested in the baryonic effect on the halo mass, for which we define the ratio

$$R_b(M_{\text{DMO}}) = \frac{M_{\text{hydro}}}{M_{\text{DMO}}}, \quad (6)$$

using M_{200c} masses. We exclusively consider central haloes, ignoring satellites. The baryonic effect, R_b , depends sensitively on the gravity-only mass. We therefore split the sample into bins of M_{DMO} . Within each bin, we rank the haloes according to a secondary halo property (see below) and compute R_b for the five quintiles: the equal-sized groups with normalized rank between $[0, 0.2]$ up to $[0.8, 1]$. The mass bins are small enough that the correlation between the secondary property and halo mass is minimal. In each case, we compute the halo property from the gravity-only simulation and consider its role in determining the suppression of the halo mass in the hydrodynamical version, such that the direction of causality is unambiguous. We focus on the following properties:

(i) *Maximum circular velocity*, V_{max} . The maximum circular velocity is defined in terms of the cumulative radial mass profile $M(\leq r)$, computed using all particles bound to the main subhalo, as $V_{\text{max}} = \max_{r>0} \sqrt{GM(\leq r)/r}$, where the radius r is relative to the centre of potential.

(ii) *Concentration*, c_v . We use a velocity-based proxy for the halo concentration,

$$c_v = V_{\text{max}}/V_{200c}, \quad (7)$$

using the maximum circular velocity, V_{max} , and virial velocity, $V_{200c} = \sqrt{GM_{200c}/R_{200c}}$. For the usual definition of concentration in terms of the scale radius, R_s , we have $c = R_{200c}/R_s \propto c_v^2$ (Springel et al. 2008; Prada et al. 2012). This velocity-based definition of concentration remains sensible when the density profile cannot be determined reliably and can be computed directly from properties available in our halo catalogues.

(iii) *Formation epoch*, a_x . The scale factor time, a , at which the halo first accreted x per cent of its present-day mass, computed by

⁷Here, M_{200c} corresponds to the total mass contained in a spherical region with an average density equal to 200 times the critical density.

linearly interpolating between adjacent snapshots. We will consider both a_{25} and a_{50} .

(iv) *Environmental density, δ_r* . We characterize the environment by computing the total mass, M_r , enclosed by haloes within a radius of r Mpc, excluding the halo itself. The environmental density, δ_r , is then defined as $\delta_r = M_r / \langle M_r \rangle - 1$, where $\langle M_r \rangle$ is the average value for all haloes in the sample. We will use δ_8 .

The resulting $R_b(M_{\text{DMO}})$ curves, split into quintiles of the secondary halo property, are shown in Fig. 2. Each curve shows the median of R_b in a given bin of mass and secondary property. First of all, we note that the general trend arises from the interplay between the depth of the gravitational potential well and the strength of stellar and AGN feedback at those masses (Cui, Borgani & Murante 2014; Velliscig et al. 2014). For the lowest mass shown, $10^{12} M_\odot$, AGN feedback is not important and the baryonic suppression of the mass is mainly driven by the outflow of gas due to supernovae. As the mass increases, AGN feedback becomes increasingly important and this drives the hydrodynamical mass down relative to the gravity-only mass, even as SN feedback becomes less effective. Finally, the ratio eventually approaches unity for the most massive haloes beyond a few times $10^{14} M_\odot$, since even though gas is still ejected from massive galaxy clusters, particularly from satellites and progenitors of satellites, this is increasingly compensated by infalling gas (Mitchell et al. 2020; Mitchell & Schaye 2022; Wright et al. 2024).

Let us now consider the effect of the halo concentration, c_v , in greater detail. This is shown in the top left panel of Fig. 2. There is a clear dependence of R_b on concentration. For haloes with dark matter masses between 10^{12} and $10^{13} M_\odot$, the suppression is smaller for less concentrated haloes, but the trend reverses for $M > 10^{13} M_\odot$. There are different mechanisms at play in these two régimes. Halo concentration is anticorrelated with formation epoch, older haloes being more concentrated on average, as the cosmic matter density was higher at the time of their formation (e.g. Navarro et al. 1996, 1997; Wechsler et al. 2002; Ludlow et al. 2013). In the low-mass range, the dependence on concentration is due to the sensitivity of the black hole mass to the formation epoch of the halo. In the high-mass range, the dependence on concentration is instead due to the binding energy of the halo rather than due to the formation history.

To see this, consider the dependence on the formation epoch shown in the top right panel for a_{50} . In this case, we additionally restrict the halo concentration, c_v , to the [40 per cent, 60 per cent] inter percentile range to reduce the correlation between c_v and a_{50} . For haloes $M < 10^{13} M_\odot$, the suppression does depend on formation epoch. In this mass range, the masses of older haloes are more strongly suppressed. This could be due to early galaxy mergers triggering rapid growth of the central supermassive black hole (Davies et al. 2022) or simply because there has been more time for mergers and accretion (Matthee et al. 2017). There is no dependence on a_{50} , however, for haloes beyond $10^{13} M_\odot$. This shows that the dependence on concentration seen in that mass range is not due to the formation epoch. To understand this, we show the black hole mass relative to the gravity-only mass, $M_{\text{BH}}/M_{\text{DMO}}$, in the inset graph. We see that haloes with masses between 10^{12} and $10^{13} M_\odot$ fall into a critical transition range where non-linear black hole growth is on the cusp of being triggered (Bower et al. 2017; McAlpine et al. 2018), depending on the mass and formation epoch. At the high mass end, all black holes are self regulating, limiting their own growth by stopping the inflow of gas, and attain a more or less universal mass as a function of the dark matter mass and concentration, as might be expected from black hole scaling relations (Booth & Schaye

2010, 2011). From this point on, the dependence on formation epoch essentially disappears. If $M_{\text{BH}}/M_{\text{DMO}}$ is kept fixed, the dependence of R_b on concentration becomes monotonic, with more concentrated haloes suffering a smaller suppression (not shown). This confirms that the formation epoch plays a role in determining when the initial growth stage of the black hole occurs, but that the halo concentration determines the intensity of AGN feedback once the black holes become self regulating.

In the bottom left panel, we once again show the dependence on concentration, c_v , but now controlling for the formation history. We do this by restricting both formation time proxies, a_{25} and a_{50} , to their [30 per cent, 70 per cent] inter percentile ranges. In the low mass range around $5 \times 10^{12} M_\odot$, the dependence on concentration disappears. However, beyond $10^{13} M_\odot$, we recover the behaviour seen in the top left panel, with more concentrated haloes experiencing a smaller baryonic suppression. We attribute this to the increased gravitational binding energies of the dark matter haloes, trammelling the outflows driven by AGNs.

A third possibility is that cosmology affects feedback by altering the halo environment. We study this possibility by determining the dependence of R_b on the environmental density, δ_8 , defined in terms of the mass contained by haloes within 8 Mpc. The bottom right panel of Fig. 2 shows that this property is barely correlated with the baryonic suppression of halo mass. This may at first seem counterintuitive, given that haloes with greater concentrations are found in denser regions (Avila-Reese et al. 2005; Wechsler et al. 2006). However, the environmental dependence of concentration is very weak compared to the scatter in concentrations at fixed mass (Macciò et al. 2007). The conclusion is the same for different definitions of δ_r , such as δ_4 or δ_{12} , as well as definitions based on the total matter density. Hence, the large-scale environmental density does not appear to play a major role in regulating feedback.

Returning to the matter power spectrum, we note that the baryonic suppression on scales $0.1 h \text{ Mpc}^{-1} \leq k \leq 10 h \text{ Mpc}^{-1}$ is mostly determined by haloes with masses $10^{13} M_\odot < M < 10^{14} M_\odot$ (e.g. Semboloni et al. 2011; Debackere et al. 2020; Salcido et al. 2023; van Loon & van Daalen 2024). The results of this section indicate that the strength of baryonic feedback in this mass range is strongly correlated with the binding energy, as described by the halo concentration. Hence, a model of the non-factorizable corrections should first account for the change in halo concentration.

3.3 A simple physical model

Let us now develop a physical model for the non-factorizable correction that also incorporates the dependence on the universal baryon fraction, $f_b = \Omega_b / (\Omega_b + \Omega_c)$. We focus on AGN feedback, which is the primary mechanism responsible for the baryonic suppression of the matter power spectrum on large scales, given the halo masses involved. The energy injected by the AGN is directly proportional to the black hole mass accretion rate:

$$\dot{E}_{\text{AGN}} = \epsilon_r \epsilon_f \dot{m}_{\text{accr}} c^2, \quad (8)$$

where ϵ_r is the radiative efficiency of the black hole and ϵ_f is the efficiency with which the energy is coupled to the gas. In the FLAMINGO simulations, $\epsilon_r \epsilon_f = 0.015$ is fixed to reproduce the observed black hole scaling relations (Booth & Schaye 2009). The growth rate of the black hole mass is $\dot{M}_{\text{BH}} = (1 - \epsilon_r) \dot{m}_{\text{accr}}$. Therefore, neglecting the small initial seed mass, the total energy injected can be related to the final black hole mass as

$$E_{\text{AGN}} = \epsilon_r \epsilon_f \int dt \dot{m}_{\text{accr}} c^2 = \frac{\epsilon_r \epsilon_f}{1 - \epsilon_r} M_{\text{BH}} c^2. \quad (9)$$

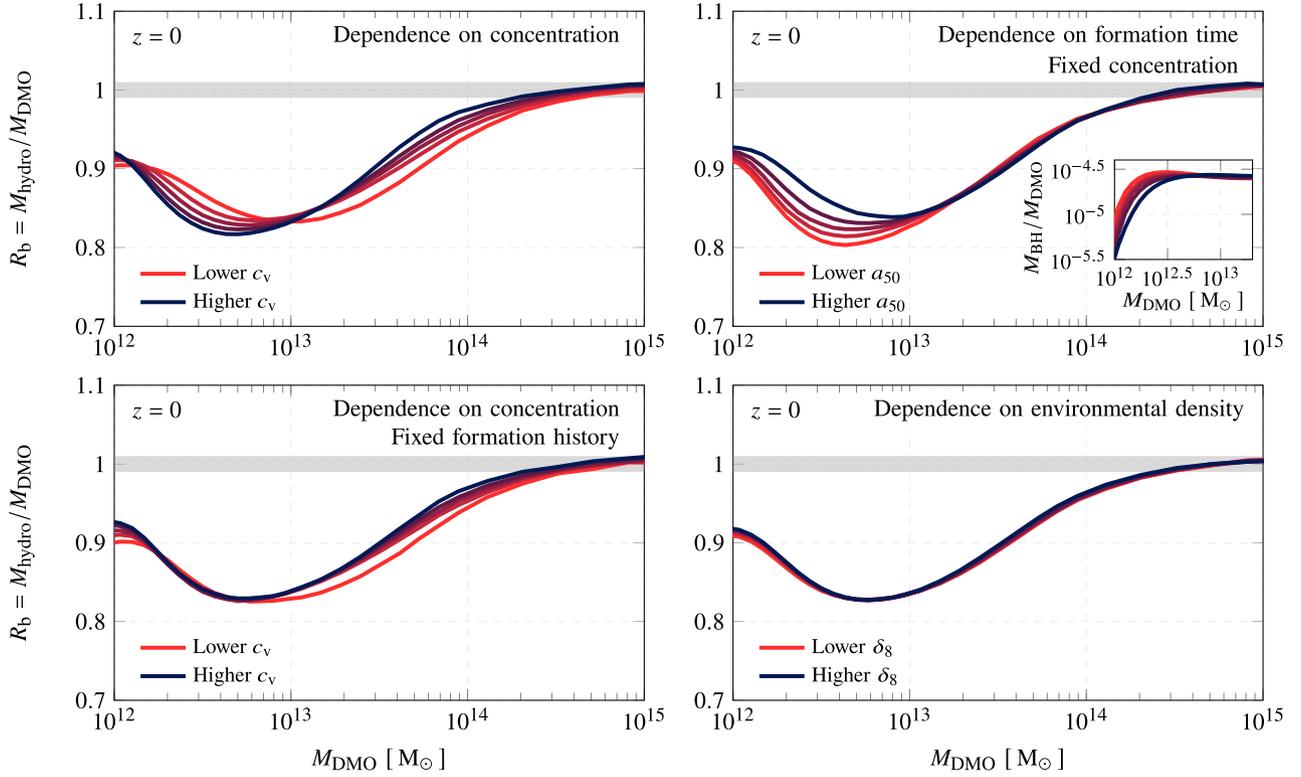


Figure 2. The influence of different halo properties on the baryonic effect on halo mass, $R_b = M_{\text{hydro}}/M_{\text{DMO}}$, comparing the masses of matched haloes in the corresponding gravity-only and hydrodynamical simulations. We show the dependence of the mass ratio on secondary halo properties: concentration (top left), formation time at fixed concentration (top right), concentration at fixed formation history (bottom left), and environmental density (bottom right). The inset graph in the top right panel shows how the ratio of black hole mass to gravity-only mass, $M_{\text{BH}}/M_{\text{DMO}}$, depends on mass and formation epoch. The colours indicate quintiles of the secondary halo property, calculated within each mass bin, with red indicating a lower value of that property and dark blue a higher value.

This energy is used to heat gas around the black hole in the centre of the galaxy. As a consequence, gas is ejected from the central region, thereby limiting further black hole growth. The gravitational binding energy of gas that once occupied the central region at some small radius R , but is now located at some larger radius $R' \gg R$, must decrease significantly. Let us assume that the energy injected by the AGN is used to lower the gravitational binding energy:

$$E_{\text{AGN}} = -\Delta E_{\text{grav}} = E_{\text{grav}}^{\text{ini}} - E_{\text{grav}}^{\text{fin}} \approx E_{\text{grav}}^{\text{ini}}. \quad (10)$$

Consider the initial time before the rapid growth phase of the black hole was triggered and gas was ejected. Let M be the total mass and $M_b = f_b M$ the baryonic mass contained in the central region with radius R . Then the initial gravitational binding energy is

$$E_{\text{grav}}^{\text{ini}} = \frac{GM M_b}{R}. \quad (11)$$

We will assume that baryons initially dominated the gravitational potential at the centre, such that $M \approx M_b$ and $E_{\text{grav}} \propto f_b^2$. On the other hand, if dark matter dominated the potential, $E_{\text{grav}} \propto f_b$. In general, we may write $E_{\text{grav}} \propto f_b^n$. Continuing with $n = 2$, we find that the black hole mass should scale as

$$M_{\text{BH}} c^2 \propto E_{\text{AGN}} \propto f_b^2 \frac{GM^2}{R}. \quad (12)$$

Here, it is worth pausing and considering the implications so far. The idea of relating the black hole mass to the gravitational binding energy of the gas is not new (Silk & Rees 1998; Ostriker, Bode & Babul 2005; Booth & Schaye 2010; Zubovas & King 2016; Bower et al. 2017; Oppenheimer 2018; Chen et al. 2020;

Davies et al. 2020). However, many previous models inferred that $M_{\text{BH}} \propto E_{\text{grav}} \propto f_b^n$ with $n = 1$ (e.g. Zubovas & King 2016; Chen et al. 2020; Davies et al. 2020), which would be the case if the gravitational potential were initially dominated by dark matter rather than baryons.

We verified for the clusters in our simulations that the mass density is dominated by baryons at high redshift for $R \lesssim 10$ kpc, due to early star formation and gas cooling. This is in line with the expectation from higher resolution simulations (e.g. Schaller et al. 2015). However, we caution that the density profile is not converged at these small radii at the fiducial FLAMINGO resolution. As an alternative way to verify our assumptions, we ran a number of simulations varying only the universal baryon fraction by $\Delta f_b/f_b \in \{-4 \text{ per cent}, -2 \text{ per cent}, +2 \text{ per cent}, +4 \text{ per cent}\}$, relative to the fiducial cosmology. We compute the ratio of the black hole mass energy available for feedback, $\epsilon_r \epsilon_f / (1 - \epsilon_r) M_{\text{BH}} c^2$, to the gravitational binding energy, $E_{\text{grav}} = GM^2/R$. We fix the radius of the central region at $R = 100$ kpc, which is resolved and corresponds approximately to the scale radius of $10^{13} M_{\odot}$ haloes. The results are shown in Fig. 3 for haloes in two mass bins with $\log_{10}(M_{200c}/M_{\odot}) \in [12, 13]$ and $[13, 14]$. While we emphasize that our assumptions are simplistic, ignoring for instance the dependence of radiative cooling losses on the baryon fraction, the proportionality (12) is reproduced by the simulations. This suggests that it is the binding of baryons to baryons that determines the black hole mass in the FLAMINGO simulations.

Next, let us assume that the gas heated by the AGN and ejected from the central region has a velocity distribution $f(v/V_g)$, with scale

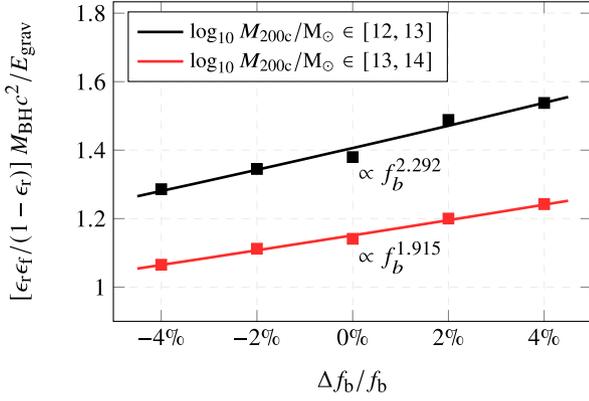


Figure 3. The ratio of the black hole subgrid mass energy available for feedback, $\epsilon_r \epsilon_f / (1 - \epsilon_r) M_{\text{BH}} c^2$, to the gravitational binding energy of the halo, $E_{\text{grav}} \equiv GM(\leq R)^2/R$, in a central sphere with $R = 100$ kpc, as a function of the universal baryon fraction, f_b . We compute the median of this ratio in two mass bins for matched haloes in five simulations varying only the universal baryon fraction, with binning based on the central ($\Delta f_b = 0$) simulation. We find that the mass scales as $M_{\text{BH}} c^2 \propto f_b^2 E_{\text{grav}}$.

parameter V_g . We assume that

$$V_g = \sqrt{E_{\text{AGN}}/M_b} = \sqrt{f_b GM/R}, \quad (13)$$

where we used equations (10–12). This is consistent with results from the EAGLE and IllustrisTNG simulations (Nelson et al. 2019; Mitchell et al. 2020), which show that black hole outflows have a velocity distribution that peaks at a characteristic velocity, V_g , that increases with mass. The fraction of the gas at radius r that escapes the halo corresponds to the fraction with a velocity that exceeds the escape velocity,

$$V_{\text{esc}} \approx V_{\text{max}} \sqrt{\frac{2 \log(1 + 2r/R_{\text{max}})}{r/R_{\text{max}}}} \approx 2V_{\text{max}}, \quad (14)$$

where R_{max} is the radius where the circular velocity is V_{max} , the expression holds for a Navarro–Frenk–White (NFW) profile (Klypin & Holtzman 1997; Navarro et al. 1997), and we assumed that $r \ll R_{\text{max}}$ in the second step. The factor multiplying V_{max} , given by the square root, is not very sensitive to r . Hence, the escape fraction is approximately

$$f_{\text{esc}} = \int_{2V_{\text{max}}}^{\infty} dv' f(v'/V_g) = f_{\text{esc}}(\xi), \quad (15)$$

where upon evaluation, using dimensional arguments, we write the integral as an arbitrary function of the ratio

$$\xi \equiv \frac{V_g}{V_{\text{max}}} = \frac{\sqrt{f_b GM/R}}{V_{\text{max}}} = \frac{\sqrt{f_b}}{c_v}. \quad (16)$$

Notice that the non-linear scaling of the black hole mass, $M_{\text{BH}} \propto f_b^n$, was important, since f_b would have dropped out if $n = 1$, as assumed by earlier works. In general, repeating the calculation for arbitrary n , we predict that f_{esc} should be a function of $f_b^{(n-1)/2} c_v^{-1}$. The scaling $M_{\text{BH}} \propto f_b^2$ should be confirmed with other simulations and feedback models. Moreover, the scaling should be confronted with observational lines of evidence. One possibility is to make use of the fact that baryons are not exact tracers of the dark matter even at early times (Angulo, Hahn & Abel 2013), giving rise to spatial variations in the baryon fraction and therefore perhaps spatial variations in the strength of feedback.

Let us now see how the full model compares against the simulations. For each of the cosmological model variations described in Sec-

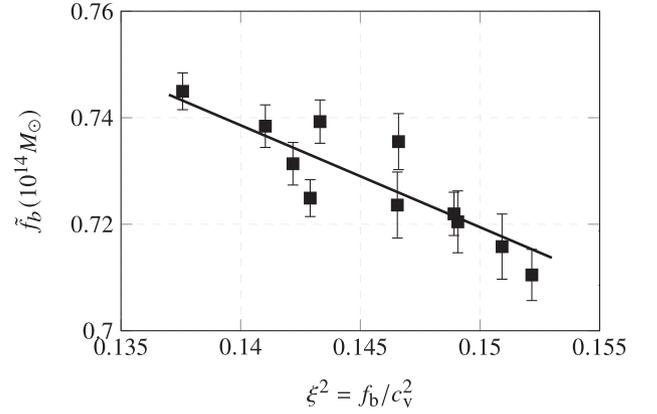


Figure 4. A fit of renormalized baryon fractions, $\tilde{f}_b = f_{b,200c}/f_b$, where $f_{b,200c}$ is the baryon fraction within R_{200c} for matched haloes with a mass of $M_{200c} = 10^{14} M_{\odot}$ and f_b is the universal baryon fraction, as a function of the cosmological parameter combination $\xi^2 = f_b/c_v^2$. The baryon fractions are evaluated at the pivot mass, $10^{14} M_{\odot}$, using the power-law fits of equation (18).

tion 2.2, we take the median of the concentration, $c_v = V_{\text{max}}/V_{200c}$, for haloes with masses M_{200c} in the range $10^{14 \pm 0.25} M_{\odot}$ from the gravity-only simulations. We compute the universal baryon fraction, $f_b = \Omega_b/(\Omega_b + \Omega_c)$, directly from the cosmological parameters. These two quantities give the cosmological parameter combination $\xi = \sqrt{f_b}/c_v$. Determining the escape fractions is more complicated because of the limited volume and the stochasticity of the hydrodynamical simulations. To get a statistically significant relationship, we again rely on pairs of haloes matched between the fiducial cosmology and the variations. For each halo, we compute renormalized baryon fractions,

$$\tilde{f}_b = \frac{f_{b,200c}}{f_b}, \quad (17)$$

where $f_{b,200c}$ is the baryon fraction within R_{200c} and f_b is the universal baryon fraction. In the mass range of interest, $10^{13.25} < M_{200c}/M_{\odot} < 10^{14.5}$, we fit a power-law relationship

$$\tilde{f}_b(M_{200c}) = a \left(\frac{M_{200c}}{10^{14} M_{\odot}} \right)^b, \quad (18)$$

in terms of the free parameters a and b , and evaluate \tilde{f}_b at the pivot mass, $10^{14} M_{\odot}$. Plots of these fits are shown in Fig. B1. In Fig. 4, we show a fit of \tilde{f}_b in terms of ξ^2 ,

$$\tilde{f}_b = 1 - f_{\text{esc}} = c + d\xi^2, \quad (19)$$

where c and d are free parameters. We find that $d < 0$. Given that $\xi^2 = f_b/c_v^2$, this is consistent with the expectation that the escape fraction increases with the universal baryon fraction, f_b , and decreases with the binding energies of haloes. In the next section, we will use this model to predict the non-factorizable corrections to the matter power spectrum.

3.4 Fitting function for the non-factorizable corrections to the matter power spectrum

The baryon fraction in groups can be related to the suppression of the matter power spectrum (e.g. Semboloni, Hoekstra & Schaye 2013; Debackere et al. 2020; van Daalen et al. 2020; Salcido et al. 2023; van Loon & van Daalen 2024). At any fixed wavenumber k , the suppression of the power spectrum is well described by an

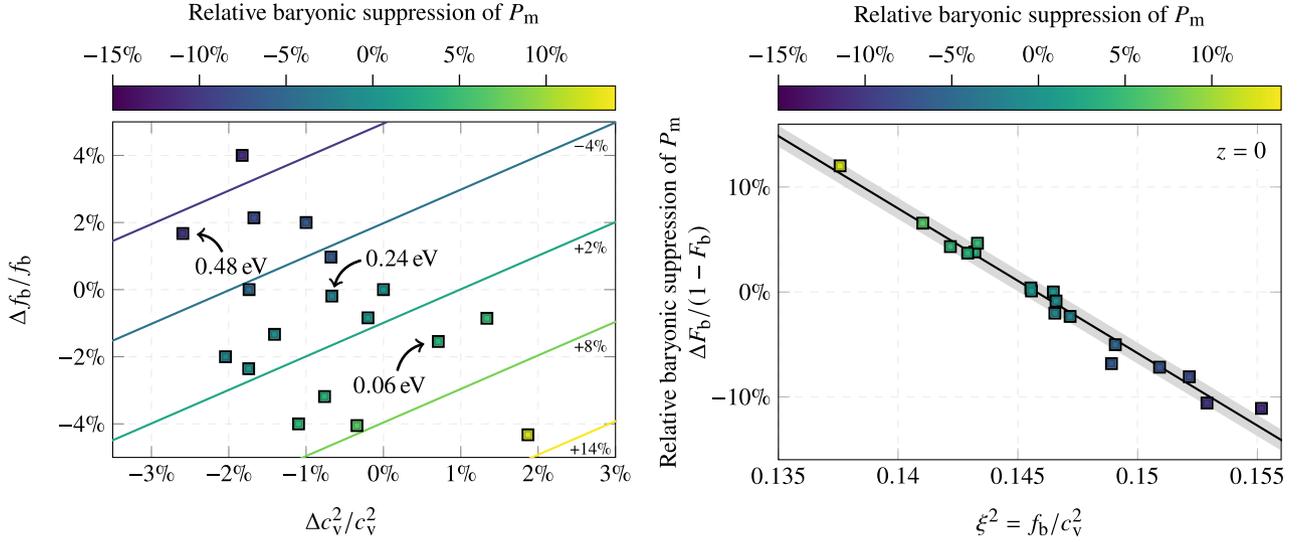


Figure 5. The non-factorizable correction to the power spectrum as a function of the changes in baryon fraction, f_b , and gravity-only halo concentration, c_v . The points are based on FLAMINGO simulations with side lengths $L = 1$ Gpc and $L = 0.2$ Gpc, shown relative to the fiducial L1_m9 model at $(\Delta c_v^2, \Delta f_b) = (0, 0)$. The arrows on the left indicate three models that only differ in the assumed neutrino mass sum of $\sum m_\nu = 0.06, 0.24$, or 0.48 eV. The right-hand panel shows that equation (22) provides an excellent fit, explaining the correction to the power spectrum in terms of $\xi^2 = f_b/c_v^2$. The grey band represents a ± 1 per cent error in the relative suppression of the power spectrum, implying an even smaller error in $P_m(k)$.

exponential fit of the form:

$$F_b = \frac{P_m^{\text{hydro}}}{P_m^{\text{DMO}}} = 1 - \exp(e \tilde{f}_b + g), \quad (20)$$

with the free parameters e and g .⁸ Combining this with equation (19), we find that the suppression of the power spectrum should depend on cosmology as

$$F_b = 1 - \exp(\alpha \xi^2 + \beta) = 1 - \exp\left(\alpha \frac{f_b}{c_v^2} + \beta\right), \quad (21)$$

where $\alpha = de$ and $\beta = g + ce$. Going forward, we will simply consider α as a free parameter and fit the model to the power spectra in the simulations, expanding equation (21) to first-order and writing the change in baryonic suppression relative to the fiducial case as

$$\frac{\Delta F_b}{1 - F_b} = -\alpha \Delta(\xi^2), \quad (22)$$

Here, $\Delta F_b = F_b - F_b^{\text{fid}}$, such that $\Delta F_b > 0$ corresponds to weaker feedback and therefore greater $P(k)$. For each model variation, we compute the average baryonic suppression of the power spectrum, F_b , in the range between $0.1 h \text{ Mpc}^{-1} \leq k \leq 10 h \text{ Mpc}^{-1}$ at $z = 0$. The median concentration, c_v , and universal baryon fraction, f_b , are determined as in the previous section. Fitting model (22) to the simulations yields $\alpha = 13.8 \pm 0.6$.

The left panel of Fig. 5 shows the relative change in the baryonic suppression, $\Delta F_b/(1 - F_b)$, in the plane of f_b and c_v . The contour lines indicate the level sets of ΔF_b . As expected, an increase in the universal baryon fraction leads to a greater baryonic suppression, while an increase in the halo concentration leads to a smaller suppression. From the slope of the contour lines, we see that the logarithmic slope of F_b with respect to f_b is approximately equal to the logarithmic slope with respect to $1/c_v^2$, consistent with

⁸This does not imply that two parameters are needed per k -bin. On large scales, $F_b(k, \tilde{f}_b)$ can be fitted with five free parameters (van Daalen et al. 2020).

equation (21). Three simulations, which differ only in the assumed neutrino mass sum of $\sum m_\nu = 0.06, 0.24$, and 0.48 eV, are marked in Fig. 5. The vector between these models makes a large angle with the contour lines, implying a significant change in baryonic suppression. The non-factorizable correction between these models is large for two reasons. First of all, haloes are less concentrated in the large neutrino mass cosmology because the matter density is lower when haloes collapse. Secondly, more gas is available for haloes of a given dark matter mass, because neutrinos cluster less effectively on small scales, such that haloes are primarily composed of CDM and baryons, of which baryons make up a larger fraction. Both changes increase the potency of feedback. This explains why, among the original five cosmology variations in the FLAMINGO suite (Schaye et al. 2023), the non-factorizable correction between these models is largest.

Much the same is true for the decaying dark matter simulations, but to an even greater extent. For these models, the baryon fraction increases over time as dark matter decays. To interpret the suppression of the power spectrum in terms of $\xi^2 = f_b/c_v^2$, we choose to evaluate f_b at $z = 0$, since we do the same for c_v . Comparing the *Planck* simulations with decay rates of $\Gamma = 12 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $24 \text{ km s}^{-1} \text{ Mpc}^{-1}$ to the fiducial cosmology without decays, we find changes in the baryon fraction of $\Delta f_b/f_b = 15$ per cent and 30 per cent, respectively, while the square of the median halo concentration changes by $\Delta c_v^2/c_v^2 = -6$ per cent and -11 per cent, respectively. Given that these points are far outside the parameter ranges of Fig. 5, we provide a separate plot with the decaying dark matter simulations in Fig. B2. As expected, the baryonic suppression in these models is far stronger. This will be discussed further in the next section and in Appendix B

The right-hand panel of Fig. 5 shows that equation (22) provides an excellent fit, giving the relative baryonic suppression, $\Delta F_b/(1 - F_b)$, as a function of $\xi^2 = f_b/c_v^2$ to a relative accuracy of about 1 per cent, implying an even greater absolute accuracy in P_m . Although we focus on the suppression at $z = 0$ in this paper, the same general trends

with respect to f_b and c_v remain true at higher redshifts. We will briefly revisit the time dependence in Section 4.3, but leave a detailed treatment for future work.

4 COSMOLOGICAL IMPLICATIONS

One issue that has received significant attention in recent years is the tension between different measurements of the $S_8 = (\Omega_m/0.3)^{1/2} \sigma_8$ parameter. The values obtained from various large-scale structure probes have been found to be lower than the Λ CDM expectation based on measurements of the CMB. In particular, weak lensing surveys such as the Kilo-Degree Survey (KiDS; Kuijken et al. 2015) and Dark Energy Survey (DES; Abbott et al. 2016) have reported measurements that are 5 per cent \sim 10 per cent lower than that of *Planck* (Aghanim et al. 2020) with a statistical significance of $2 \sim 3\sigma$ (Asgari et al. 2021; Amon et al. 2022; Abbott et al. 2023). It has long been recognized that baryonic processes, in particular feedback from AGNs, are relevant for the interpretation of weak lensing observations (e.g. Semboloni et al. 2011; van Daalen et al. 2011). As such, large-scale structure analyses usually take the impact of baryons into account, either by marginalizing over some parametrization of feedback or by excluding small-scale clustering where the impact of baryons is thought to be largest. However, Amon & Efstathiou (2022) and Preston, Amon & Efstathiou (2023) have recently argued that lensing- and CMB-based measurements of S_8 can be reconciled by adopting a baryonic feedback model that is significantly stronger than what is predicted by hydrodynamical simulations and X-ray observations of clusters. That such a solution is not feasible is confirmed by results from the new FLAMINGO suite (McCarthy et al. 2023), which suggest that baryonic effects are too small even when allowing for large uncertainties in the observed cluster gas fractions and theoretical modelling. While we focus on weak lensing in this paper, they also showed that other probes, such as the thermal tSZ effect, exhibit large tensions not reconcilable with baryonic feedback alone.

Setting aside the impact of baryons, the S_8 tension could also be interpreted as a hint of new physics that suppresses the growth of cosmic structure at late times. Such a modification of the concordance model must simultaneously be large enough to reconcile large differences in power spectra at low redshifts, without distorting the tightly constrained expansion history or the clustering at higher redshifts and larger scales effectively probed by CMB lensing. Adding to the difficulty is the fact that solutions to the S_8 tension often exacerbate the H_0 tension and vice versa (e.g. Pandey, Karwal & Das 2020; Vagnozzi 2023). Given the coupling between baryonic feedback and cosmology discussed in this paper, it is worth considering whether a combination of baryonic and non-baryonic suppression mechanisms could work together, obviating the need for extreme versions of either mechanism alone. This will be discussed in the following sections. First, in Section 4.1, we will determine the cosmological parameter ranges within which a feedback model calibrated assuming a fiducial *Planck* cosmology can be reliably applied. Then, in Section 4.2, we will consider the implications for extensions of Λ CDM aimed at resolving the S_8 tension. Finally, we will look at the extent to which cosmological and astrophysical parameters are degenerate in Section 4.3.

4.1 Parameter dependence

To quantify the variations in baryonic feedback that accompany variations in cosmology, we must first express equation (22) in terms of standard cosmological parameters. Using the Λ CDM simulations

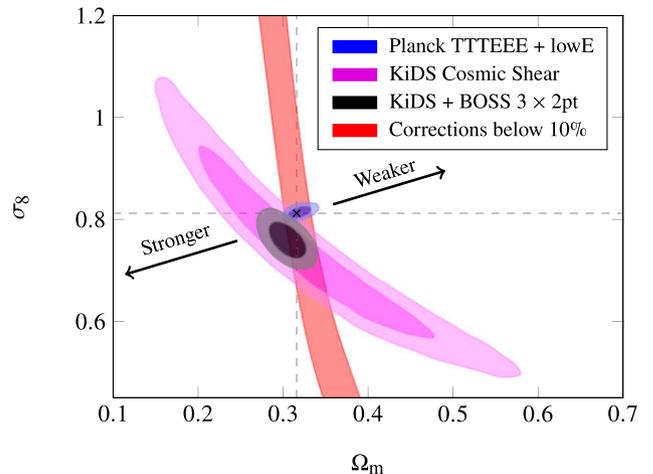


Figure 6. The cosmological parameters for which the baryonic suppression of matter clustering is similar to that in the best-fitting *Planck* model. This corresponds to the range where absolute errors to the matter power spectrum are $\lesssim 1$ per cent, or more precisely where relative non-factorizable corrections, $\Delta F_b/(1 - F_b)$, are below 10 per cent on scales $0.1 h \text{ Mpc}^{-1} \leq k \leq 10 h \text{ Mpc}^{-1}$ at $z = 0$. The arrows indicate where baryonic feedback is at least 10 per cent stronger than in the *Planck* model (lower σ_8 and Ω_m) and weaker (vice versa). This is to be compared with the marginal posteriors from KiDS-1000, KiDS + BOSS + 2dFLenS, and *Planck* TTTEEE + lowE.

described in Section 2.2, we obtain a fit for our velocity-based definition of halo concentration, for haloes with masses $M_{200c} = 10^{14 \pm 0.25} M_\odot$, in terms of Ω_m and σ_8 ,

$$c_v = 1.24(\Omega_m \sigma_8)^{1/8}, \quad (23)$$

which is in line with the expectation that cosmological model variations that reduce the strength of clustering lead to less concentrated haloes, although the dependence is relatively weak. We show the scatter around this relationship in Fig. B3. Substituting this expression into equation (22), we obtain

$$\frac{\Delta F_b}{1 - F_b} = -\alpha' \Delta \left[\frac{\Omega_b}{\Omega_b + \Omega_c} (\Omega_m \sigma_8)^{-1/4} \right], \quad (24)$$

where $\alpha' = 0.65\alpha = 8.98$. This expression gives the relative change in the baryonic suppression of the matter power spectrum, averaged over the range $0.1 h \text{ Mpc}^{-1} < k < 10 h \text{ Mpc}^{-1}$ at $z = 0$. To simplify matters further, we observe that external constraints on the baryon density, $\Omega_b h^2$, from Big Bang Nucleosynthesis (Adelberger et al. 2011; Cooke, Pettini & Steidel 2018) are much stronger than external constraints on the dark matter density, $\Omega_c h^2$, justifying a much stronger prior on $\Omega_b h^2$. It follows that the baryon fraction, $f_b = \Omega_b/(\Omega_b + \Omega_c)$, is strongly anticorrelated with the total matter density, Ω_m , in cosmic shear analyses (as it is for *Planck*). Computing the marginal expectation value, $f_b(\Omega_m)$, from the 3×2 pt chains of Heymans et al. (2021), based on data from KiDS, the Baryon Oscillation Spectroscopic Survey (BOSS) and the 2-degree Field Lensing Survey (2dFLenS), we can express ΔF_b entirely in terms of Ω_m and σ_8 . We obtain very similar results when using the marginal expectation $f_b(\Omega_m)$ from the *Planck* TTTEEE + lowE chains (Aghanim et al. 2020).

Having eliminated Ω_b , we compute the parameter ranges around the best-fitting *Planck* model, marked by a cross in Fig. 6, for which the relative corrections, $\Delta F_b/(1 - F_b)$, are below 10 per cent. The result is shown by the red contours in the figure. They are slightly

tilted from vertical, reflecting the importance of the baryon fraction, f_b , while the dependence on σ_8 through the halo concentration (23) is weaker. The importance of the baryon fraction is not surprising and has been noted previously (Schneider et al. 2020; van Daalen et al. 2020; Aricò et al. 2021; Mead et al. 2021). The secondary dependence on σ_8 is also consistent with Aricò et al. (2021), who used a baryonification algorithm to explore the dependence of feedback on cosmology.⁹ Also shown in Fig. 6 are the constraints from *Planck* temperature and polarization data in blue, the KiDS-1000 weak lensing constraints in purple, and the KiDS + BOSS + 2dFLenS 3×2 pt constraints in black. The figure shows that relative non-factorizable corrections are mostly below 10 per cent (which implies absolute corrections to the power spectrum below 1 per cent) if one restricts to the 68 per cent *Planck* constraints. However, it is not possible to sample a parameter space that covers both the constraints from *Planck* and large-scale structure surveys like KiDS with 1 per cent absolute precision unless non-factorizable corrections are taken into account.

Another interesting observation is that baryonic effects are enhanced for lower σ_8 (decreasing the binding energies of haloes) and lower Ω_m (both decreasing binding energies and increasing the baryon fraction). This is precisely the direction of the tension. Hence, new physics that involves lowering the density of matter or the amplitude of its clustering at late times also tends to increase the strength of feedback, and possibly more so than variations in standard cosmological parameters. We will explore this idea in the next section.

4.2 Model building

Within the Λ CDM model, a smaller lensing signal translates into a preference for reduced matter clustering. Although baryonic feedback does produce such an effect, the FLAMINGO model predicts that this is too small to reconcile all observations (McCarthy et al. 2023). One way to illustrate this is to show matter power spectra relative to the power spectrum for a ‘CMB cosmology’ without baryonic feedback. We do just that in Fig. 7. The grey contours represent the 68 per cent and 95 per cent intervals of Λ CDM power spectra allowed by the 3×2 pt KiDS + BOSS + 2dFLenS analysis (Heymans et al. 2021), including the effects of baryonic feedback (parametrized with the HMCODE method of Mead et al. 2015; see Section 5), relative to the gravity-only FLAMINGO simulation with the best-fitting values from *Planck* (Aghanim et al. 2020). This is computed by marginalizing over all cosmological, baryonic feedback, and nuisance parameters taken from the public chains. The black line shows the effect of turning on baryonic feedback in the *Planck* cosmology, assuming the fiducial FLAMINGO parameters. Consistent with the headline result of a $\sim 3\sigma$ tension in S_8 reported in Heymans et al. (2021), the discrepancy still exceeds 2σ on scales $0.1 h \text{ Mpc}^{-1} < k < 10 h \text{ Mpc}^{-1}$. It is worth noting that the KiDS + BOSS + 2dFLenS results plotted in Fig. 7 are more extreme than those of DES-Y3 (Abbott et al. 2022, 2023), which are intermediate between KiDS and *Planck*.

One way to reconcile weak lensing and CMB observations is by introducing new physics that slows the growth of structure at late

⁹In the baryonification algorithm, feedback is accounted for by displacing particles according to a recipe with a number of parameters. In Aricò et al. (2021), the cosmological coupling is analysed with parameters tuned to hydrodynamical simulations. Hence, the conclusions are not entirely independent.

times. Two well-motivated extensions of the Standard Model that have been considered in this context are massive neutrinos (Battye & Moss 2014; Wyman et al. 2014; McCarthy et al. 2018) and decaying dark matter (Aoyama et al. 2014; Berezhiani et al. 2015; Enqvist et al. 2015; Pandey et al. 2020; Abellán, Murgia & Poulin 2021; Tanimura et al. 2023). Both models slow the growth of structure and increase the density of baryons relative to the matter that clusters efficiently. Based on the preceding discussion and that in Section 3.4, we conclude that both extensions will therefore also enhance the strength of baryonic feedback, further boosting the overall suppression of matter clustering.

To see this more clearly, we show the effect of increasing the neutrino mass from $\sum m_\nu = 0.06 \text{ eV}$ for the fiducial *Planck* cosmology to $\sum m_\nu = 0.24$ (blue) or 0.48 eV (red) on the left-hand side of Fig. 7. The dashed lines indicate the effect that would result if baryonic feedback were independent of cosmological parameters, while the solid lines indicate the results obtained from the simulations. The bottom panel shows that the non-factorizable corrections are modest, with effects of 1 per cent – 2 per cent for $k > 2 h \text{ Mpc}^{-1}$, relative to the case without cosmological dependence, while also confirming that the suppression is indeed greater than in the case with minimal neutrino masses, $\sum m_\nu = 0.06 \text{ eV}$. This agrees with the prior findings of Mummery et al. (2017) obtained with the BAHAMAS simulations. It also explicitly confirms the finding in Section 4.1 that non-factorizable corrections exceed 1 per cent when moving from the best-fitting *Planck* model to a model preferred by large-scale structure surveys. It is striking to see that the $0.24 - 0.48 \text{ eV}$ simulations straddle the 1σ constraints from KiDS + BOSS + 2dFLenS. This is consistent with earlier studies attempting to reconcile lensing and CMB observations with neutrinos (Battye & Moss 2014; Wyman et al. 2014; McCarthy et al. 2018). However, such a solution is strongly challenged by geometric constraints obtained from the combination of CMB and BAO data (e.g. Vagnozzi et al. 2017; Aghanim et al. 2020; Brieden, Gil-Marín & Verde 2022; Tristram et al. 2023),¹⁰ the Lyman- α forest (Palanque-DeLabrouille et al. 2020), and to a much lesser extent by CMB lensing (Aghanim et al. 2020).

For decaying dark matter, the effect on baryonic feedback is much stronger. This is shown on the right-hand side of Fig. 7, for decay rates of $\Gamma = 12 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (blue) and $24 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (red). Dashed lines again indicate the predictions without dependence on cosmology, while solid lines show the simulated results. The non-factorizable corrections are now 5 per cent – 10 per cent on non-linear scales, essentially doubling the strength of feedback in the most extreme case relative to the model without decaying dark matter. This shows that the assumption made in Hubert et al. (2021) that baryonic feedback is not affected by dark matter decay is not a good approximation. It is interesting to note that decaying dark matter and warm dark matter are fundamentally different in this regard, since the factorizability approximation is more accurate for warm dark matter (Paribelli et al. 2021). Compared to the neutrino models, the scale dependence of the combined baryonic and non-baryonic effect is less consistent with the 3×2 pt constraints, although the models do provide a better fit than the *Planck* model with baryons alone. However, as in the case of massive neutrinos, geometric considerations also seem to rule out this solution (e.g. Audren et al. 2014; Aubourg et al. 2015). The non-factorizable corrections may also lead to violations of astrophysical constraints, such as cluster

¹⁰In fact, the Planckv0.24Fix simulation shown in Fig. 7 is also ruled out by *Planck* alone, since the remaining cosmological parameters are not adjusted.

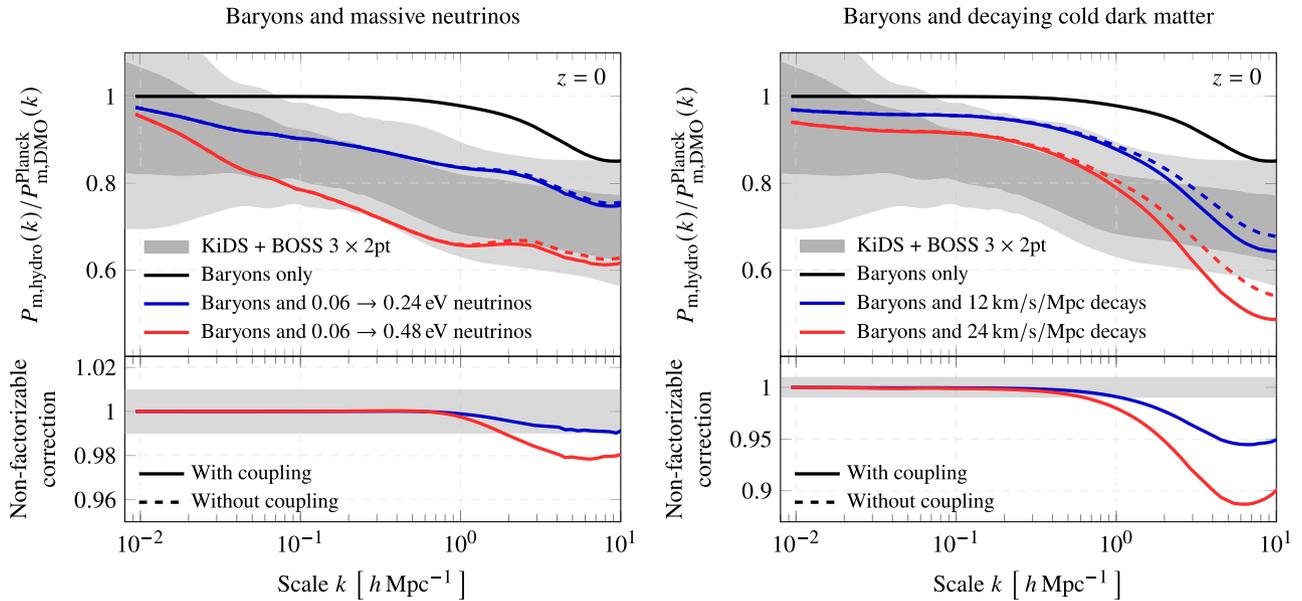


Figure 7. Matter power spectra relative to the spectrum for a *Planck*-based Λ CDM cosmology (Aghanim et al. 2020) without baryonic effects. The shaded contours in the top panel show the 68 per cent and 95 per cent ranges of Λ CDM spectra obtained from the 3×2 pt KiDS + BOSS + 2dFLenS analysis (Heymans et al. 2021), which include the effects of baryonic feedback by marginalizing over a halo model-based feedback parameter (Mead et al. 2015; see Section 5). The left panel shows the effects of baryons alone and the effects of baryons combined with changing the neutrino mass from $\sum m_\nu = 0.06$ to 0.24 eV or 0.48 eV. The solid lines represent the simulation results, while the dashed lines show the results without accounting for the cosmology dependence of baryonic feedback. The right panel shows the same for decaying cold dark matter (DCDM) models with decay rates of $\Gamma = 12 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $24 \text{ km s}^{-1} \text{ Mpc}^{-1}$. The bottom panels show the non-factorizable corrections, i.e. the ratios of the solid and dashed curves in the top panels, with shaded bars representing a 1 per cent error.

gas fractions. If this is the case, it could be another reason to exclude decaying dark matter as a viable solution. However, as mentioned in the introduction, turning baryonic feedback into a cosmological probe is only possible if the degeneracy between astrophysical and cosmological parameters could be broken. We will return to this issue shortly.

The decaying dark matter model studied in this paper is perhaps only the simplest, so it is worth considering other types of behaviour. Whereas all dark matter decays at a constant and universal rate in this model, the rate may depend on the density and velocity dispersion of dark matter, as in certain models with annihilating dark matter (Choquette, Cline & Cornell 2016). For such models, the effect would be most pronounced in the centres of massive haloes, which we speculate would lead to even greater non-factorizable corrections, given the importance of the central density of groups and clusters for AGN feedback. Two-body dark matter decay, in which a less massive daughter dark matter particle receives a small recoil velocity, would heat or disrupt dark matter haloes and lower their concentrations (Peter 2010; Peter, Moody & Kamionkowski 2010; Cheng, Chu & Tang 2015; Franco Abellán et al. 2022), likely further enhancing baryonic feedback. On the other hand, interactions between dark matter and dark energy may either boost or suppress the halo concentration (Li & Barrow 2011; Baldi & Simpson 2017; An et al. 2019; Liu et al. 2022), with uncertain effects on feedback.

4.3 Degeneracies

Given these findings, a further question is whether the cosmological dependence of baryonic feedback is degenerate with the astrophysical parameters of the model, which were kept fixed in

all cosmological model variations considered so far.¹¹ There is some indication that this may not be the case. In the left panel of Fig. 8, we show the change in baryonic suppression (the non-factorizable correction) at $z = 0$ when setting the dark matter decay rate to $\Gamma = 12 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (blue) or $24 \text{ km s}^{-1} \text{ Mpc}^{-1}$ (red), whilst keeping the feedback parameters fixed, together with two variations in subgrid model at fixed cosmology. The two astrophysics variations, listed as L1_m9- $f_{\text{gas}} - 2\sigma$ and L1_m9- $f_{\text{gas}} - 4\sigma$ in Table 1, were calibrated to achieve systematically lower cluster gas fractions, either 2σ (dashed grey) or 4σ (dashed black) below the observational data. These shifts primarily alter the AGN parameters of the model, although the SN parameters are varied as well (Kugel et al. 2023). We see that the astrophysical parameters have a very similar effect as the dark matter lifetime up to about $k \approx 1 \text{ h Mpc}^{-1}$ at $z = 0$, but that the effect of the lifetime is much stronger on smaller scales. This finding applies not just to the dark matter lifetime, but also to shifts in other cosmological parameters, as we will show below. Moreover, the effects of cosmological and astrophysical parameters also diverge over time. The right panel of Fig. 8 shows that the cosmological coupling is much weaker at $z = 1$, relative to the impact of the astrophysical parameters. Hence, the degeneracy may be broken by considering the scale and time dependence of the baryonic suppression. While encouraging, baryonic processes are complex and by no means exhaustively described by the f_{gas} variations in the FLAMINGO suite. Hence, further work is needed to disentangle the effects of cosmology and astrophysics.

¹¹We stress the difference between the factorizability of two processes (i.e. that they can be treated independently) and their degeneracy (i.e. that they have identical effects on some observable).

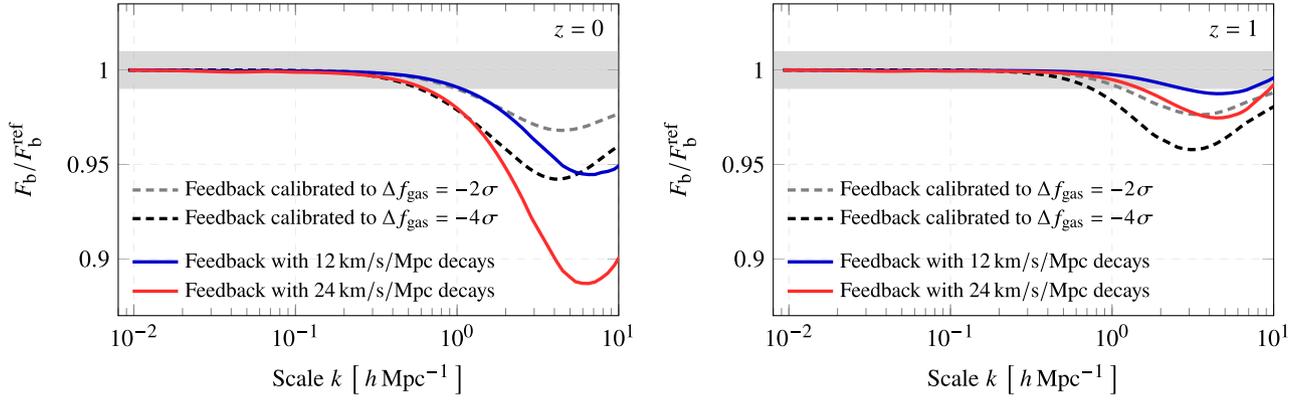


Figure 8. Ratios of the baryonic suppression of the power spectrum, relative to the fiducial case without decaying dark matter and with feedback parameters calibrated to observed cluster gas fractions, for models with different dark matter decay rates but equal subgrid parameters (solid curves) and for models without decaying dark matter but subgrid parameters calibrated to systematically lower cluster gas fractions (dashed curves). The two types of parameters have different time- and scale-dependent effects. The cosmological coupling becomes more important on small scales ($k \geq 1 h \text{ Mpc}^{-1}$) and at late times ($z < 1$).

5 HALO MODEL APPROACHES

Baryonic effects are often included in cosmic shear analyses using approximate prescriptions that do not fully capture the dependence on cosmological parameters, with the result that feedback parameters encode both cosmological and astrophysical information. To illustrate the consequences, we will consider in Section 5.1 the commonly used and simplest version of the halo model approach of Mead et al. (2015), as implemented in HMCODE and used in the KiDS-1000 analysis of Asgari et al. (2021). In Section 5.2, we will turn to a more sophisticated version that has been released since (Mead et al. 2021). This version provides a clear improvement, but still does not fully capture the cosmological coupling discussed in this paper.

5.1 Comparison with HMCODE

Let us briefly review the basic HMCODE approach, while referring to Asgari, Mead & Heymans (2023) for a more comprehensive overview. In the halo model, the matter power spectrum is written as the sum

$$P_{\text{m}}(k) = P_{2\text{h}}(k) + P_{1\text{h}}(k), \quad (25)$$

where the ‘2-halo’ term, $P_{2\text{h}}(k)$, describes the variance in the mass-weighted density of haloes and the ‘1-halo’ term, $P_{1\text{h}}(k)$, describes the variance in the mass-density of matter within haloes. The model has a number of free parameters affecting both terms, but baryonic effects only impact the 1-halo term in this model. The 1-halo term is given by an integral over halo masses,

$$P_{1\text{h}}(k) = \frac{1}{\bar{\rho}^2} \int_0^\infty M^2 \bar{\rho}^2(k, M) F(M) dM, \quad (26)$$

where $\bar{\rho}$ is the mean density of matter, $\bar{\rho}(k, M)$ is the normalized Fourier transform of the density profile of a halo of mass M , and $F(M)$ is the halo mass function. In HMCODE, the halo density profile is given by a modified NFW form (Navarro et al. 1997). The impact of baryons on $\bar{\rho}$ is captured by two free parameters: A and η_0 . The first parameter, A , is a normalization of the relation between the concentration, c , of a halo and its mass, M , at redshift z :

$$c(M, z) = A \frac{1 + z_f}{1 + z}, \quad (27)$$

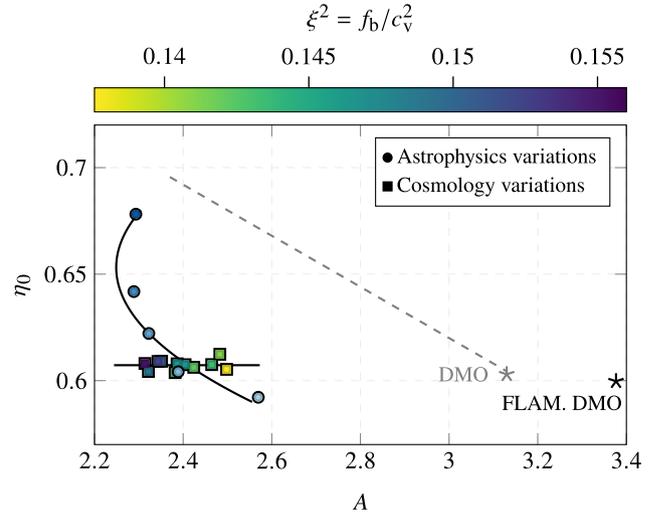


Figure 9. Best-fitting values of the two parameters, A and η_0 , used in the HM-CODE model to describe the effect of baryons on the matter power spectrum, obtained by fitting the model to the suppression of the power spectrum in the FLAMINGO simulations. The circles correspond to simulations that vary astrophysical parameters at fixed cosmology, while the squares correspond to simulations that vary cosmological parameters with fixed subgrid parameters. The lighter star labelled DMO marks the parameters in the absence of baryonic effects and the grey dashed line is a fit, $\eta_0 = 0.98 - 0.12A$, from Joudaki et al. (2018) to feedback variations from the OWLS suite (Schaye et al. 2010). The darker star marks the best-fitting parameters for the fiducial gravity-only FLAMINGO simulation.

where z_f is the formation redshift of the halo. The second parameter, η_0 , describes a mass-dependent modification of the density profile,

$$\bar{\rho}(k, M) \rightarrow \bar{\rho}(v^\eta k, M), \quad (28)$$

where $\eta = \eta_0 - 0.3\sigma_8(z)$ and $v = \delta_c/\sigma(M)$ is the peak height in terms of the linear-theory collapse threshold, $\delta_c \approx 1.686$, and the standard deviation of the linear matter density field, $\sigma(M)$, in spheres of radius $(3M/4\pi\bar{\rho})^{1/3}$. Fitting the model to power spectra from dark matter only simulations, Mead et al. (2015) determined best-fitting values of $(A, \eta_0) = (3.13, 0.603)$ in the absence of baryonic effects. This point is marked by a grey star labelled DMO in Fig. 9. Doing the same for power spectra measured from hydrodynamical simulations

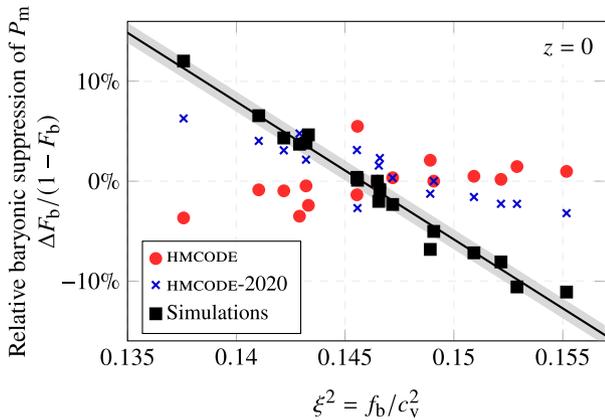


Figure 10. Non-factorizable corrections to the power spectrum at $z = 0$, relative to the fiducial L1_m9 model, measured from the FLAMINGO simulations (squares), and computed with HMCODE (circles), and HMCODE-2020 (crosses). The FLAMINGO points are the same as in the right-hand panel of Fig. 5.

from the OWLS suite (Schaye et al. 2010), they obtained a range of parameters for different feedback scenarios. To eliminate one degree of freedom, Joudaki et al. (2018) and Asgari et al. (2021) exploited the correlation between η_0 and A in the best-fitting OWLS parameters and used a linear fit, $\eta_0 = 0.98 - 0.12A$, in their cosmic shear analyses. This relation is shown as the grey dashed line in Fig. 9.

One of the advantages of the halo model approach is that it automatically captures some of the ways in which baryonic feedback could be coupled with cosmological parameters, namely through changes in the halo mass function, $F(M)$, or halo formation epochs, z_f . However, the halo model does not capture the cosmology dependence of baryonic processes inside the galaxy. We have shown in preceding sections that this coupling causes properties like the masses of supermassive black holes (equation 12 and Fig. 3) or gas escape fractions (equation 19 and Fig. 4) to depend on cosmological parameters.

To demonstrate the impact, we fit the model to the baryonic suppression, $F_b(k)$, in our fiducial simulation (L1_m9) with A and η_0 as free parameters. We fit to the data at $z = 0$ and use the implementation of HMCODE in CLASS. We then fix A and η_0 at these best-fitting values and use HMCODE to compute the non-factorizable corrections, $\Delta F_b/(1 - F_b)$, relative to the fiducial model, when the cosmological parameters are changed to those of the Λ CDM simulations discussed in Section 2.2 and those listed in Table 1. The average corrections, on scales $0.1 h \text{ Mpc}^{-1} \leq k \leq 10 h \text{ Mpc}^{-1}$, are shown in red in Fig. 10, along with the corrections computed from the FLAMINGO simulations in black. We see that the cosmological coupling is much smaller in HMCODE than in the simulations and, unlike for the simulations, there is no clear trend with respect to ξ^2 . The agreement with the simulations is better for the more recent implementation, HMCODE-2020, as will be discussed below.

Since HMCODE does not fully capture the non-factorizable corrections seen in the simulations, the baryonic parameters A and η_0 must depend on cosmological parameters. To demonstrate this, we fit the model to $F_b(k)$ and obtain the best-fitting values of A and η_0 for all of our simulations. The results are shown in Fig. 9, where the coloured squares correspond to the cosmology variations discussed in Section 2.2 and the blue circles correspond to the astrophysics variations L1_m9- $f_{\text{gas}} \pm n\sigma$ listed in Table 1. These astrophysics

variations have subgrid physics parameters calibrated to cluster gas fractions that are $n\sigma$ higher or lower than the observed data (Kugel et al. 2023), but all assume the fiducial cosmology. Interestingly, the two types of variations appear to have different effects on η_0 and A , with η_0 being essentially independent of cosmology but quite sensitive to shifts in astrophysical parameters. This can be understood in terms of a difference in scales: η_0 affects the suppression on larger scales, while A is more important on smaller scales. The finding that the cosmological coupling is more important on small scales agrees with what was seen in Section 4.3 for the decaying dark matter models. We note that HMCODE treats A and η_0 as free parameters that are chosen to match the power spectrum, rather than the actual halo concentrations and density profiles in simulations. Hence, the dependence of A on cosmological parameters cannot be interpreted directly in terms of the halo concentration. Instead, the figure demonstrates that A depends on the combination $\xi^2 = f_b/c_v^2$.

Next, let us compare the astrophysics variations on the FLAMINGO suite with the grey dashed line, which corresponds to the linear fit based on simulations from the OWLS suite (Schaye et al. 2010). In both cases, η_0 increases and A generally decreases with the strength of baryonic feedback. However, the detailed behaviour is very different. For the same value of A , we find a smaller suppression and hence a smaller value of η_0 for the FLAMINGO simulations. This shows that a 1-parameter model is not sufficiently flexible to describe the baryonic suppression in general. Moreover, some cosmological information is lost when marginalizing over feedback parameters without fully modelling the cosmological coupling.

To mitigate these limitations, one could adopt more flexible modelling approaches that include the dependence on cosmology. For instance, one could incorporate equation (21) into existing approximate prescriptions. As a first attempt, let us demonstrate how this could be done for the basic version of HMCODE. Let \bar{A} and $\bar{\eta}_0$ be the parameters that describe feedback for some fixed cosmology. Combining a quadratic fit, $\bar{A}(\bar{\eta}_0)$, to the astrophysics variations with fiducial cosmology and a linear fit, $A(\xi^2)$, to the cosmology variations with fiducial feedback parameters shown in Fig. 9, we obtain¹²

$$A = 36.69 (1 - 2.738\bar{\eta}_0 + 2.096\bar{\eta}_0^2 - 0.2988\xi^2), \quad (29)$$

for $\bar{\eta}_0 \in [0.59, 0.68]$ and $\xi^2 = f_b/c_v^2 \cong 0.65 f_b/(\Omega_m \sigma_8)^{1/4}$. This prescription covers a wide range of astrophysical and cosmological scenarios with a single feedback parameter that is independent of cosmology at first-order: $\bar{\eta}_0$. The range $\bar{\eta}_0 \in [0.59, 0.68]$ could be taken as a prior motivated by FLAMINGO. For a typical *Planck* cosmology, the model then excludes the DMO case with $(A, \eta_0) = (3.13, 0.603)$.

While the HMCODE parameters are poorly constrained by current weak lensing observations, at least when assuming Λ CDM (e.g. Joudaki et al. 2018; Asgari et al. 2021), this situation will change with the arrival of *Euclid*, LSST, and The Wide-Field Infrared Survey Telescope (WFIRST), or when considering extensions like decaying dark matter. We caution that approximations like equation (29) are not adequate for future surveys (e.g. Taylor, Kitching & McEwen 2018; Lacasa 2019). A more accurate approach would be to rely on suites of simulations that vary both astrophysical and cosmological parameters, like the CAMELS suite (Villaescusa-Navarro et al. 2021), but in significantly larger volumes to model clustering accurately over the range of scales probed by weak lensing surveys.

¹²We remind the reader that the baryon fraction, $f_b = \Omega_b/(\Omega_b + \Omega_c)$, should be defined relative to the cold matter species, thus excluding neutrinos.

5.2 Comparison with HMCODE-2020

Next, we will compare with an updated version of HMCODE called HMCODE-2020 (Mead et al. 2021), which brings numerous improvement over the model discussed in the previous section. Let us focus on the implementation of baryonic feedback. As in the simpler model, HMCODE-2020 allows baryonic effects to alter halo concentrations by modifying the amplitude, A , of the mass–concentration relation (27). Baryonic effects also change the halo density profile, but rather than rescaling the profile as in equation (28), it is modified via

$$\bar{\rho}(k, M) \rightarrow \left(\frac{\Omega_c}{\Omega_m} + f_g(M) \right) \bar{\rho}(k, M) + f_*, \quad (30)$$

where $f_g(M)$ is the gas mass fraction and f_* the stellar mass fraction. In this expression, the first term accounts for the expulsion of gas by rescaling the overall amplitude of the profile. Secondly, a constant shot noise term is added to model the stellar population. The mass-dependent gas fraction is defined as

$$f_g(M) = \left(\frac{\Omega_b}{\Omega_m} - f_* \right) f_{\text{ret}}(M), \quad (31)$$

where $f_{\text{ret}}(M)$ is the fraction of gas that is retained, given by

$$f_{\text{ret}}(M) = 1 - f_{\text{esc}}(M) = \frac{(M/M_b)^2}{1 + (M/M_b)^2}. \quad (32)$$

The parameter M_b is a transition mass, defined such that haloes with $M \gg M_b$ retain all their gas. Baryonic feedback is thus controlled by three parameters: A , M_b , and f_* . In Mead et al. (2021), three further parameters are used to model the time dependence of A , M_b , and f_* .

To compare HMCODE-2020 with our results, we again fit the model to the baryonic suppression, $F_b(k)$, at $z = 0$ measured from our fiducial L1_m9 simulations. We subsequently take the best-fitting values of A , M_b , f_* as fixed, while varying the cosmological parameters, and use HMCODE-2020 to determine the non-factorizable corrections. The results are shown in Fig. 10 as blue crosses. In contrast to the HMCODE model discussed in the previous section, there is now a clear trend with higher baryon fractions, f_b , and lower concentrations, c_v , leading to stronger baryonic feedback. This is in qualitative agreement with our results. However, as can be seen from the figure, HMCODE-2020 predicts a weaker dependence on cosmology than what is seen in the FLAMINGO simulations, particularly for models with large values of ξ^2 and strong baryonic feedback. This is consistent with the comparison in Mead et al. (2021) of their model with the BAHAMAS simulations (McCarthy et al. 2017).

We can understand this by noting that the escape fraction, $f_{\text{esc}}(M)$, given by equation (32), does not depend on cosmological parameters. This is in contrast to the discussion in Section 3.3, where we argued that the escape fraction also depends on cosmology. In other words, while equation (30) accounts for the fact that a greater fraction of the mass is susceptible to feedback when Ω_b/Ω_m is larger, it does not incorporate the finding that this feedback itself is also stronger. Similarly, the escape fraction should also depend on cosmological parameters through the halo concentration. In summary, HMCODE-2020 provides a clear improvement over HMCODE, but does not fully capture the cosmological coupling discussed in this paper.

6 CONCLUSION

Upcoming weak lensing surveys will measure the clustering of matter with unprecedented precision and provide tight constraints on cosmological models. Since a large fraction of the information

resides on non-linear scales, where baryonic processes are important, one crucial question for the interpretation of these observations is the coupling between the cosmological parameters of interest and astrophysical feedback processes. Previous work has often neglected this coupling, assuming the effects of cosmology and feedback to be independent. Using the FLAMINGO suite of hydrodynamical simulations (Kugel et al. 2023; Schaye et al. 2023), we determined that the cosmological coupling of baryonic feedback gives rise to non-factorizable corrections to the matter power spectrum on scales $1 h \text{ Mpc}^{-1} < k < 10 h \text{ Mpc}^{-1}$, which cannot be ignored at the level of 1 per cent accuracy needed for Stage-IV surveys (e.g. Taylor et al. 2018; Lacasa 2019).

Our model of the non-factorizable corrections is built on a careful analysis of the ways in which baryonic feedback could depend on cosmology, using secondary halo properties, such as the halo concentration and formation epoch, as proxies for different mediating mechanisms. We determined that the cosmological effects on the baryon fractions and binding energies of haloes are most important, with greater baryon fractions leading to stronger feedback, while greater binding energies lead to weaker feedback. By contrast, the role of the halo environment is negligible. We then constructed a simple physical model of AGN feedback and showed that the non-factorizable corrections to the power spectrum can be accurately predicted from a single parameter combination, $f_b/c_v^2 \sim f_b/(\Omega_m \sigma_8)^{1/4}$, where f_b is the universal baryon fraction and c_v^2 a velocity-based definition of halo concentration, as described by equations (22) and (24). Interestingly, our model predicts that feedback is stronger for models with lower σ_8 and Ω_m , as suggested by the S_8 tension between high- and low-redshift probes of matter clustering (Aghanim et al. 2020; Asgari et al. 2021; Amon et al. 2022; Secco et al. 2022; Abbott et al. 2023). Given that baryonic and novel non-baryonic suppression mechanisms have both been considered as possible solutions to the S_8 tension (e.g. Amon & Efstathiou 2022; McCarthy et al. 2023; Preston et al. 2023), the question arises whether the two could work together to produce a greater overall suppression.

By running hydrodynamical simulations for two models with suppressed structure formation, involving massive neutrinos or decaying dark matter, we demonstrate that the combined effect of baryonic and non-baryonic suppression mechanisms is indeed greater than the sum of its parts. For massive neutrinos, we find that a combination of a summed neutrino mass of $\sum m_\nu \in [0.24, 0.48] \text{ eV}$ and standard baryonic feedback can reconcile CMB and weak lensing observations. However, this explanation is at odds with constraints on the expansion history inferred from CMB and BAO (Aghanim et al. 2020) and other probes (e.g. Palanque-DeLabrouille et al. 2020; Brieden et al. 2022). For decaying dark matter, we find a strong dependence of feedback on the dark matter lifetime, leading to sizeable non-factorizable corrections. For the most extreme model with a decay rate of $\Gamma = 24 \text{ km s}^{-1} \text{ Mpc}^{-1}$ ($\tau = 41 \text{ Gyr}$), the baryonic suppression is roughly twice as strong as for the case without decaying dark matter. Such short dark matter lifetimes are similarly disfavoured by geometric constraints (e.g. Audren et al. 2014; Aubourg et al. 2015). Hence, both models can reconcile CMB and weak lensing measurements and relieve the S_8 tension, but only at the expense of distorting the expansion history. Nevertheless, it seems likely that other suppression mechanisms also enhance baryonic feedback. In particular, we expect that velocity-dependent dark matter annihilation (Choquette et al. 2016) would give rise to larger corrections and a greater boost of baryonic feedback for the same overall loss of dark matter and change in expansion history, given that the loss would be concentrated in the centres of groups and clusters. This possibility will be explored in future works.

Finally, we considered the extent to which cosmological and astrophysical parameters are degenerate within the FLAMINGO model. We determined that the cosmological coupling of feedback becomes important on scales $k > 1 h \text{Mpc}^{-1}$ and for $z < 1$, suggesting that the degeneracy with key parameters of the FLAMINGO galaxy formation model may be broken by considering the dependence of the power spectrum on scale and time. This would require a model for the redshift evolution of the non-factorizable corrections, which we leave as a topic for future work. We also looked at popular feedback prescriptions that do not fully account for the non-factorizable corrections (Mead et al. 2015, 2021) and demonstrated that, as a result, their parameters encode both cosmological and astrophysical information. Hence, some cosmological information is lost by marginalizing over such parameters, which is the current practice for cosmic shear analyses. This is particularly problematic for non-standard parameters with greater effects on feedback, such as the neutrino mass and dark matter lifetime. We conclude that optimal use of forthcoming observations for cosmological inference requires baryonic feedback prescriptions that are more flexible and incorporate the dependence of feedback on cosmology or the use of large simulations that vary both astrophysical and cosmological parameters.

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DATA AVAILABILITY

The FLAMINGO data will be released publicly in the future. Those interested in working with the simulations now are encouraged to contact the corresponding author.

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APPENDIX A: DEPENDENCE ON SIMULATION VOLUME

In this work, we primarily use two simulation volumes: most of the large simulations listed in Table 1 have side length $L = 1$ Gpc, while the smaller simulations described in Section 2.2 have side length $L = 200$ Mpc. In Fig. A1, we show the non-factorizable correction to the matter power spectrum at $z = 0$ when changing the neutrino mass from $\sum m_\nu = 0.06$ eV to 0.24 eV or 0.48 eV, for both simulation volumes. We see that the two volumes agree to within about 0.5 per cent on the scales of interest. Since we are interested in

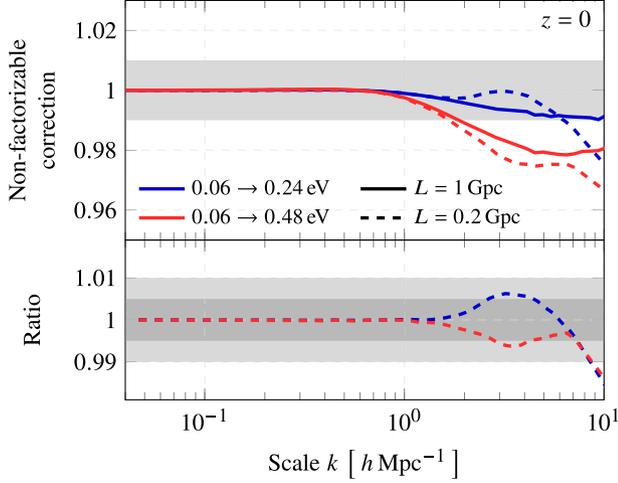


Figure A1. Dependence of the non-factorizable corrections on the simulation volume. We show the corrections at $z = 0$ when changing the sum of neutrino masses from $\sum m_\nu = 0.06$ eV to 0.24 eV or 0.48 eV. Solid lines correspond to $(1 \text{ Gpc})^3$ simulations, while dashed lines correspond to $(0.2 \text{ Gpc})^3$ simulations. The ratio is mostly within ± 0.5 per cent (dark grey) on the scales of interest.

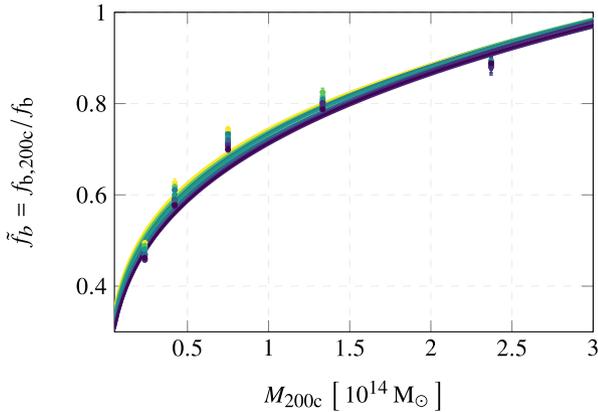


Figure B1. Fits of the renormalized baryon fractions, $\tilde{f}_b = f_{b,200c}/f_b$, where $f_{b,200c}$ is the baryon fraction within R_{200c} for matched haloes and f_b is the universal baryon fraction, as a function of halo mass, M_{200c} , for 11 small Λ CDM simulations. The error bars are difficult to see except at the high-mass end. The points and curves are colour coded according to the average baryonic suppression of the power spectrum, as in Fig. 1.

effects exceeding 1 per cent, we choose to use both volumes in our analysis, but expect to see a somewhat larger scatter for the power spectrum predictions from the smaller simulations.

APPENDIX B: ADDITIONAL FITS

In Section 3.3, we introduced a two-parameter power law (18) to describe the renormalized baryon fractions in haloes, $\tilde{f}_b = f_{b,200c}/f_b$, as a function of halo mass, M_{200c} . In Fig. B1, we show these fits for the Λ CDM simulations from Section 2.2. The points correspond to the median of \tilde{f}_b in each mass bin with bootstrapped error bars that are difficult to see at the scale of the plot, except at the high-mass end. The simulations have the same colours as in Fig. 1, indicating the average baryonic suppression of the power spectrum. As expected, the unambiguous trend is that the power spectrum is more strongly

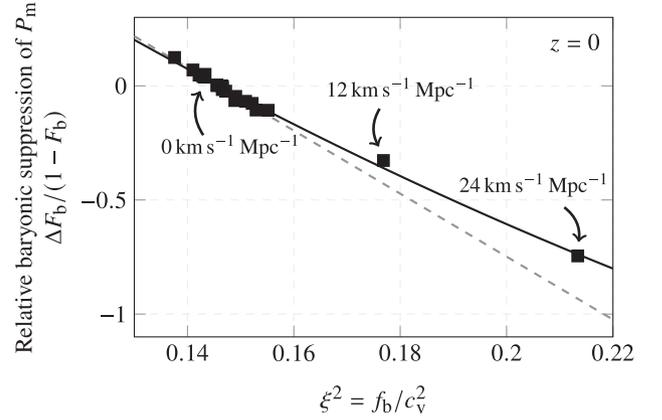


Figure B2. Non-factorizable corrections to the power spectrum at $z = 0$ as a function of ξ^2 for the FLAMINGO simulations with decaying dark matter (points labelled with decay rates of $12 \text{ km s}^{-1} \text{ Mpc}^{-1}$ and $24 \text{ km s}^{-1} \text{ Mpc}^{-1}$) and without decays (labelled with $0 \text{ km s}^{-1} \text{ Mpc}^{-1}$). The fit of equation (22) in the right-hand panel of Fig. 5 is reproduced here as a grey dashed line. A new two-parameter fit to all simulations, including those with decaying dark matter and given by equation (B1), is shown as a black line.

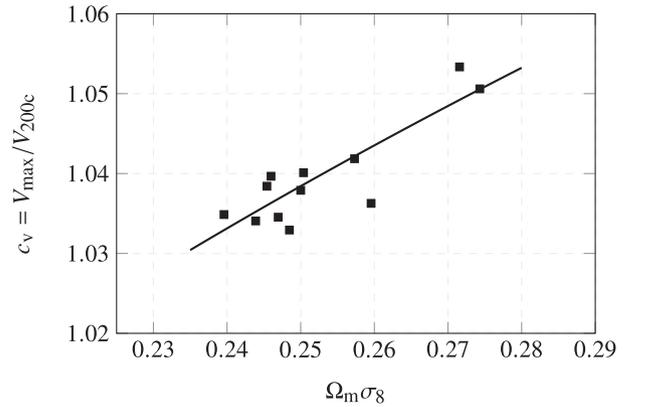


Figure B3. Fit of the median halo concentration, c_v , in terms of the cosmological parameter combination $\Omega_m \sigma_8$, as given by equation (23).

suppressed for models with lower renormalized baryon fractions. The renormalized baryon fractions, in turn, are lower for simulations with greater universal baryon fractions, f_b , and lower halo concentrations, c_v , as shown in Fig. 4.

Next, we provide an extension of the right-hand panel of Fig. 5, showing the non-factorizable corrections to the power spectrum as a function of $\xi^2 = f_b/c_v^2$. In Fig. B2, we reproduce all the data points from Fig. 5 and add two further points for the FLAMINGO simulations with decaying dark matter. The haloes in these simulations are much more strongly affected by baryonic feedback and their concentrations and baryon fractions are far outside the parameter ranges considered in Fig. 5. We caution that there is an additional choice in the definition of ξ^2 for the decaying dark matter simulations, since the universal baryon fraction, f_b , now depends on time. In this plot, we have chosen to evaluate f_b at $z = 0$, given that we do the same for c_v and $P(k)$.

The one-parameter fit to the Λ CDM (and massive neutrino) simulations from equation (22) is shown as a grey dashed line in Fig. B2. When extrapolated, this model does not fit the decaying dark matter simulations well, but this is not surprising given that the

models are far outside the original parameter range. We can describe all simulations, including the ones with decaying dark matter, by adding just one further parameter:

$$\frac{\Delta F_b}{1 - F_b} = -\alpha_1 \Delta(\xi^2) + \alpha_2 [\Delta(\xi^2)]^2, \quad (\text{B1})$$

with $\alpha_1 = 18.1 \pm 3.5$ and $\alpha_2 = 19.9 \pm 10.1$. This relation is shown as a black curve in Fig. B2.

Finally, we show a fit of the median halo concentration, c_v , for haloes with masses M_{200c} in the range $[10^{13.75} M_\odot, 10^{14.25} M_\odot]$, as a

function of the cosmological parameter combination $(\Omega_m \sigma_8)^{1/8}$. This parametrization was introduced in equation (23) in Section 4.1. The data for the Λ CDM simulations from Section 2.2 and the resulting fit are shown in Fig. B3.

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