

# 1 Structural health monitoring of tendons in a multibody floating offshore wind turbine

## 2 under varying environmental and operating conditions

3 Christos S. Sakaris <sup>a</sup>, Yang Yang <sup>b</sup>, Musa Bashir <sup>a,\*</sup>, Constantine Michailides <sup>c</sup>, Jin Wang <sup>a</sup>,

4 John S. Sakellariou <sup>d</sup>, Chun Li <sup>e</sup>

5 <sup>a</sup> *Department of Maritime and Mechanical Engineering, Liverpool John Moores University, Liverpool, Byrom*  
6 *Street, L3 3AF, UK*

7 <sup>b</sup> *Faculty of Maritime and Transportation, Ningbo University, Ningbo, 315211, P.R. China*

8 <sup>c</sup> *Department of Civil Engineering and Geomatics, Cyprus University of Technology, 2-8 Saripolou, 3036*  
9 *Limassol, Cyprus*

10 <sup>d</sup> *Department of Mechanical Engineering & Aeronautics, University of Patras, GR 26504 Patras, Greece*

11 <sup>e</sup> *School of Energy and Power Engineering, University of Shanghai for Science and Technology, Shanghai,*  
12 *200093, P.R. China*

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14 **Abstract:** The structural health monitoring of a Floating Offshore Wind Turbine (FOWT) tendons, taking into  
15 account the comprehensive damage diagnosis problem of damage detection, damaged tendon identification and  
16 damage precise quantification under varying environmental and operating conditions (EOCs), is investigated  
17 for the first time. The study examines a new concept of a 10 MW multibody FOWT whose tower is supported  
18 by a platform consisting of two rigid-body tanks connected by 12 tendons. Normal and the most severe EOCs  
19 from a site located in the northern coast of Scotland, are selected for the simulation of the FOWT structure  
20 under constant current but varying wind and wave conditions. Dynamic responses of the platform under  
21 different damage states are obtained based on the simulated FOWT. The damage scenarios are modelled via  
22 stiffness reduction (%) at the tendon's connection point to the platform's upper tank. Damage diagnosis is

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\* Corresponding author: [m.b.bashir@ljmu.ac.uk](mailto:m.b.bashir@ljmu.ac.uk)

23 achieved via an advanced method, the Functional Model Based Method, that is formulated to operate using a  
 24 single response signal and stochastic Functional Models representing the structural dynamics under the effects  
 25 of varying EOCs and any magnitude of the considered damages. Due to the robustness and high number of the  
 26 existing tendons, the effects of considered damages on the FOWT dynamics are minor and overlapped by the  
 27 effects of the varying EOCs, indicating a highly challenging damage diagnosis problem. Very good damage  
 28 detection results are obtained with the damage detection almost faultless and with no false alarms. Accurate  
 29 tendon identification is achieved for the 95% of the considered test cases, while the mean error in damage  
 30 quantification is approximately equal to 4% using measurements from just a single accelerometer within a very  
 31 limited frequency bandwidth of [0-5] Hz.

32 **Keywords:** Damaged tendon diagnosis, Structural Health Monitoring, Functional Models, Statistical time series  
 33 methods, Floating Offshore Wind Turbine, Varying environmental and operating conditions

34

## 35 1. Introduction

36 Structural Health Monitoring (SHM) of offshore structures such as fixed and floating platforms for  
 37 Offshore Wind Turbines (OWTs), is vital as damage on critical parts may lead to loss of stability, inefficient  
 38 operation or total loss of asset. Offshore structures operate under varying Environmental and Operating  
 39 Conditions (EOCs) such as wind speed (WS), significant wave height (SWH), current, temperature and others,  
 40 which partially or fully “mask” the effects of damages on the structural dynamics, rendering SHM highly  
 41 challenging [1-4]. The SHM of tendons [5-8], mooring lines [9-13], offshore platforms [14-21] and OWT towers  
 42 [21-23], has been mostly investigated albeit under constant EOCs. However, the realistic case of varying EOCs  
 43 that significantly affects the structural dynamics and makes SHM difficult, has been considered only in a limited  
 44 number of studies [1-3, 24-25] with focus mostly on platforms and towers of OWTs. More so, these studies  
 45 were confined only to the first level of SHM, which is damage detection [26].

46 The damage detection methods employed in the above studies are conducted using a data-based model such  
 47 as a state space [1, 25] or a regression [2, 24] models. The data-based model is exclusively developed using  
 48 vibration signals from the healthy structure and measurements of the EOCs. Model features which are sensitive  
 49 to damage, such as its residual signal and selected modal parameters are acquired for damage detection. Thus,  
 50 based on the explicit modelling [27, 28] of the varying EOCs' effects on the dynamics of healthy OWTs and  
 51 measurements of the present EOCs, damage detection is achieved through a comparison of the features of the  
 52 present (unknown structural state) model with their counterparts from the healthy dynamics. These methods  
 53 usually require several sensors, multiple vibration signals and continuous measurements of the varying EOCs  
 54 both in the baseline (method's training) and inspection (diagnostics in real time) phases [1-3, 24-25]. The use  
 55 of several sensors and EOCs measurements are often costly and impractical.

56 Recently, a novel approach has been exclusively presented for damage detection under varying EOCs. The  
 57 main advantage of this approach over the previous methods is that no measurable EOCs are needed in the  
 58 diagnostics phase [27, 28], leading to reduced cost and equipment. This approach is based on the general  
 59 framework of the Functional Model Based Method (FMBM) [29], which has been successfully applied for  
 60 damage detection under varying EOCs in a railway vehicle suspension [27] and a composite beam [28]. In these  
 61 referenced studies, the healthy structural dynamics under varying EOCs are modelled via a stochastic Functional  
 62 Model (FM) whose parameters are expressed as functions of the EOCs. Additionally, the FM is based on a  
 63 concept of representing the transmittance function [30] under varying EOCs using a pair of vibration response  
 64 signals received via two sensors (one sensor per signal), with one measurement point taken as input and the  
 65 other as output. A further advantage of this approach is that the FM is estimated using a relatively low number  
 66 of response signal pairs, while the operating parameter that includes the EOCs may be scalar or vector of any  
 67 dimension according to the population of the EOCs. Two types of FMs have been used in this FMBM version  
 68 [27, 28], a Functionally Pooled AutoRegressive model with eXogenous excitation (FP-ARX) [27] and a Vector  
 69 FP-ARX (VFP-ARX) model [28]. It is noted that various other versions of the FMBM have been presented in  
 70 the past for damage precise localization [29, 31-36] and precise quantification [31, 37-38] under constant EOCs.

71 The goal of this study is to investigate, for the first time, the problem of SHM in tendons of a Floating  
 72 Offshore Wind Turbine (FOWT), taking into account the complete damage diagnosis process (damage  
 73 detection, damaged tendon identification and damage precise quantification) under varying EOCs. This is  
 74 achieved through the use of a new version of FMBM [27, 28] that is formulated to operate using just a single  
 75 response signal received via a single sensor instead of two signals received via two sensors used in [27, 28].  
 76 The structure examined in this study is a new concept of a 10 MW multibody FOWT whose tower is supported  
 77 by an improved and more stable version of the multibody floating platform (TELWIND) [39] consisting of two  
 78 rigid tanks connected by 12 tendons. The FOWT is subjected to varying EOCs corresponding to seven different  
 79 WSs, irregular SWHs and current of constant speed and direction, thus reflecting normal and the most severe  
 80 EOCs of the selected case study site located in the northern coast of Scotland. The FMBM used in this study is  
 81 based on two types of FMs, a single Functionally Pooled AutoRegressive (FP-AR) model and multiple Vector  
 82 FP-AR (VFP-AR) models (one per tendon). Due to the dependence of SWH on WS, only the WS is considered  
 83 as an operating parameter in the FMs. Therefore, the FP-AR model describes the healthy structural dynamics  
 84 under the effects of varying EOCs of any potential WS and it is used for damage detection. As for the VFP-AR  
 85 models, each model describes the structural dynamics under the effects of varying EOCs of any potential WS  
 86 and any damage magnitude on the considered tendon. The VFP-AR models are used for damaged tendon  
 87 identification and damage precise quantification. It should be noted that the structural complexity of the FMs  
 88 employed in this study, is significantly reduced, thus offering the advantage for their quick estimation.

89 In addition, various damage scenarios corresponding to reduced stiffness (%) at a tendon's connection point  
 90 to the platform's upper tank, are realized. Two of the total 12 tendons are examined in this study, namely, the  
 91 tendon under the largest tension due to its proximity to the wave direction and an arbitrarily selected tendon  
 92 being far from the mooring line. It should be noted that the effects of varying EOCs on the healthy FOWT fully  
 93 "mask" the effects of damages of magnitude less than 20 %. On the other hand, the damages of magnitude [20-  
 94 80] % have small effects on the structural dynamics due to the high number and robustness of the existing  
 95 tendons. Additionally, the damages of magnitude [20-80] % on the one tendon under constant EOC, affect the

96 structural dynamics in a similar manner. The damages of magnitude [10-100] % on different tendons, also have  
 97 similar effects on the structural dynamics. Thus, these conditions lead to a highly challenging damage diagnosis  
 98 problem.

99       Consequently, a numerical model of the coupled FOWT is used for the implementation of damage scenarios  
 100 and the simulation of healthy and damaged structures under the seven WSs and SWHs. A single underwater  
 101 accelerometer measures the dominant response, surge (translation movement along axis x) acceleration, within  
 102 a limited and low frequency bandwidth of [0-5] Hz, corresponding to realistic operating conditions under  
 103 physical excitation.

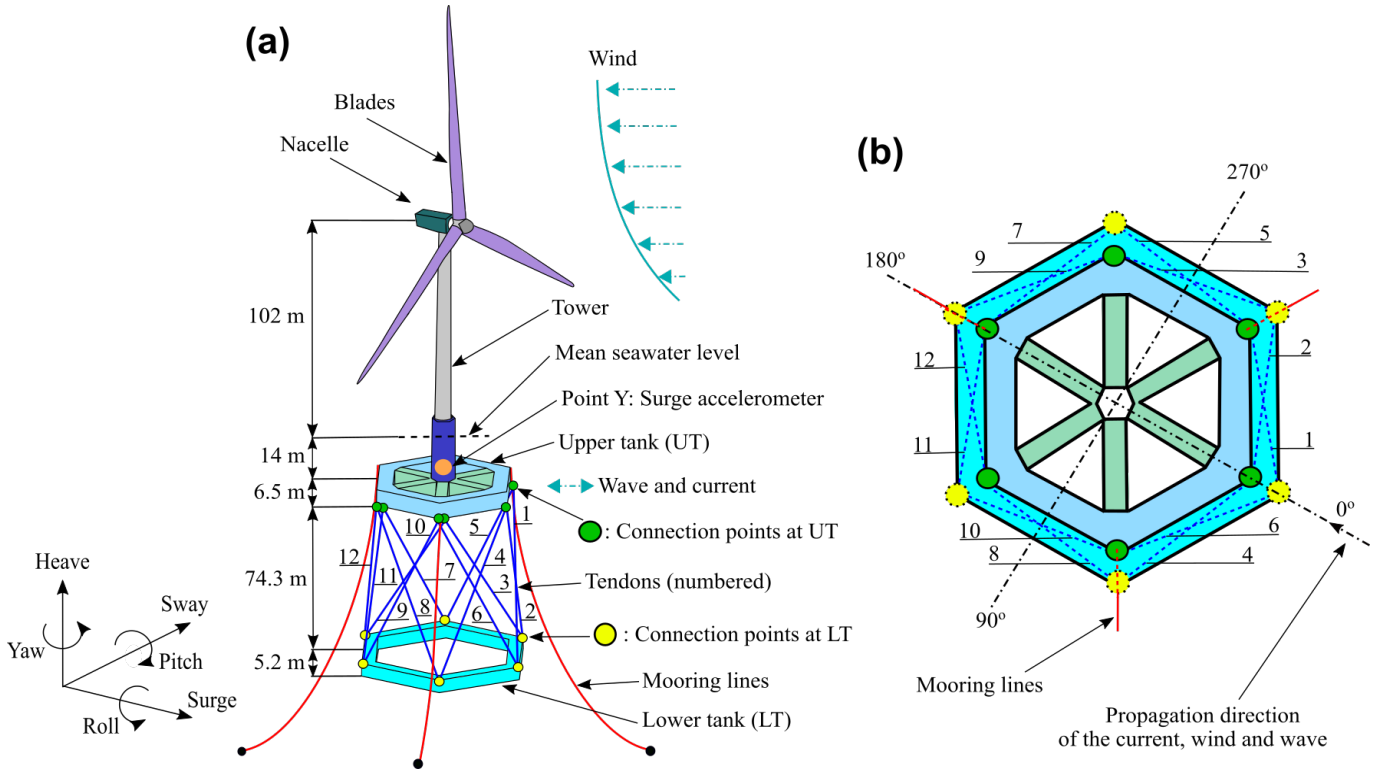
104       The rest of this paper is structured as follows: The FOWT, the varying EOCs, the tendon damages and the  
 105 simulation details are presented in Section 2. The methodology for damaged tendon diagnosis is presented in  
 106 Section 3. The damaged tendon diagnosis results are presented in Section 4. The conclusions are presented in  
 107 Section 5.

## 108 **2. The FOWT structure, its dynamics, damage scenarios and simulations under** 109 **varying EOCs**

### 110 **2.1 The 10 MW multibody FOWT structure**

111       The examined structure is a new concept of a 10 MW FOWT, which consists of a tower supported by  
 112 improved and more stable (with reduced weight) version of the multibody floating platform (TELWIND)  
 113 developed by Esteyco [40] in the ARCWIND project [39]. The multibody platform consists of a lower tank  
 114 (LT) and an upper tank (UT) connected by 12 tendons (steel cables) (Figure 1) as opposed to 6 tendons (albeit  
 115 with changes to tendon properties) on the previous version [39]. Three mooring lines are connected to fairleads  
 116 attached to the UT's top surface at 14 m below the mean sea level for station-keeping of the platform. Part of  
 117 the reasons for the increase in tendons is to provide sufficient redundancy of tendons connecting between the  
 118 upper tank and the lower tank. This further guarantees that the 10 MW FOWT remains safe and stable in the  
 119 event that a single tendon is broken. With regards to the model properties, the upper tank has a draught of 20.5  
 120

121 m, a mass of  $5.31 \cdot 10^6$  kg and a volume of  $7399.02 \text{ m}^3$ . The draught of the lower tank is 100 m, the mass is  
 122  $8.72 \cdot 10^6$  kg and the volume equals  $7922.92 \text{ m}^3$ . The pretension of the 12 tendons is approximately  $3 \cdot 10^6$  N.



123  
 124 **Figure 1.** (a) The 10 MW multibody FOWT, the position of the accelerometer (Point Y) and the damage  
 125 locations which are the connection points at the UT. (b) Bottom view of the platform with the propagation  
 126 direction of the current, wind and wave.

## 128 2.2 The varying EOCs and damage scenarios

129 In this study, the FOWT is examined under varying EOCs corresponding to seven different WSs 4 m/s, 8  
 130 m/s, 11.4 m/s, 14.5 m/s, 18 m/s, 21.5 m/s and 25 m/s with SWHs 1.61 m, 1.67 m, 2.16 m, 2.55 m, 2.95 m, 3.56  
 131 m, 4.02 m (Table 1). The FOWT is in a nonoperational state below its cut-in speed of 4 m/s and above a cut-  
 132 out speed of 25 m/s. The wind is generated via the Kaimal spectrum [41] and a different time series is used as  
 133 wind excitation to the FOWT for each simulation. Consequently, the same spectral intensity is maintained. The  
 134 irregular waves are generated via the modified two-parameter Pierson-Moskowitz spectrum [42], [43]. The  
 135 EOC also includes current of constant speed and direction. Details of the wind, wave and current parameters  
 136 corresponding to the varying EOCs used in this study, are presented in Table 1 and Figure 1(b). These  
 137

138 parameters represent the characteristics of normal and the most severe EOCs of the selected site located in the  
139 northern coast of Scotland.

140 The healthy scenarios are considered under the seven WSs and SWHs. Each examined damage scenario  
141 corresponds to a reduction in the tendon's stiffness (%) at its connection point to the upper tank of the platform  
142 under given WS and SWH. The stiffness reduction covers a range of [10-100] % with an increment of 5 %.  
143 Tendons 6 and 8 are examined, with tendon 6 suffering the largest tension due to its proximity to the wave  
144 direction and tendon 8 randomly selected due to its proximity to a mooring line (Figure 1(b)). WS response for  
145 each healthy state is designated as  $F_w$  with  $w$  being the WS. Equally, each examined damage condition is  
146 designated as  $F_{w,m}^q$  with  $q = 6, 8$  for the examined tendon and  $m$  the damage magnitude (% stiffness reduction).

147 **Table 1. Details of the varying EOCs.**

Wind speed (WS)	Significant wave height (SWH)	Peak frequency	Propagation direction of sea current, wave, wind	Current speed	Excitation bandwidth
4 m/s	1.61 m	0.285 Hz	0°	0.22 m/s	[0.1-100] Hz
8 m/s	1.67 m	0.199 Hz	0°	0.22 m/s	[0.1-100] Hz
11.4 m/s	2.16 m	0.185 Hz	0°	0.22 m/s	[0.1-100] Hz
14.5 m/s	2.55 m	0.152 Hz	0°	0.22 m/s	[0.1-100] Hz
18 m/s	2.95 m	0.14 Hz	0°	0.22 m/s	[0.1-100] Hz
21.5 m/s	3.56 m	0.121 Hz	0°	0.22 m/s	[0.1-100] Hz
25 m/s	4.02 m	0.112 Hz	0°	0.22 m/s	[0.1-100] Hz

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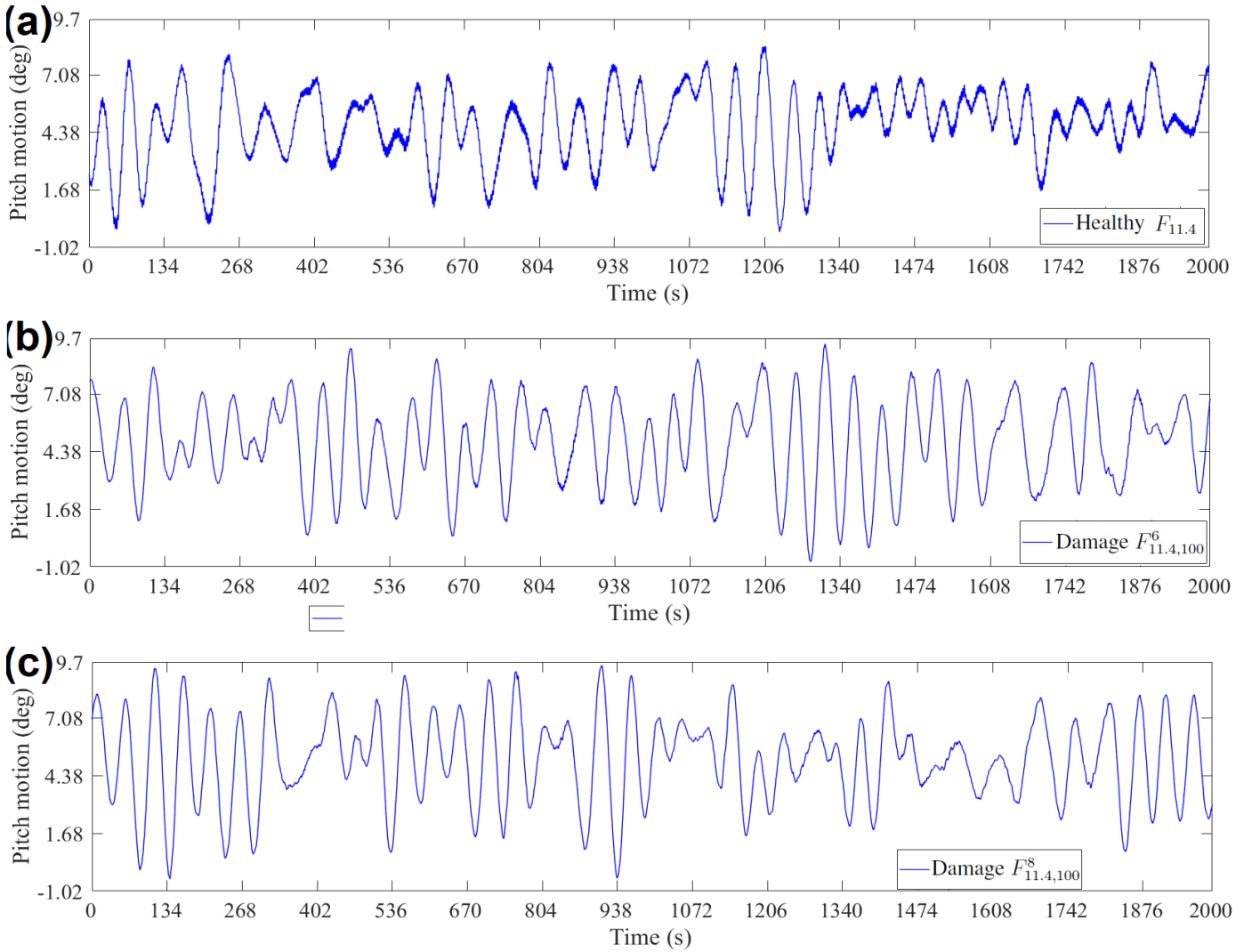
## 150 2.3 The simulations

151

152 This study uses vibration responses of the 10 MW multibody FOWT under varying EOCs, which correspond  
153 to healthy and different damaged states. The responses are obtained from a numerical simulation [44] conducted  
154 using F2A, a coupled ANSYS-AQWA and NREL FAST [45]. The platform is modeled as a fully coupled  
155 multibody, consisting of two rigid tanks (UT and LT), connected by 12 flexible tendons and kept in station by  
156 three mooring lines modelled as nonlinear catenary.

157 An important consideration in the simulation of the platform is its stability in the event of a tendon failure.  
158 The tendons in this concept are designed to have redundancy in the event a tendon or the connection between

the upper and the lower tanks fails. The goal is to ensure that the remaining tendons have sufficient reserved capacity to provide stability and support operations. Thus, the FOWT remains safe and stable even if a single tendon is broken. Furthermore, the results of the coupled analysis of a 10 MW multibody FOWT (upper and lower tanks connected by tendons) have shown that this platform remains stable even after the break of a tendon [46]. This is further confirmed by the non-exceedance of the variation range (-15 deg to 15 deg) of the platform's pitch motion response under healthy and damaged states (Figure 2). Further details on the platform's natural frequencies and eigenmodes are available in [8, 46].



**Figure 2.** Pitch motion signals from Point Y for the (a) healthy state  $F_{11.4}$ , (b) the damage state  $F_{11.4,100}^6$  and (c) the damage state  $F_{11.4,100}^8$ .



170 Although the six degrees of freedom (surge, heave, sway, roll, yaw and pitch) accelerations are measured  
 171 using a single sensor placed on the UT (Point Y, Figure 1(a)), only the surge acceleration is used in this study.  
 172 This is because the surge acceleration is determined as the most dominant response. The acceleration signals  
 173 are sampled at  $f_s = 10$  Hz (acceleration signal bandwidth of [0–5] Hz) with each being  $N = 20000$  samples  
 174 (2000 s) long.

175 Similarly, 6 acceleration signals are obtained from each simulation, one for each degree of freedom. A total  
 176 of 43 simulations are conducted for the healthy structure under the seven WSs (Table 1). A total of 474  
 177 simulations are conducted with a single damage for each of the 19 considered magnitudes from each of the two  
 178 damage locations considered (connection points of tendons 6, 8 at the UT, Figure 1) under each WS. 4  
 179 simulations for the healthy structure (one under each of the WSs 4 m/s, 11.4 m/s, 18 m/s, 25 m/s) and 80  
 180 simulations for the damaged structure (one per damage magnitude, covering a range of [10-100] % with an  
 181 increment of 10%, under each of the WSs 4 m/s, 11.4 m/s, 18 m/s, 25 m/s on each of the two tendons) are used  
 182 in the method's training phase. The remaining 39 simulations of healthy and 394 of damaged structures are  
 183 solely used in the inspection phase for performance assessments. The 39 simulations correspond to 9 simulations  
 184 under each of the WSs 4 m/s, 11.4 m/s, 18 m/s, 25 m/s and 1 simulation under each of the WSs 8 m/s, 14.5 m/s,  
 185 21.5 m/s. The 394 simulations correspond to i) 2 simulations for each damage magnitude, covering a range of  
 186 [10-100] % with an increment of 10 %, under each of the WS 4 m/s, 11.4 m/s, 18 m/s, 25 m/s on each of the  
 187 two tendons, ii) 3 simulations for each damage magnitude, covering a range of [15-95] % with an increment of  
 188 5 %, under each of the WS 4 m/s, 11.4 m/s, 18 m/s, 25 m/s on each of the two tendons, iii) 1 simulation for each  
 189 damage magnitude 10 % and 35 % under WS 8 m/s on each of the two tendons, iv) 1 simulation for each damage  
 190 magnitude 10 %, 35 %, 55 % and 75 % under WS 14.5 m/s on each of the two tendons, and v) 1 simulation for  
 191 each damage magnitude 10 %, 35 % and 55 % under WS 21.5 m/s on each of the two tendons. Each signal is  
 192 sample mean corrected and scaled by its sample standard deviation. Details of the simulations and measured  
 193 signals, are presented in Table 2.

## 2.4 Effects of damage and varying EOCs on the FOWT dynamics

The dynamics of the FOWT under the healthy state, vary due to the variability of the WS. This is confirmed through discrepancies between the PSDs estimated via the Welch estimator [47] (Welch estimation details:

**Table 2.** Details of the performed simulations and vibration signals.

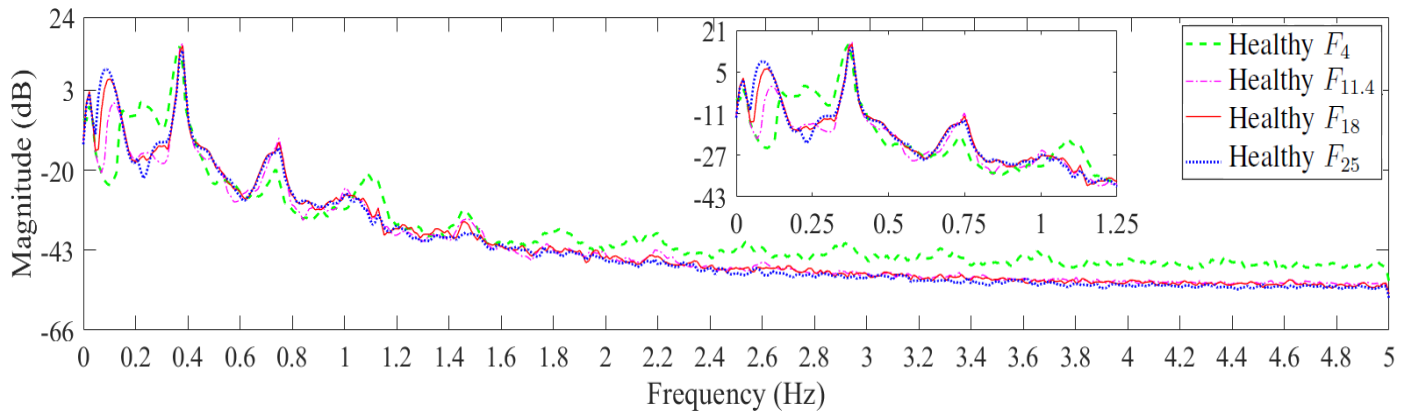
Structural state	Description	No. of damaged tendons	No. of damage magnitudes	No of WSs	No. of simulations – Baseline phase	No. of simulations – Inspection phase
Healthy	-	-	-	7	4 (one under each WS [4, 11.4, 18, 25] m/s)	36 (9 under each WS [4, 11.4, 18, 25] m/s) 3 (1 under each WS [8, 14.5, 21.5] m/s)
Damaged	Reducing the stiffness of a single tendon (%) (increment of 5%)	2 (Tendons 6, 8)	19	7	80 (one per damage magnitude [10, 20, 30, 40, ..., 100] % under each WS [4, 11.4, 18, 25] m/s on each tendon)	394 (2 per damage magnitude [10, 20, 30, ..., 100] % under each WS [4, 11.4, 18, 25] m/s on each tendon) (3 per damage magnitude [15, 25, 35, ..., 95] % under each WS [4, 11.4, 18, 25] m/s on each tendon) (1 per damage magnitude [10, 35] % under WS [8] m/s on each tendon) (1 per damage magnitude [10, 35, 55, 75] % under WS [14.5] m/s on each tendon) (1 per damage magnitude [10, 35, 55] % under WS [21.5] m/s on each tendon)
Sampling frequency: $f_s = 10$ Hz, acceleration signal bandwidth: [0-5] Hz						
Signal length: $N = 20000$ samples (2000 s)						

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Matlab function *pwelch.m*; signal length 20000 samples, window length 868 samples, 95% overlap, Hamming window, frequency resolution of 0.011 Hz) and corresponding to the healthy state under the four WSs 4 m/s, 11.4 m/s, 18 m/s, 25 m/s, in Figure 3. The discrepancies are evident in the bandwidths of [0.04-0.3] Hz and [1.05-1.2] Hz. Moreover, in Figure 4, the effects of selected damage cases on the structural dynamics, are shown via Welch-based (Welch estimation details: Matlab function *pwelch.m*; signal length 20000 samples, window

204 868 samples, 95% overlap, Hamming window, frequency resolution of 0.011 Hz) PSD estimates corresponding  
 205 to the healthy structure and the structure under 3 damage magnitudes 10 %, 20 %, 80% on tendon 6 and under  
 206 the four WSs. In Figure 4(a), the PSDs of the healthy and damaged structure under damage of magnitude 10 %,  
 207 overlap throughout the frequency bandwidth. In Figures 4(b)-(c), the PSDs of the healthy and damaged structure  
 208 under damage of magnitudes 20 %, 80 %, overlap extensively for most of the frequency bandwidth. Deviations  
 209 between the healthy and damaged structural dynamics are noticed in bandwidth of [0.85-1.2] Hz for magnitude  
 210 20 % (Figure 4(b)) and in bandwidths of [0.5-0.6] Hz and [0.85-1.2] Hz for magnitude 80 % (Figure 4(c)). It is  
 211 noted that similar changes on the dynamics are observed for damages on tendon 8. Based on these results, it is  
 212 evident that the effects of varying WS on the healthy FOWT dynamics, fully 'mask' the effects of damages of  
 213 magnitude less than 20 %. Furthermore, small deviations (less than 0.1 Hz) between the healthy and damaged  
 214 structural dynamics exist for magnitude [20-80] % due to the robustness and high number of the existing  
 215 tendons. Hence, it is confirmed by the deviations corresponding to damage magnitude [10-80] % that these  
 216 damages have small effects on the structural dynamics and that damage detection is quite challenging.

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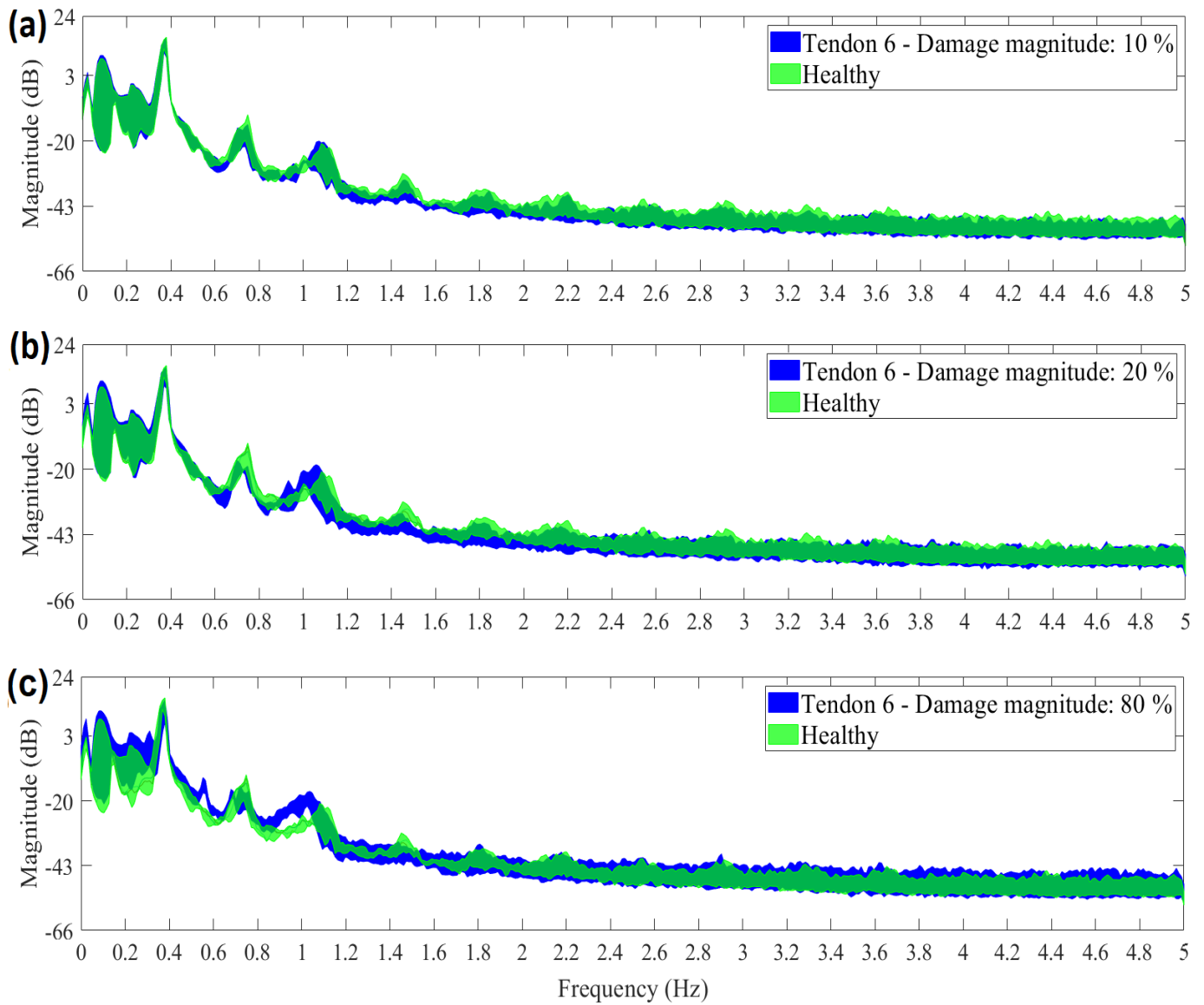
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219 **Figure 3.** Welch-based PSD estimates using surge acceleration signals from Point Y for the healthy FOWT  
 220 under the four considered WSs 4 m/s, 11.4 m/s, 18 m/s, 25 m/s.

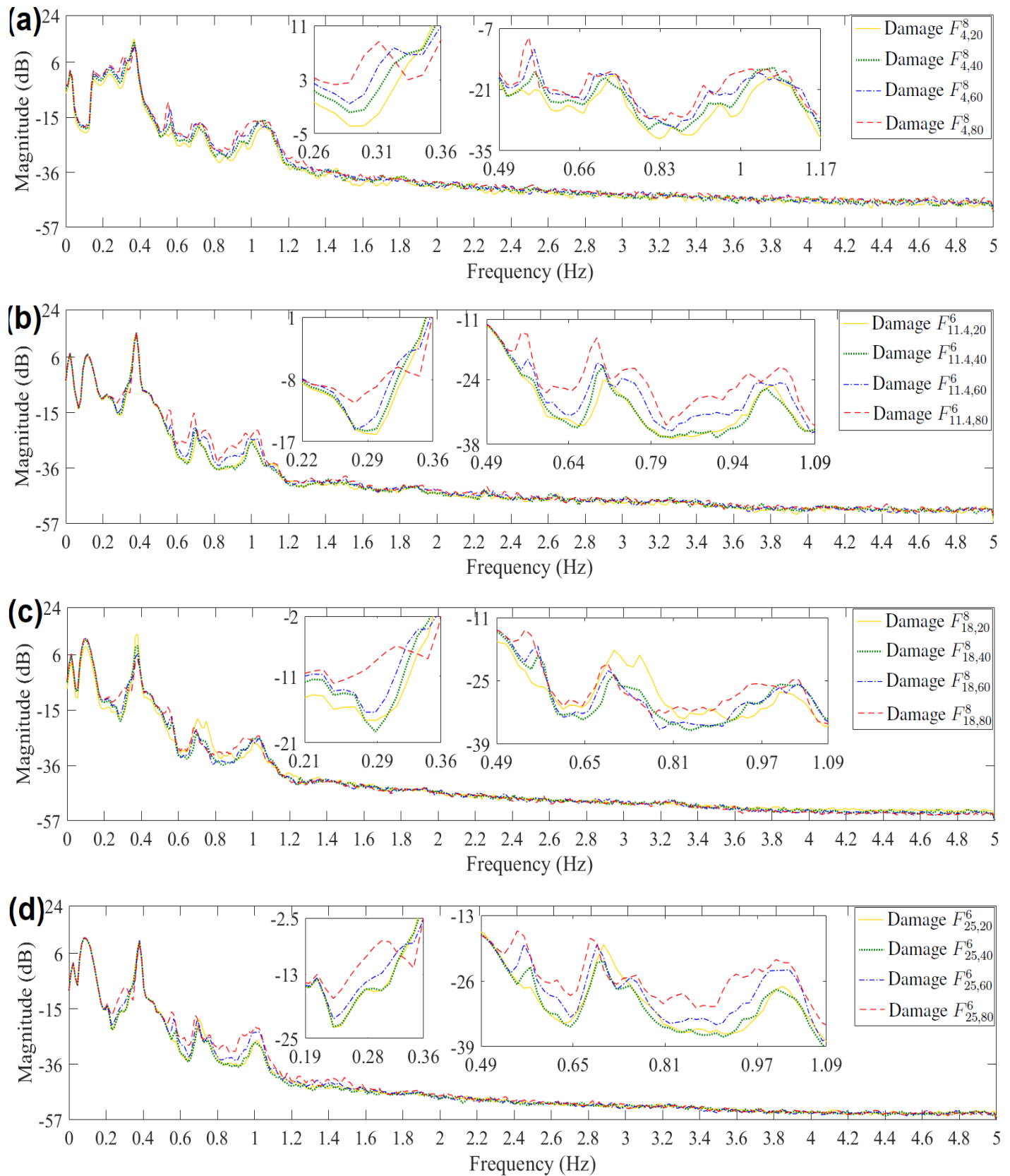
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222 In Figure 5, a comparison of Welch-based (Welch estimation details: Matlab function *pwelch.m*; signal  
 223 length 20000 samples, window 868 samples, 95% overlap, Hamming window, frequency resolution of 0.011  
 224 Hz) PSD estimates corresponding to damage of magnitudes 20 %, 40 %, 60 %, 80 % on tendons 6 for WSs 11.4  
 225 m/s, 25 m/s and on tendon 8 for WSs 4 m/s, 18 m/s, is presented. The effects of these damages differ in

226 bandwidths of [0.27-0.34] Hz, [0.5-0.6] Hz and [0.85-1.1] Hz for WS 4 m/s (Figure 5(a)) and in bandwidths of  
 227 [0.23-0.34] Hz, [0.5-0.6] Hz, [0.64-0.78] Hz, [0.85-1.07] Hz for WSs 11.4 m/s (Figure 5(b)), 18 m/s (Figure  
 228 5(c)) and 25 m/s (Figures 5(d)). It is obvious that the differences between these damages under constant WS,  
 229 are less than 0.23 Hz which is quite small. These small differences mean that damages of magnitude [20-80] %  
 230 under constant WS, similarly affect the structural dynamics due to the robustness and number of the existing  
 231 tendons. Also, similar effects indicate that damaged tendon identification and damage precise quantification are  
 232 highly challenging.



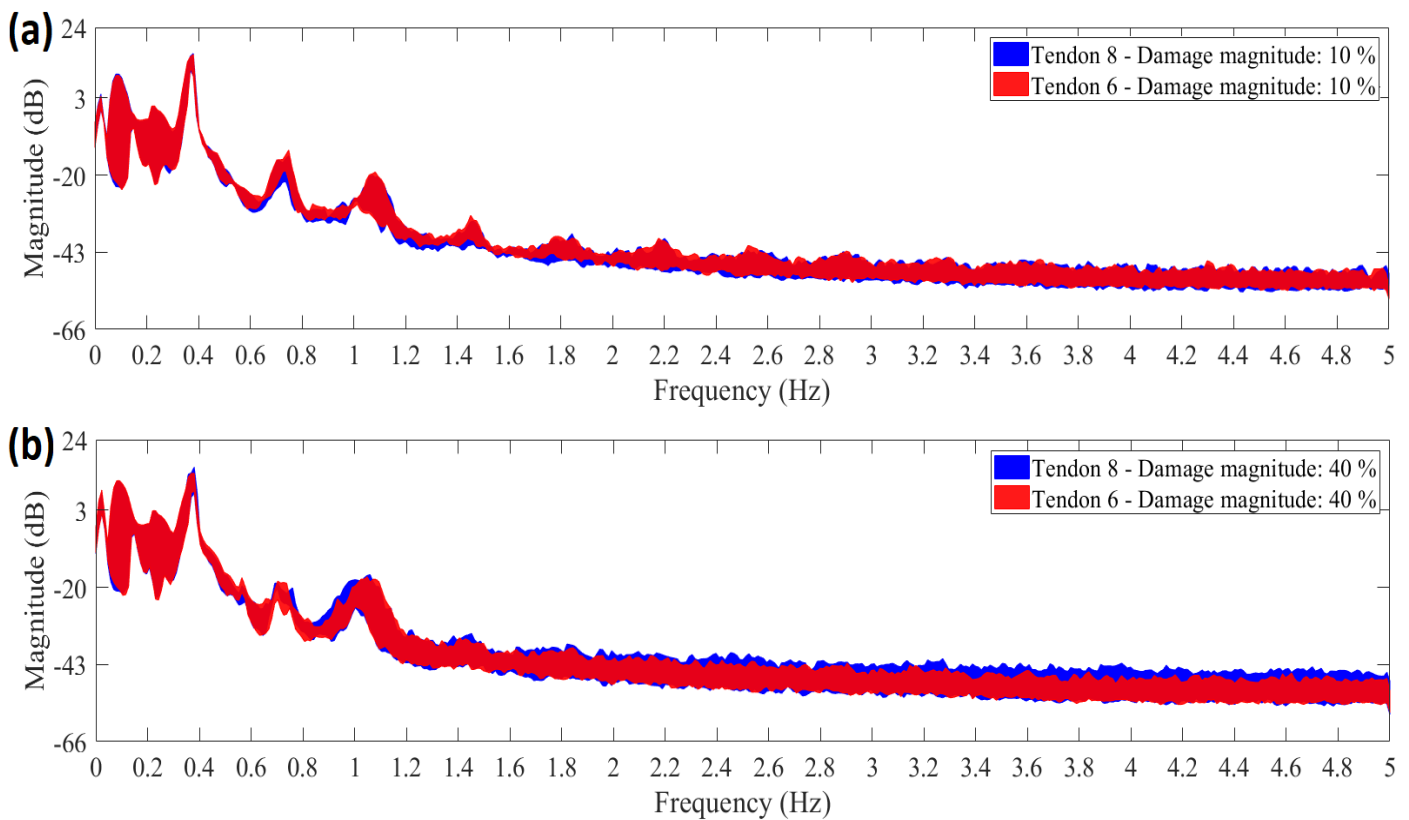
233  
 234 **Figure 4.** Welch-based PSD estimates using surge acceleration signals from Point Y for the healthy and the  
 235 damaged FOWT for the four WSs 4 m/s, 11.4 m/s, 18 m/s, 25 m/s, with damages on tendon 6 and of  
 236 magnitudes (a) 10 %, (b) 20 % and (c) 80 %.



237

238 **Figure 5.** Welch-based PSD estimates using surge acceleration signals from Point Y for the FOWT with  
 239 damage of magnitudes 20 %, 40 %, 60 %, 80% on (b),(c) tendon 6 for WS 11.4 m/s, 25 m/s and (a),(c) tendon  
 240 8 under WS 4 m/s, 18 m/s.

241 The difficulty of damaged tendon identification and damage precise quantification is also revealed by the  
 242 similarity in the effects of damages on different tendons. This similarity is confirmed through additional  
 243 comparisons between the Welch-based (Welch estimation details: Matlab function *pwelch.m*; signal length  
 244 20000 samples, window 868 samples, 95% overlap, Hamming window, frequency resolution of 0.011 Hz) PSD  
 245 estimates for some of the considered damage cases under the four WSs 4 m/s, 11.4 m/s, 18 m/s and 25 m/s,  
 246 presented in Figure 6. For each pair of the compared damage cases (damages of magnitude 10 % on tendons 6,  
 247 8 and damages of magnitude 40 % on tendons 6, 8), the corresponding PSDs almost coincide with each other.



248  
 249 **Figure 6.** Comparison between Welch-based PSD estimates using surge acceleration signals from Point Y for  
 250 damages on tendons 6, 8 and of the same magnitude for the four considered WSs 4 m/s, 11.4 m/s, 18 m/s, 25  
 251 m/s: (a) Magnitude 10 % and (b) magnitude 40 %.

252

### 253 3. Damaged tendon diagnosis method

254 In this study, the formulation of the new version of the FMBM [27, 28] based on a single response signal  
 255 received from a single sensor instead of two signals received via two sensors as in [27, 28], is presented for

256 damage diagnosis of tendons of a FOWT under varying EOCs. Due to the dependence of SWH on WS, only  
 257 the WS is considered as an operating parameter in the FMs. In step 1 of the method, damage detection is  
 258 achieved based on a single FP-AR model and damaged tendon identification and damage precise quantification  
 259 (steps 2 and 3) are achieved based on multiple VFP-AR models (one per tendon). The method consists of two  
 260 phases, the baseline phase and the inspection phase. The baseline (training) phase is performed based on data  
 261 from known structural states and when the structure is not operational (shutdown condition). The inspection  
 262 phase runs periodically or continuously during the structure's normal operation (on-line) based on current  
 263 vibration data, while the structure is under unknown health state.

### 264 3.1 Baseline phase

265

266 Initially, a FP-AR model [8] having the ability to represent the (partial) dynamics of the healthy FOWT under  
 267 varying EOCs of any potential WS, is identified. For identifying the FP-AR model,  $M_1$  response signals  
 268 corresponding to a sample of the considered WSs, are acquired. These sampled WSs cover the range  
 269  $[w_{min}, w_{max}]$  via the discretization  $w_v \in w_1, w_2, \dots, w_{M_1}$  and each response signal is characterized by a specific  
 270 WS  $w_v$ . Thus, for each WS, the following operating parameter  $k$  is defined as  $k = w_v \Leftrightarrow k_v$  with  $v =$   
 271  $1, \dots, M_1$  and a pool of  $M_1$  response signals  $y_k[t]$ , each of length  $N$ , is obtained with  $t = 1, \dots, N$ .

272 Based on the pool of the acquired response signals, a mathematical description of the healthy structural  
 273 (partial) dynamics under varying EOCs of any potential WS, is obtained through a FP-AR( $na$ ) <sub>$p$</sub>  model of the  
 274 following form [8]:

$$275 \quad y_k[t] + \sum_{i=1}^{na} \alpha_i(k) \cdot y_k[t-i] = e_k[t] \quad \text{with} \quad e_k[t] \sim \text{iid } \mathcal{N}(0, \sigma_e^2(k)) \quad \text{and} \quad k \in R \quad (1)$$

276

$$277 \quad \alpha_i(k) = \sum_{j=1}^p a_{i,j} \cdot G_j(k) \quad (2)$$

278

279 with  $na$  designating the AutoRegressive (AR) order,  $y_k[t]$  the response signal and  $e_k[t]$  the disturbance  
 280 (residual) signal that is white (serially uncorrelated) zero-mean with variance  $\sigma_e^2(k)$ . iid stands for identically

independently distributed and  $\mathcal{N}(\cdot, \cdot)$  designates normal distribution with the indicated mean and variance. Based on Equation (2), the AR parameters  $a_i(k)$  are functions of  $k$  belonging to a  $p$ -dimensional functional subspace spanned by the (mutually independent) functions  $G_1(k), G_2(k), \dots, G_p(k)$  (functional basis). The latter are univariate (one variable) orthogonal polynomials (Chebyshev, Legendre and other families) forming a functional basis  $\mathcal{G}$  [8, 37]. The constants  $a_{i,j}$  designate the AR projection coefficients which can be formed in the vector  $\boldsymbol{\theta} = [a_{1,1} \dots a_{na,p}]_{[na \cdot p \times 1]}^T$  (bold-face upper/lower case symbols designate matrix/column-vector quantities, respectively;  $^T$  designates transposition).

The FP-AR( $na$ ) $_p$  model (Equations (1), (2)) is re-written in a linear regression form (see details in [33, 36, pp. 28-31, 37]):

$$y_k[t] = [\boldsymbol{\varphi}_k^T[t] \otimes \mathbf{g}^T(k)] \cdot \boldsymbol{\theta} + e_k[t] = \boldsymbol{\phi}_k^T[t] \cdot \boldsymbol{\theta} + e_k[t] \quad (3)$$

with  $\boldsymbol{\varphi}_k[t] = [-y_k[t-1] \dots -y_k[t-na]]_{[na \times 1]}^T$  designating the regression vector,  $\mathbf{g}(k) = [G_1(k) \dots G_p(k)]_{[p \times 1]}^T$  the functional basis vector and  $\otimes$  the Kronecker product.

Pooling together Equation (3) of the FP-AR model corresponding to the various operating parameters  $k(k_1, k_2, \dots, k_{M_1})$  of the obtained  $M_1$  response signals for a single value of  $t$ , leads to:

$$\begin{bmatrix} y_{k_1}[t] \\ \vdots \\ y_{k_{M_1}}[t] \end{bmatrix}_{[M_1 \times 1]} = \begin{bmatrix} \boldsymbol{\phi}_{k_1}^T[t] \\ \vdots \\ \boldsymbol{\phi}_{k_{M_1}}^T[t] \end{bmatrix}_{[M_1 \times p \cdot na]} \cdot \boldsymbol{\theta} + \begin{bmatrix} e_{k_1}[t] \\ \vdots \\ e_{k_{M_1}}[t] \end{bmatrix}_{[M_1 \times 1]} \Rightarrow \mathbf{y}[t] = \boldsymbol{\Phi}[t] \cdot \boldsymbol{\theta} + \mathbf{e}[t] \quad (4)$$

Then, the data for  $t = 1, \dots, N$  are substituted in Equation (4) for the estimation of the parameter vector  $\boldsymbol{\theta}$  through the Ordinary Least Squares (OLS) estimator [33, 36, p. 15] (a hat ^ above a quantity designates its estimate):

$$\hat{\boldsymbol{\theta}} = [\sum_{t=1}^N \boldsymbol{\Phi}^T[t] \boldsymbol{\Phi}[t]]^{-1} \cdot [\sum_{t=1}^N \boldsymbol{\Phi}^T[t] \mathbf{y}[t]] \quad (5)$$

The order of the FP-AR model is determined through a conventional AR( $na$ ) model [48, pp. 81-83] based on a single response signal from the healthy structure under one of the considered WS values. The minimization of the Bayesian Information Criterion (BIC) [48, pp. 505-507] leads to the selection of the order



304 of the AR model. The determination of the FP-AR model's functional subspace  $p$ , given a selected orthogonal  
 305 polynomial family, is achieved via a Genetic Algorithm (GA) procedure [33, 36, p. 16, 49] based on the  
 306 minimization of an extended version of the BIC [36, pp. 33-35, 50].

307 FP-AR model's validation is achieved through the verification of the uncorrelatedness (whiteness) of the  
 308 model's residual signals. The whiteness check is conducted based on the Pena-Rodriguez test [36, p. 19, 51]  
 309 which detects changes in the partial autocorrelation function  $\pi_e[\tau]$  ( $\tau = 1, \dots, h$  is the lag) [52, pp. 64-68] of the  
 310 residual signals. The Pena-Rodriguez test is based on a D statistic which is a function of  $\pi_e[\tau]$  and it follows a  
 311 standard normal distribution  $D \sim \mathcal{N}(0,1)$ . A signal's whiteness is confirmed only if D does not exceed the  
 312 critical limits of the distribution,  $-Z_{1-\alpha} \leq D \leq Z_{1-\alpha}$  ( $-Z_{1-\alpha}, Z_{1-\alpha}$  the critical limits,  $\alpha$  the risk level).

313 A VFP-AR [28, 31, 33, 36, pp. 13-16, 53] model having the ability to represent the FOWT (partial) dynamics  
 314 under varying EOCs of any potential WS and damage of any magnitude at the location of interest on a single  
 315 tendon, is identified for each examined tendon. For identifying the VFP-AR model,  $M_3$  response signals are  
 316 obtained for a sample of the considered WSs (the same WSs with those considered in the FP-AR model) and a  
 317 sample of different damage magnitudes on the examined tendon. These sampled WSs and damage magnitudes  
 318 cover the range  $[w_{min}, w_{max}] \times [m_{min}, m_{max}]$  via the discretizations  $w_v \in w_1, w_2, \dots, w_{M_1}$  and  $m_l \in$   
 319  $m_1, m_2, \dots, m_{M_2}$  with  $M_3 = M_1 \times M_2$ . Each signal is characterized by a specific pair of WS  $w_v$  and magnitude  
 320  $m_l$ . Thus, for a pair of WS and damage magnitude, the following operating parameter vector  $\mathbf{k}$  is defined as  
 321  $\mathbf{k} = [w_v \ m_l]^T \Leftrightarrow \mathbf{k}_{v,l}$  with  $v = 1, \dots, M_1$  and  $l = 1, \dots, M_2$  and a pool of  $M_3$  response signals  $y_{\mathbf{k}}[t]$ , each of  
 322 length  $N$ , is obtained with  $t = 1, \dots, N$ .

323 Based on this pool of data, a mathematical description of the structural (partial) dynamics under varying  
 324 EOCs of any potential WS and damage of any potential magnitude on the examined tendon, is obtained through  
 325 a VFP-AR( $na$ ) $_p$  model of the following form [28, 31, 33, 36, pp. 13-16, 53]:

$$326 \quad y_{\mathbf{k}}[t] + \sum_{i=1}^{na} \alpha_i(\mathbf{k}) \cdot y_{\mathbf{k}}[t-i] = e_{\mathbf{k}}[t] \quad \text{with} \quad e_{\mathbf{k}}[t] \sim \text{iid } \mathcal{N}(0, \sigma_e^2(\mathbf{k})) \quad \text{and} \quad \mathbf{k} \in R^2 \quad (6)$$

$$327 \quad a_i(\mathbf{k}) = \sum_{j=1}^p a_{i,j} \cdot G_j(\mathbf{k}) \quad (7)$$

328

329 with  $y_k[t]$  being the response signal and  $e_k[t]$  being the disturbance (residual) signal that is essentially a white  
 330 (serially uncorrelated) zero-mean with variance  $\sigma_e^2(\mathbf{k})$ . Based on Equation (7), the AR parameters  $a_i(\mathbf{k})$  are  
 331 functions of  $\mathbf{k}$  belonging to a  $p$ -dimensional functional subspace spanned by the (mutually independent)  
 332 functions  $G_1(\mathbf{k}), G_2(\mathbf{k}), \dots, G_p(\mathbf{k})$  (functional basis). The latter are bivariate (two variables) orthogonal  
 333 polynomials forming a functional basis  $\mathcal{G}$  [31, 33, 34, 36, p. 28]. Based on the  $M_3$  response signals corresponding  
 334 to the various operating parameter vectors  $\mathbf{k}(\mathbf{k}_{1,1}, \mathbf{k}_{2,1}, \dots, \mathbf{k}_{M_1, M_2})$ , the vector of projection coefficients  $\boldsymbol{\theta}$   
 335 (Equation (6)) is estimated based on the OLS estimator (Equation (5)) (for more details see [33, 36, p. 15]).

336 For the selection of the VFP-AR model orders, the determination of the model's functional subspace  
 337 dimensionality  $p$  and the model validation, the same procedures are followed as in the FP-AR model  
 338 identification (see also in [33, 36, p. 16]).

339 **Remark:** For simplicity of notation, the same symbols  $na, p, \boldsymbol{\theta}$  are commonly used in the FP-AR and VFP-AR  
 340 models without necessarily being equal. They are separately obtained as described in the above identification  
 341 procedures.

## 342 3.2 Inspection phase

343

344 *Step 1: Damage detection.* A response  $y_u[t]$  signal is obtained under the current (unknown) structural state.  
 345 Then the signal is driven through the FP-AR( $na$ ) $_p$  model (Equation (1)) which is re-parametrized in terms of  
 346 the currently unknown state,  $k = w$ :

$$347 \quad y_u[t] + \sum_{i=1}^{na} a_i(k) \cdot y_u[t-i] = e_u[t, k] \quad (8)$$

348

349 The estimation of  $k$  is achieved based on the following Nonlinear Least Squares (NLS) estimator [28, 33,  
 350 36, pp. 16-17, 37, 38] (realized via golden search and parabolic interpolation [54]):

$$351 \quad \hat{k} = \arg \min_{k \in K} \sum_{t=1}^N e_u^2[t, k], \quad \hat{\sigma}_{e_u}^2 = \frac{1}{N} \sum_{t=1}^N e_u^2[t, \hat{k}] \quad (9)$$

352 with  $e_u[t, k]$  provided by Equation (8) and  $K = [w_{min}, w_{max}]$  the boundaries of the examined WS range. The  
 353 estimate  $\hat{k}$  is asymptotically ( $N \rightarrow \infty$ ) normally distributed with mean  $\mu_k$  and variance  $\sigma_k^2$ , that is  $\hat{k} \sim$   
 354  $\mathcal{N}(\mu_k, \sigma_k^2)$ .

355 Then damage detection is accomplished by checking the validity of estimate  $\hat{k}$ . The latter is accepted as valid  
 356 only when the residual signal  $e_u[t, \hat{k}]$  uncorrelatedness (whiteness) is confirmed via the Portmanteau Test [28,  
 357 37, 38] which detects changes in the normalized autocorrelation function  $\rho[\tau]$  ( $\tau = 1, \dots, h$  is the lag) [51, pp.  
 358 21-26] of  $e_u[t, \hat{k}]$ . The Portmanteau Test is based on a Q statistic which is a function of  $\rho[\tau]$  and it follows a  
 359 chi-square distribution  $Q \sim \chi_h^2$ . A signal's whiteness is confirmed only if Q does not exceed the critical limit of  
 360 the distribution,  $Q \leq \chi_{1-\alpha, h}^2$  ( $\chi_{1-\alpha, h}^2$  the critical limit,  $\alpha$  the risk level). The non-acceptance of the  $\hat{k}$  validity  
 361 means that a damage is detected, otherwise the examined structural state is healthy.

362  
 363 *Step 2: Damaged tendon identification.* After the detection of a damage, the signal  $y_u[t]$  is driven through  
 364 each (baseline phase) VFP-AR model (one model per examined tendon; Equation (6)) which is now re-  
 365 parametrized in terms of the currently unknown state,  $\mathbf{k} = [w \ m]^T$ :

$$366 \quad y_u[t] + \sum_{i=1}^{na} a_i(\mathbf{k}) \cdot y_u[t-i] = e_u[t, \mathbf{k}] \quad (10)$$

367  
 368 The estimation of  $\mathbf{k}$  is achieved based on the following Nonlinear Least Squares (NLS) estimator [28, 31,  
 369 33, 36, p. 18]:

$$370 \quad \hat{\mathbf{k}} = \arg \min_{\mathbf{k} \in K} \sum_{t=1}^N e_u^2[t, \mathbf{k}], \quad \hat{\sigma}_{e_u}^2 = \frac{1}{N} \sum_{t=1}^N e_u^2[t, \hat{\mathbf{k}}] \quad (11)$$

371  
 372 with  $e_u[t, \mathbf{k}]$  provided by Equation (10) and  $K = [w_{min}, w_{max}] \times [m_{min}, m_{max}]$  including the boundaries of  
 373 the examined WS and magnitude ranges. The minimization in Equation (11) is achieved via a GA, followed by  
 374 a refinement via Sequential Quadratic Programming (SQP) techniques [55]. The estimate  $\hat{\mathbf{k}}$  is asymptotically  
 375 ( $N \rightarrow \infty$ ) normally distributed with mean  $\mu_k$  and covariance matrix  $\Sigma_k$ , that is  $\hat{\mathbf{k}} \sim \mathcal{N}(\mu_k, \Sigma_k)$ .

The validity of the estimate  $\hat{\mathbf{k}} = [\hat{w} \ \hat{m}]^T$  based on the VFP-AR model for the examined tendon, is accepted only when the uncorrelatedness (whiteness) of the residual signal  $e_u[t, \hat{\mathbf{k}}]$  is confirmed via the Pena-Rodriguez test. The whiteness of the residual signal is confirmed only if the D statistic does not exceed the critical limits of the normal distribution (see subsection 3.1). The acceptance of the validity means that the VFP-AR model is able to represent the structural dynamics under the current damage and that the examined tendon is identified as the damaged tendon. It should be noted that if the above procedure underlines that the estimate  $\hat{\mathbf{k}}$  belongs to two or more tendons, the one with the lowest D statistic is selected as the actual damaged tendon. If  $e_u[t, \hat{\mathbf{k}}]$  is not white then an alternative VFP-AR model (representing a different tendon) shall be checked.

*Step 3. Damage precise quantification.* If the examined tendon has been successfully identified as the damaged tendon, then the estimate  $\hat{\mathbf{k}} = [\hat{w} \ \hat{m}]^T$  is accepted. The estimated magnitude of the examined damage on the identified damaged tendon is  $\hat{m}$  under an estimated WS  $\hat{w}$ . Therefore, confidence intervals for  $\hat{w}$ ,  $\hat{m}$  are constructed [31, 35, 36, p. 18, 37, 38] as:

$$\left[ \hat{w} - t_{1-\frac{\alpha}{2}, N-1} \cdot \hat{\sigma}_w, \hat{w} + t_{1-\frac{\alpha}{2}, N-1} \cdot \hat{\sigma}_w \right], \left[ \hat{m} - t_{1-\frac{\alpha}{2}, N-1} \cdot \hat{\sigma}_m, \hat{m} + t_{1-\frac{\alpha}{2}, N-1} \cdot \hat{\sigma}_m \right] \quad (12)$$

with  $-t_{1-\frac{\alpha}{2}, N-1}$  and  $t_{1-\frac{\alpha}{2}, N-1}$  designating the  $t$  distribution's (with  $N - 1$  degrees of freedom) critical limits,  $\alpha$  the risk level and  $\hat{\sigma}_w, \hat{\sigma}_m$  the square roots of the first and second diagonal components of the estimated covariance matrix  $\hat{\Sigma}_k$  provided by the Cramer-Rao lower bound [31, 33, 36, p. 18].

## 4. Damaged tendon diagnosis method

### 4.1 Baseline phase

An AR(171) model is identified based on a response signal from the healthy structure under WS 11.4 m/s (see details in Table 3). The order of the conventional AR model is adopted as the order of a FP-AR model representing the healthy structural dynamics under varying EOCs of any potential WS.  $M_1 = 4$  response signals

**Table 3.** Details of the FMBM.

<b>Baseline phase</b>								
State	Tendon	Signal length	Estimated model	No. of signals	No. of projection coefficients	Sample per Parameter	Condition number <sup>a</sup>	BIC
Healthy	-	$N=20000$ samples	AR(171)	$M=1$	-	116.59	$5.88 \cdot 10^6$	-8.18
Healthy	-	$N=20000$ samples	FP-AR(171) <sub>4</sub>	$M_1=4$	513	155.94	$2.16 \cdot 10^7$	-32.02
Damaged	6	$N=20000$ samples	VFP-AR(171) <sub>9</sub>	$M_3=40$	1539	519.81	$5.59 \cdot 10^7$	-317.24
Damaged	8	$N=20000$ samples	VFP-AR(171) <sub>9</sub>	$M_3=40$	1539	519.81	$1.81 \cdot 10^8$	-321.48

*Order selection based on an AR model:* Estimation method: OLS, Matlab function: *arx.m*

*Functional subspace dimensionality determination based on Genetic Algorithm:* population=100, elite count 20, crossover fraction=0.7, maximum number of generations=100, Tolerance of the objective function =  $10^{-4}$ ; Matlab function: *ga.m*

*FP-AR(171)<sub>4</sub> model's functional basis:*  $p_1=4$  univariate Shifted Legendre polynomials:  $G_1 = [G_0(k) \ G_1(k) \ G_2(k) \ G_3(k)]^b$

*VFP-AR(171)<sub>9</sub> model's functional basis (tendon 6):*  $p_2=9$  bivariate Shifted Legendre polynomials:

$$G_2 = [G_{0,0}(\mathbf{k}) \ G_{0,1}(\mathbf{k}) \ G_{0,2}(\mathbf{k}) \ G_{1,0}(\mathbf{k}) \ G_{1,1}(\mathbf{k}) \ G_{1,2}(\mathbf{k}) \ G_{2,0}(\mathbf{k}) \ G_{2,1}(\mathbf{k}) \ G_{3,0}(\mathbf{k})]^c$$

*VFP-AR(171)<sub>9</sub> model's functional basis (tendon 8):*  $p_2=9$  bivariate Shifted Legendre polynomials:

$$G_2 = [G_{0,0}(\mathbf{k}) \ G_{0,1}(\mathbf{k}) \ G_{0,2}(\mathbf{k}) \ G_{1,0}(\mathbf{k}) \ G_{1,1}(\mathbf{k}) \ G_{2,0}(\mathbf{k}) \ G_{2,1}(\mathbf{k}) \ G_{3,0}(\mathbf{k}) \ G_{3,9}(\mathbf{k})]^c$$

*Validation method:* Pena-Rodriguez test with risk levels  $\alpha = 4 \times 10^{-1}$  (FP-AR(171)<sub>4</sub> model),  $\alpha = 4.4 \times 10^{-1}$  (VFP-AR(171)<sub>9</sub> model – tendon 6),  $\alpha = 4.4 \times 10^{-1}$  (VFP-AR(171)<sub>9</sub> model – tendon 8) & no. of lags = 2100

### Inspection phase – Step 1: Damage detection

*FP-AR model based estimation of  $k$ :* NLS estimator based on golden search & parabolic interpolation (Tolerance of the objective function =  $10^{-10}$ ; Tolerance of the estimated value =  $10^{-10}$ ; Matlab function: *fminbnd.m*)

*Validation method:* Portmanteau test with no. of lags = 950

### Inspection phase – Step 2: Damaged tendon identification & Step 3: Damage precise quantification

*VFP-AR models based estimation of  $\mathbf{k}$ :* NLS estimator based on Genetic Algorithm (tolerance of the objective function =  $10^{-10}$ ; Matlab function: *ga.m*) and Sequential Quadratic Programming (tolerance of the objective function =  $10^{-10}$ ; tolerance of the estimated value =  $10^{-10}$ ; Matlab function: *fmincon.m*).

*Validation method:* Pena-Rodriguez test with no. of lags = 2100

<sup>a</sup> Condition number of  $\sum_{t=1}^N \Phi^T[t] \Phi[t]$  in Equation (5).

<sup>b</sup>  $G_i(k)$  : univariate orthogonal polynomial of degree  $i$ .

<sup>c</sup>  $G_{i,j}(\mathbf{k})$  : bivariate orthogonal polynomial of total degree  $i+j$ , obtained as tensor product from two univariate polynomials  $G_i(w)$ ,  $G_j(m)$  of degrees  $i, j$ , respectively.

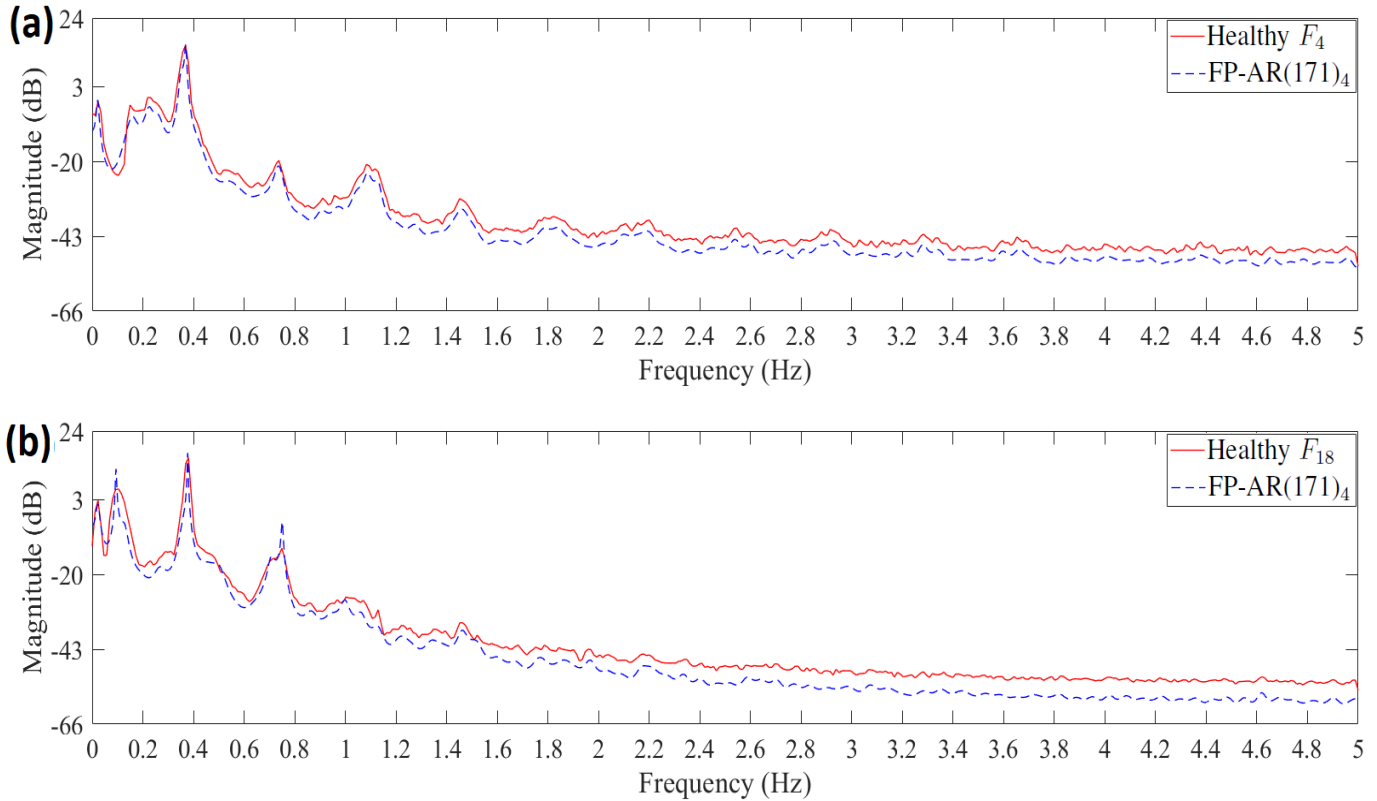
are used for identifying a FP-AR model with WS considered in the WS range  $w_v \in [4, 25]$  m/s and the range covered via the discretization  $w_v \in [4, 11.4, 18, 25]$  m/s (see subsection 3.1). The FP-AR model's functional subspace dimensionality  $p_1$  is determined via a GA-based procedure based on the minimization of BIC. The initial functional subspace is selected to be spanned by 4 univariate Shifted Legendre polynomials which are functions of the WS  $w_v$  normalized with respect to the maximum value that is  $w_v = w_v/25 \in [0, 1]$ .

The identification procedure leads to a FP-AR model. A comparison between the Welch-based (Welch estimation details: Matlab function *pwelch.m*; signal length 20000 samples, window 868 samples, 95% overlap, Hamming window, frequency resolution of 0.011 Hz) and the FP-AR model's PSD estimates, is presented in Figure 7. The agreement between the PSDs shows the high accuracy in modelling the healthy structural dynamics under varying EOCs. The dependence of an indicative FP-AR model parameter as a function of WS, is depicted in Figure 8(a). The FP-AR model based PSD magnitude as a function of frequency and WS, is depicted in Figure 8(b). Full details on the FP-AR model identification are presented in Table 3.

Subsequently, for each examined tendon,  $M_3 = 40$  response signals are used for identifying a VFP-AR model. This model represents the structural dynamics under varying EOCs of any potential WS in the WS range  $w_v \in [4, 25]$  m/s and under any damage magnitude on the tendon in the damage magnitude range  $m_l \in [10, 100]$  % (see subsection 3.1). The WS range is covered via the discretization  $w_v \in [4, 11.4, 18, 25]$  m/s and the magnitude range is covered via the discretization  $m_l \in [10, 20, 30, \dots, 80, 90, 100]$  %. The AR model order is selected based on the AR(171) model. Then the dimensionality of the functional subspace  $p_2$  of the VFP-AR model, is determined via a GA-based procedure based on the minimization of BIC. The initial functional subspace is spanned by 40 bivariate Shifted Legendre polynomials which are functions of the WS  $w_v$  and the magnitude  $m_l$  normalized with respect to the corresponding maximum values that are  $w_v = w_v/25 \in [0, 1]$  and  $m_l = m_l/100 \in [0, 1]$ .

Two VFP-AR models are identified for tendons 6 and 8. The dependence of indicative VFP-AR models parameters as a function of WS and damage magnitude, is depicted in Figure 9. PSD magnitudes of the

two VFP-AR models as a function of frequency and WS, are depicted in Figures 10(a),(b) and of frequency and damage magnitude in Figure 10(c),(d). Full details on the VFP-AR models identification are presented in Table 3.

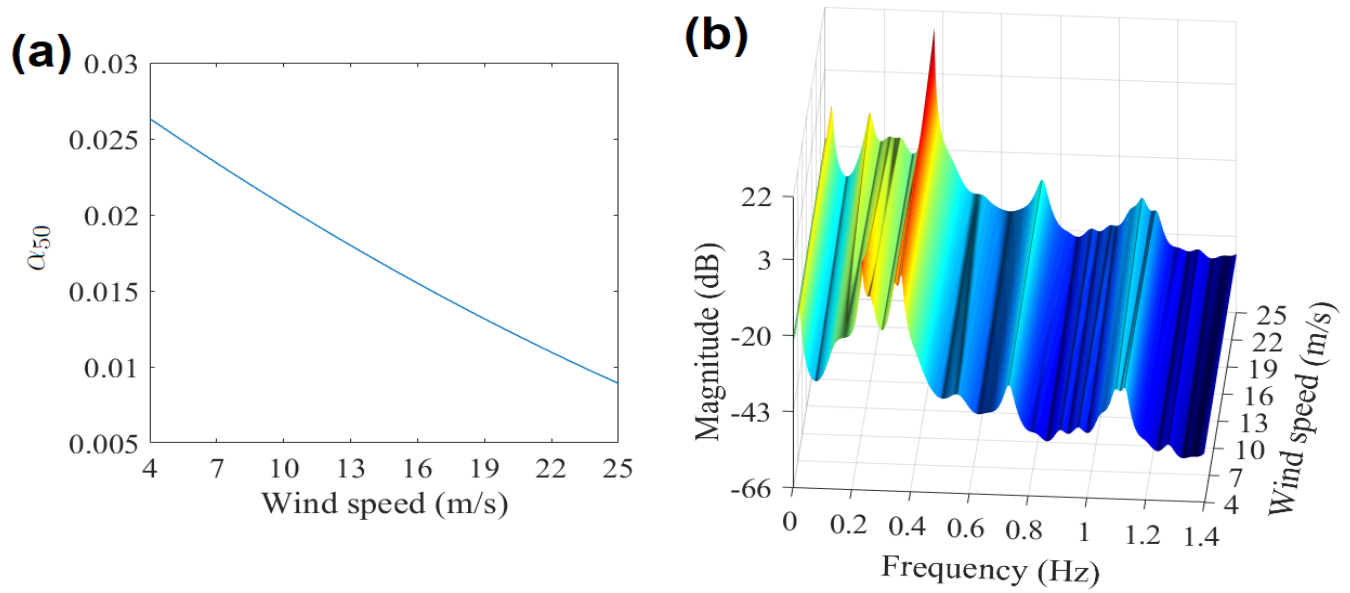


**Figure 7.** (a) Welch based PSD estimate (—) for the healthy state  $F_4$  and the FP-AR model's PSD estimate (---); (b) Welch based PSD estimate (—) for the healthy state  $F_{18}$  and the FP-AR model's PSD estimate.

## 4.2 Inspection phase

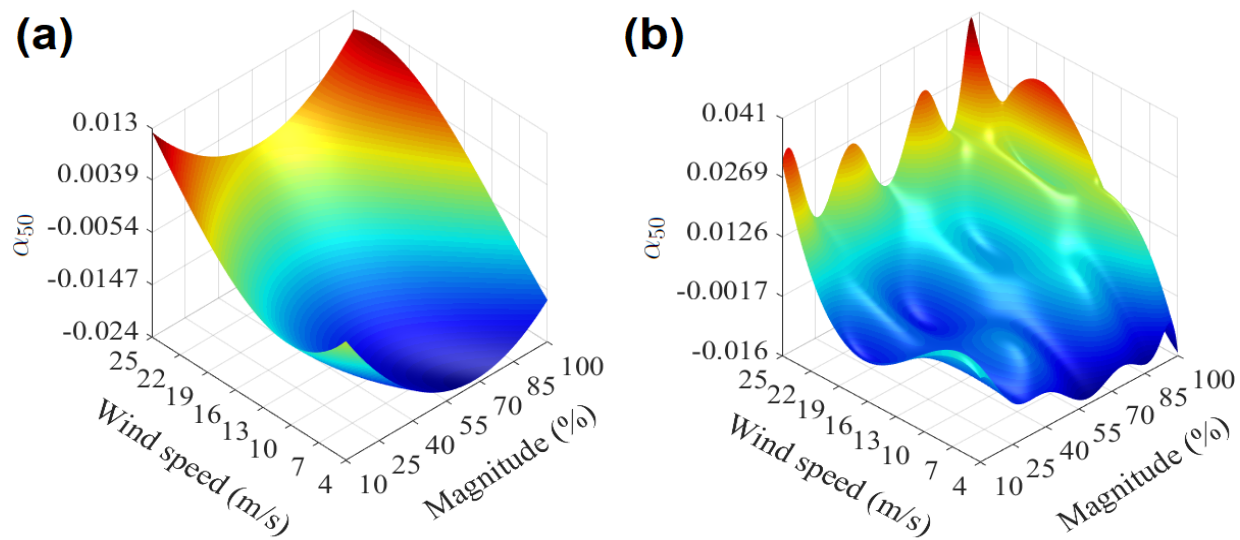
*Step 1: Damage detection.* A response signal corresponding to an unknown structural state is driven through the FP-AR model which is re-parametrized in terms of  $k$  (Equation (8)). Then  $k$  is estimated based on the NLS estimator of Equation (9) which searches for the estimate  $\hat{k}$  leading to the minimum of the estimation criterion. Finally, damage detection is achieved through the corresponding Q statistic based on the normalized autocorrelation of  $e_u[t, \hat{k}]$  (Matlab function: *autococorr.m*; see subsection 3.2 and details in Table 3). Thus, it

442 is checked if the model trained to describe healthy dynamics under varying EOCs, is able to describe the current  
 443 unknown dynamics as well.



444

445 **Figure 8.** (a) Indicative AR parameter of the FP-AR model as function of WS and (b) PSD magnitude  
 446 of the FP-AR model as function of frequency and WS.

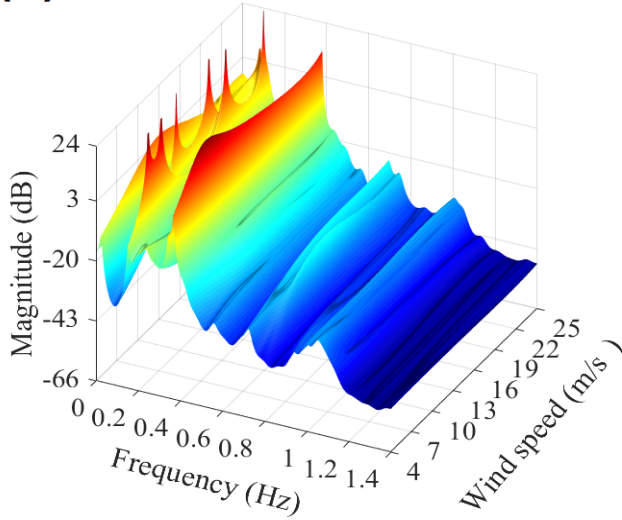
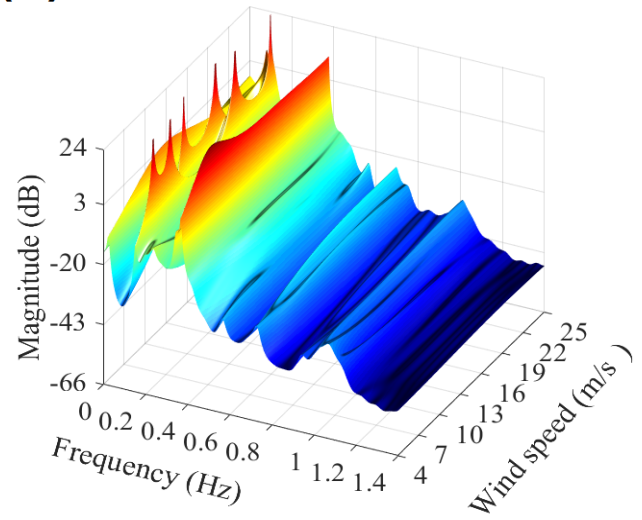
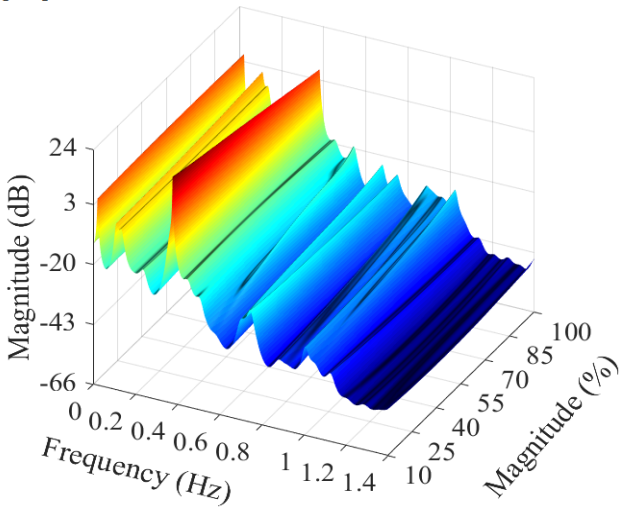
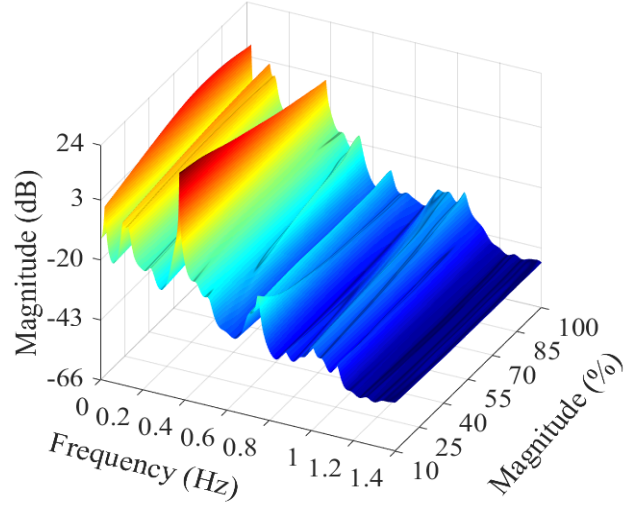


447

448 **Figure 9.** (a) Tendon 6 - VFP-AR model and (b) Tendon 8 - VFP-AR model indicative AR  
 449 parameter as function of WS and damage magnitude.

450



**(a)** Tendon 6 - Magnitude=30 %**(b)** Tendon 8 - Magnitude=30 %**(c)** Tendon 6 - Wind speed=11.4 m/s**(d)** Tendon 8 - Wind speed=11.4 m/s

451

452 **Figure 10.** PSD magnitudes of the two VFP-AR

models representing the structural dynamics under

453 damaged tendons 6, 8 as function (a),(b) of frequency and WS and (c),(d) of frequency and damage magnitude.

454

455 39 healthy and 394 damage cases are examined (see Table 2) with the damage detection results presented

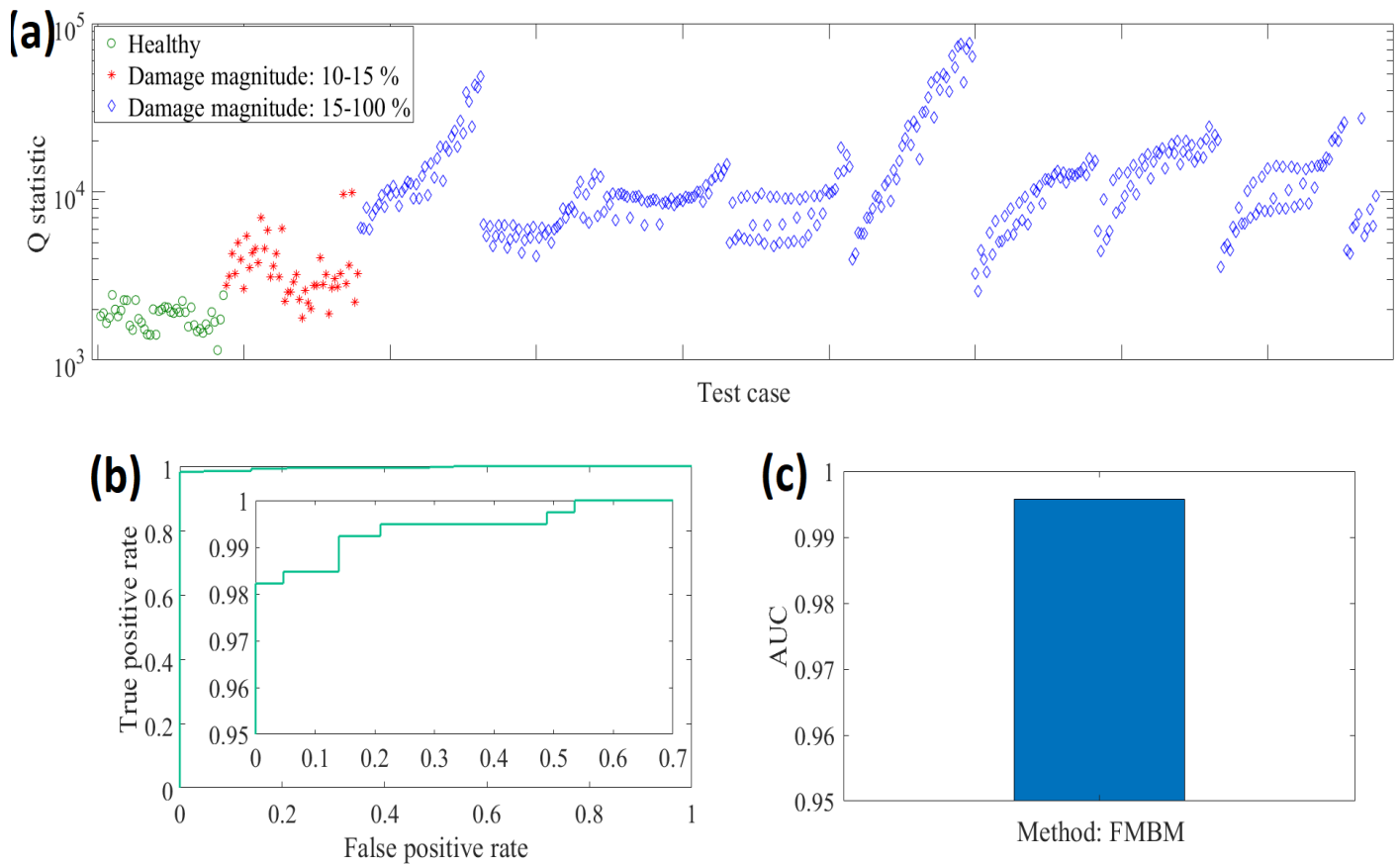
456 through the corresponding Q statistics in Figure 11(a). It must be noted that the Q statistics corresponding to 7

457 damage cases of magnitude [10-15] % from tendon 8, are not separable from the Q statistics corresponding to

458 healthy cases. This happens due to the effects of the varying EOCs on the healthy FOWT dynamics, fully

459 'masking' the effects of damages of magnitude [10-15] % (see subsection 2.4).

460 The damage detection results are also presented through a Receiver Operating Characteristic (ROC) curve  
 461 (Figure 11(b)) and the Area Under the ROC Curve (AUC) (Figure 11(c)). The ROC curve represents the true  
 462 positive rate (percentage of damages detected correctly) versus the false positive rate (percentage of false alarms)  
 463 for varying decision threshold, with the perfect detection (no false alarms or missed damages) confirmed when  
 464 the ROC curve includes the (0,1) point (Matlab function: *perfcurve.m*) [56, 57]. The AUC ranges from 0 to 1  
 465 with values close to 1 indicating great performance and values close to 0.5 poor performance (Matlab function:  
 466 *perfcurve.m*) [57]. In Figure 11(b), the ROC curve is very close to the best possible point (0,1) with the true  
 467 positive rate (correct detection rate) being 98.2 % for false positive rate (false alarm rate) equal to 0 %. The 1.8  
 468 % missed damages correspond to the aforementioned 7 damages of magnitude [10-15] %. In Figure 11(c), the  
 469 AUC is 0.9957. The ROC and AUC based results are excellent and they show that damage detection in the  
 470 tendons of a FOWT under varying EOCs, is almost perfect.



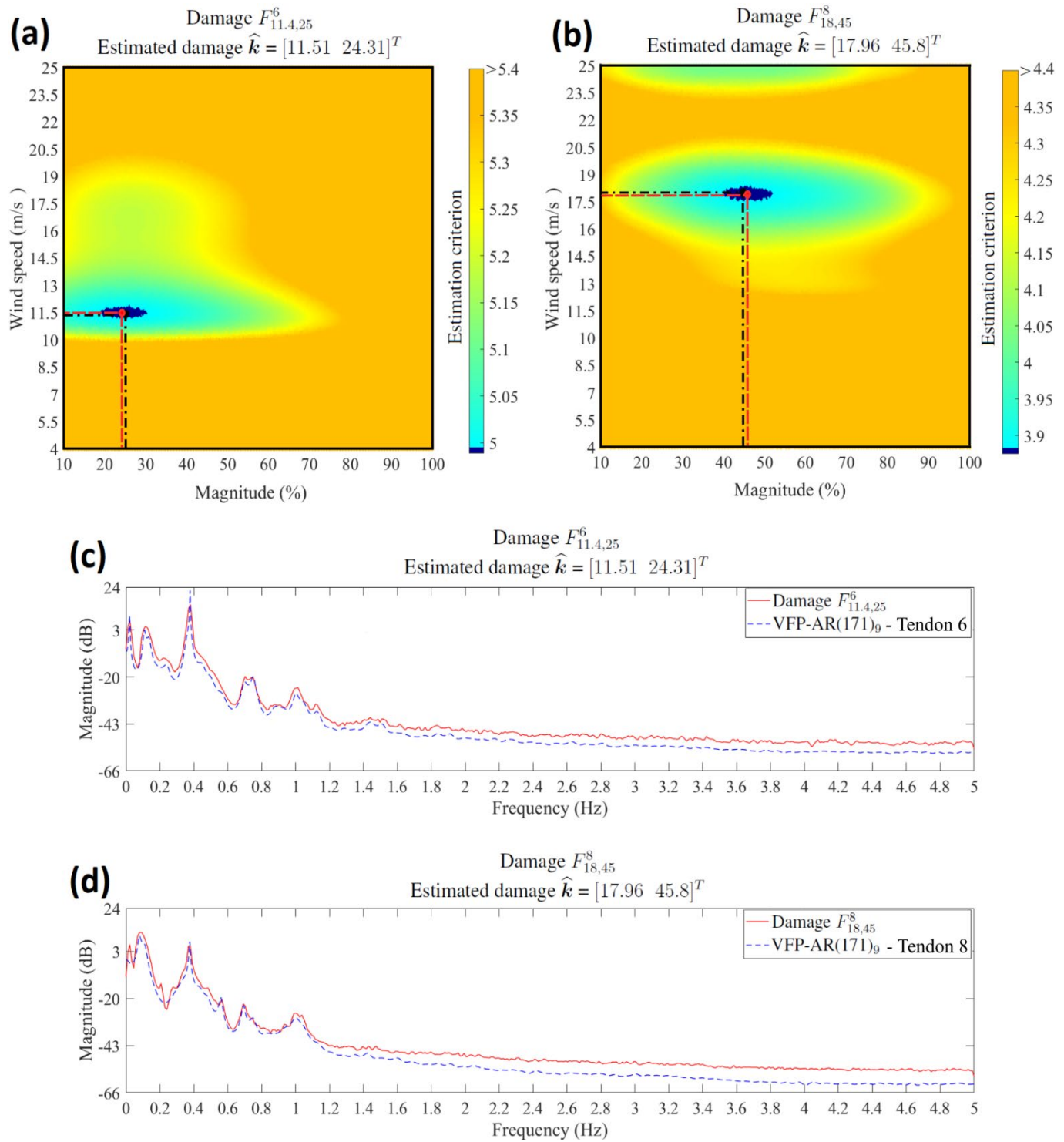
471

472 **Figure 11.** Damage detection performance of the FMBM: (a) the method's Q statistic, (b) the ROC curve and  
 473 (c) the AUC value (39 healthy and 394 damage cases).

474 *Step 2: Damaged tendon identification.* When a damage is detected, damaged tendon identification starts.  
 475 The response signal corresponding to the unknown detected damage, is driven through each considered baseline  
 476 VFP-AR model which is re-parametrized in terms of  $\mathbf{k}$  (Equation (10)). Based on each re-parametrized  
 477 model, the NLS estimator of Equation (11) obtains the estimate  $\hat{\mathbf{k}}$  (see details in Table 3). Then the identification  
 478 of damaged tendon is achieved through the D statistic based on the partial autocorrelation of  $e_u[t, \hat{\mathbf{k}}]$  (Matlab  
 479 function: *parcocorr.m*; see subsection 3.2 and Table 3).

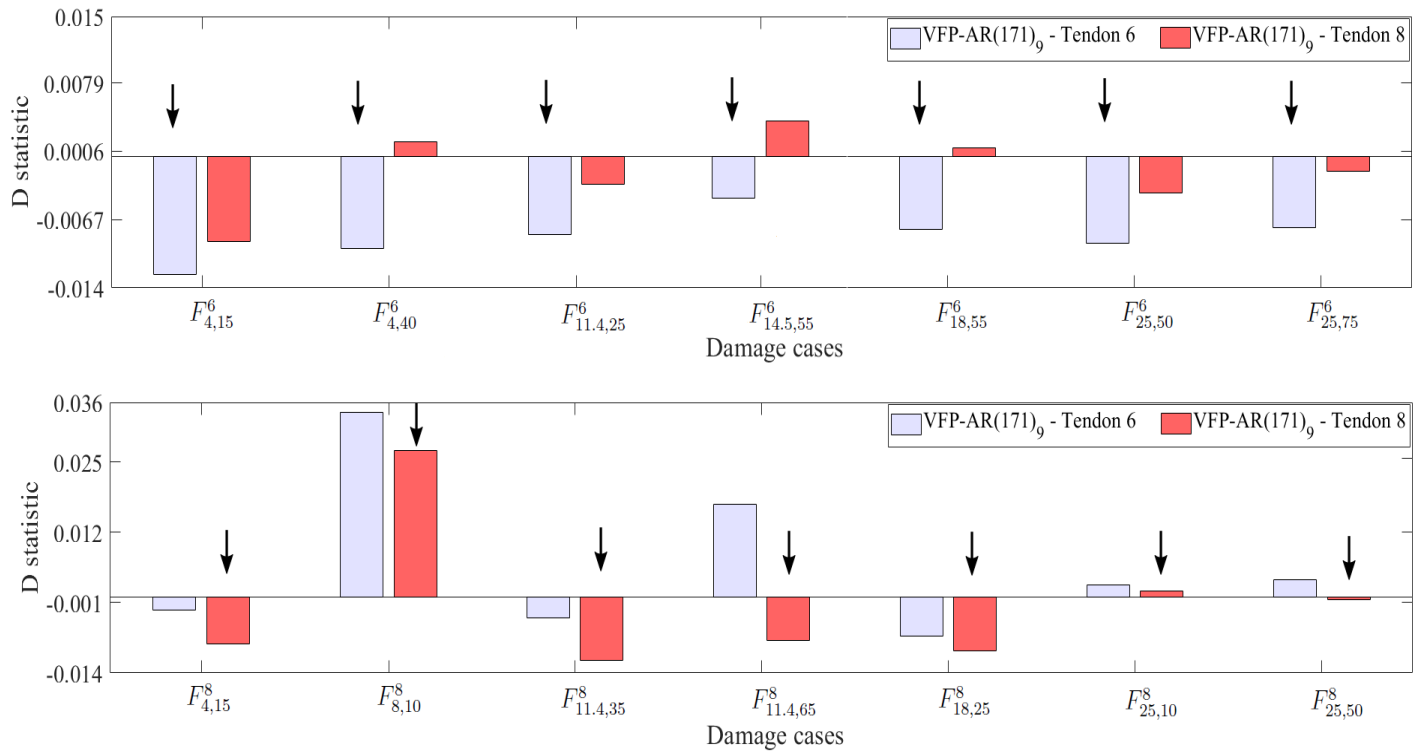
480 In Figure 12 (a),(b), estimation of  $\mathbf{k}$  results are presented for two damage cases from tendons 6, 8. For  
 481 each damage case, the  $\mathbf{k}$  estimation is presented based only on the VFP-AR model of the actual  
 482 tendon. The NLS computes the estimation criterion while searching for the minimum criterion value (criterion  
 483 values are color coded with the darkest value corresponding to the minimum) on the examined range. Evidently,  
 484 the actual WS  $w$  and magnitude  $m$  and their estimates  $\hat{w}$ ,  $\hat{m}$  are very close, practically coinciding with  
 485 each other. Moreover, for each damage case, the agreement of the VFP-AR model based PSD  
 486 with its Welch-based counterpart in Figure 12(c),(d), shows the high accuracy in modelling the damaged  
 487 structural dynamics under varying EOCs through the selected VFP-AR model.

488 Due to the fact that the considered damages in this study affect the FOWT dynamics in a highly similar way  
 489 (see subsection 2.4), damaged tendon identification is achieved through the Portmanteau test by selecting the  
 490 tendon with the lowest D statistic. Indicative damaged tendon identification results based on damage cases from  
 491 tendon 6 and 8, are provided in Figure 13 and it is evident that the lowest D statistic leads to the identification  
 492 of the actual damaged tendon. In this step, the total number of 387 damage cases is considered (the 7 undetected  
 493 damages are excluded from the 394 damage cases examined in *step 1*), 197 cases from tendon 6 and 190 cases  
 494 from tendon 8. Damaged tendon identification is achieved successfully in 184 damage cases from tendon 6 with  
 495 a success rate of 93.4 % and in 188 damage cases from tendon 8 with a success rate of 98.94 %. The no-  
 496 identification of the actual tendon for the 15 damage cases, happens due to the fact that damages on different  
 497 tendons similarly affect the platform's structural dynamics (see subsection 2.4). The total success rate 96.12 %



498

499 **Figure 12.** Indicative estimation of  $k$  results for two damage cases: (a), (c)  $F_{11.4,25}^6$  and (b), (d)  $F_{18,45}^8$ . (a), (b)  
500 The estimation criterion values are shown using a color code (the darkest color indicating minimum, and thus  
501 the estimated damage magnitude). The actual WS and damage magnitude (---) and their estimates (· - · - ·)  
502 are also numerically provided over each plot. (c), (d) Welch-based PSD magnitude for the considered WS and  
503 damage magnitude (—) compared to that of the VFP-AR model (---).



504

505 **Figure 13.** Indicative damaged tendon identification results for 14 damage cases. The actual structural state is  
 506 presented below each pair of bars. The dark arrow shows the tendon selected as the actual damaged tendon in  
 507 each case.

508

509 The fact that there are 372 from the 387 damage cases is very high and this shows that damaged tendon  
 510 identification in a FOWT is achievable in spite of the effects of the varying EOCs and the similarity between  
 511 the effects of the considered damages. An overview of the corresponding results is provided in Table 4.

512

513

**Table 4.** Damaged tendon identification and damage precise quantification results.

Step 2: Damaged tendon identification			Step 3: Damage precise quantification	
Tendon	Model	Identification	Quantification error	Quantification error
			for wind speed	for damage magnitude
			(sample mean $\pm$ std)	(sample mean $\pm$ std)
6	VFP-AR(171) <sub>9</sub>	184/197 (93.4 %)	0.19 $\pm$ 0.64 (m/s)	4.21 $\pm$ 3.02 (%)
8	VFP-AR(171) <sub>9</sub>	188/190 (98.94 %)	0.17 $\pm$ 0.6 (m/s)	4.06 $\pm$ 2.90 (%)

518

519

520 *Step 3. Damage precise quantification.* After the identification of the damaged tendon, the corresponding  
 521 estimate  $\hat{k}$  (Equation (11)) is accepted and the confidence intervals are constructed (Equation (12)).

522 Indicative damage precise quantification results in terms of WS and damage magnitude estimates and  
 523 confidence intervals, are provided in Figure 14. It is obvious that damage precise quantification is achieved at  
 524  $\alpha = 1 \times 10^{-2}$  as the estimated and the actual WSs and damage quantities are very close, with the actual values  
 525 being within or just outside of the obtained confidence intervals. A summary of all damage precise  
 526 quantification results based on the 372 considered damage cases (the 15 unidentified damages are excluded  
 527 from the 387 damage cases examined in *step 2*), is presented in Table 4 and Figure 15. The quantification error  
 528 for WS is the error between the actual WS  $w$  and its estimate  $\hat{w}$ , whereas the quantification error for damage  
 529 magnitude is the error between the actual damage magnitude  $m$  and its estimate  $\hat{m}$ . In Figure 15 where the  
 530 distribution of the quantification error for damage magnitude is presented based on the 372 cases, the error  
 531 remains smaller than 9 % for 91.31 % of the 184 cases from tendon 6 and for 92.01 % of the 188 cases from  
 532 tendon 8. The mean quantification errors for magnitude are 4.21 % for tendon 6 and 4.06 % for tendon 8 and  
 533 the mean errors for WS for tendons 6 and 8 are close to 0 (Table 4). These errors are quite small for large  
 534 structures such as a FOWT operating under varying EOCs and damages affecting the structural dynamics in a  
 535 similar manner. They show that damage precise quantification under varying EOCs, can be achieved with a  
 536 high precision.

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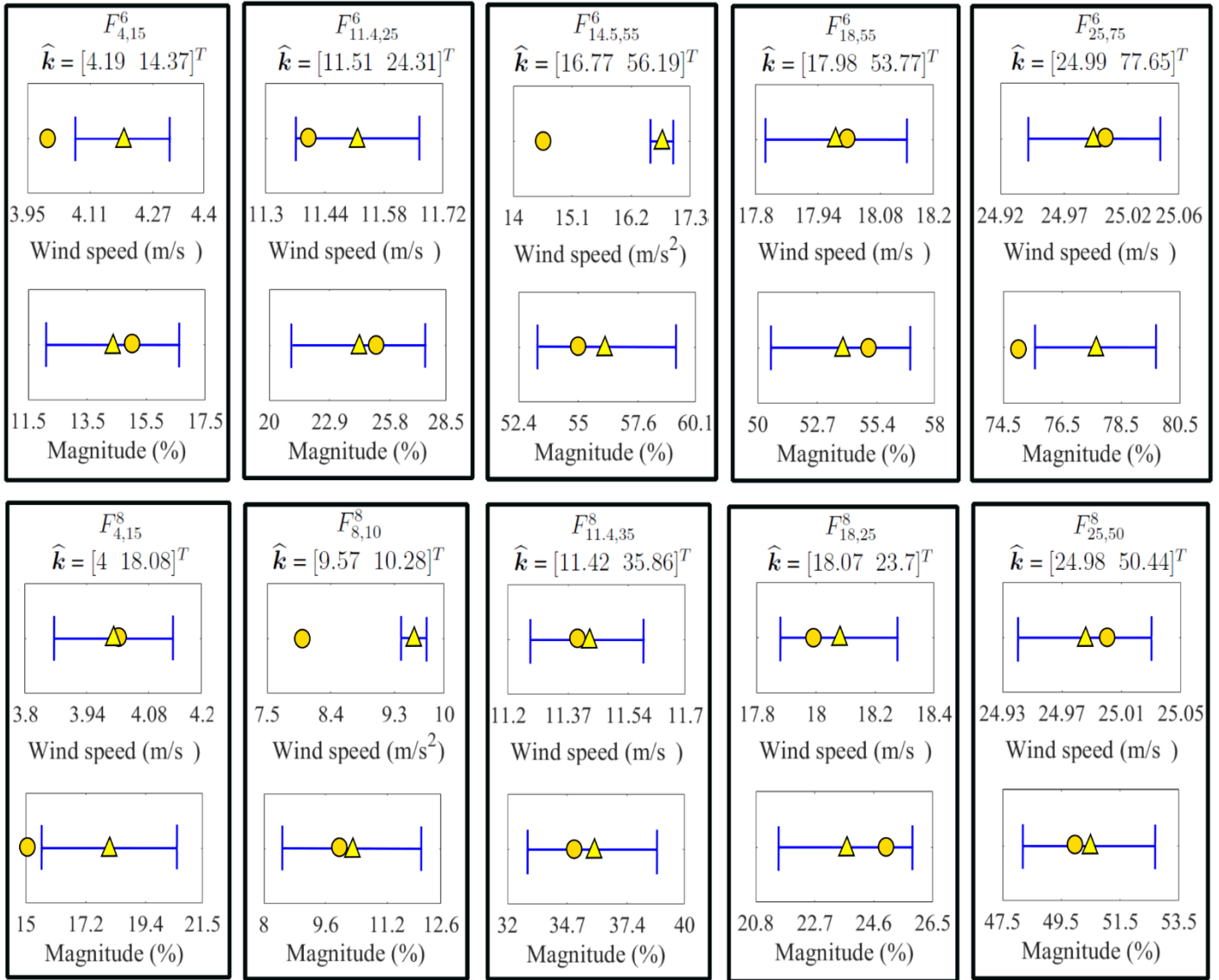
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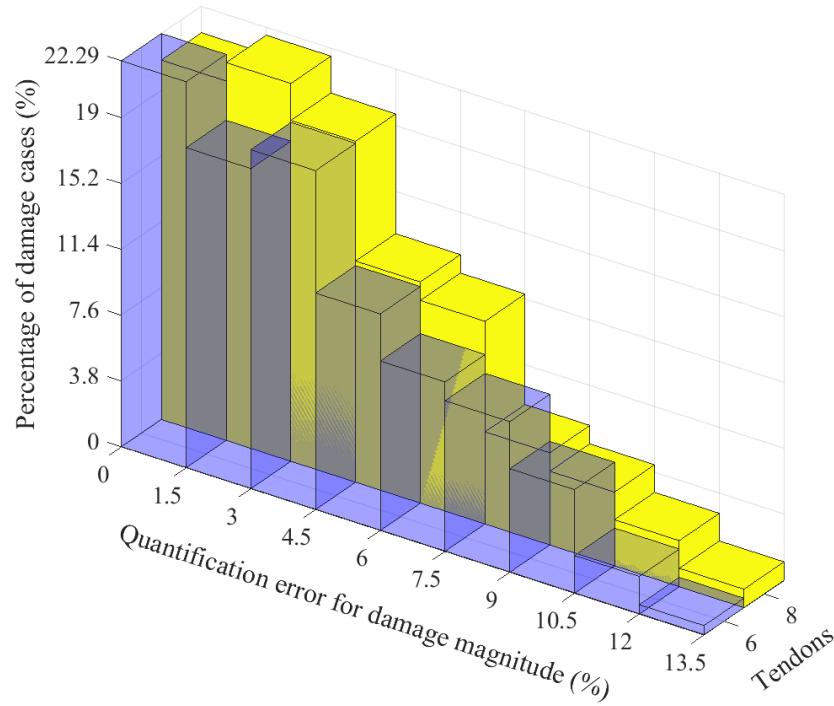
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545

546 **Figure 14.** Indicative damage precise quantification results for 10 damage cases (● : true WS / damage  
547 magnitude; ▲ : point estimate; ┃ : confidence interval). The true and estimated WS and damage magnitude  
548 are numerically provided above each plot.



549

550 **Figure 15.** Damage precise quantification results in terms of the quantification error for damage magnitude (%)  
 551 which is the error between the actual and its estimated damage magnitude (184 damage cases based on tendon  
 552 6 and 188 damage cases based on tendon 8).

553

## 554 5. Conclusions

555 The combined problem of damage detection, damaged tendon identification and damage precise  
 556 quantification in a new type of a FOWT under varying EOCs has been investigated for the first time through  
 557 the novel FMBM. The method has been formulated to operate using a single response signal from the FOWT  
 558 received via a single sensor instead of two signals received via two sensors as in the method's previous version.  
 559 The examined structure is a new concept of FOWT with its tower supported by an improved version of the  
 560 multibody floating TELWIND platform that consists of two tanks connected via 12 tendons. The FOWT has  
 561 been subjected to varying EOCs corresponding to seven different WSs and irregular SWHs and current of  
 562 constant speed and direction, thus reflecting normal and the most severe EOCs of the selected site located in the  
 563 northern coast of Scotland. The formulated FMBM has been based on FMs where only the WS have been  
 564 considered as an operating parameter due to the dependence of SWH on WS. Thus, the FMs have represented



565 the structural dynamics under varying EOCs of any potential WS and under any magnitude of the considered  
566 damages.

567 Various damage scenarios have been simulated via the stiffness reduction (%) at the tendon's connection  
568 point to the upper tank of the platform. Two out of the total 12 tendons have been examined. A numerical  
569 coupled model of the FOWT has been used for the simulation of the healthy and damaged structure under  
570 varying EOCs. Surge acceleration signals have been collected from the upper tank of the platform, within a  
571 limited bandwidth of low frequencies in the range [0-5] Hz corresponding to realistic operating conditions under  
572 physical excitation. Furthermore, it is observed that the tendons intersect each other and form an "x-cross"  
573 connection. Thus, the caused interference between the crossing tendons is capable of creating wears and it is  
574 recommended the effect to be further investigated.

575 The FMBM has been applied under challenging conditions corresponding to i) effects of the varying EOCs  
576 on the healthy FOWT, fully "masking" the effects damages of magnitude less than 20 %, ii) small effects of  
577 damages of magnitude [20-80] %, on the dynamics due to the high number and robustness of the existing  
578 tendons, iii) damages of magnitude [20-80] % on the one tendon under constant WS, having similar effects on  
579 the structural dynamics and iv) damages of magnitude [10-100] % on different tendons, having similar effects  
580 on the structural dynamics.

581 The main achievements of the study, are presented below:

- 582 • The modeling of the healthy structural dynamics under varying EOCs of any potential WS in the  
583 continuous WS range of [4-25] m/s, has been realized via a single, data-based, response-only, FP-AR  
584 model.
- 585 • More advanced VFP-AR models with an operating parameter vector that includes varying EOCs of any  
586 potential WS and damage of any magnitude at a tendon's connection point, have been employed for the  
587 representation of the structural dynamics under damage and varying EOCs.

- 588 • Damage detection has been remarkable with correct detection for 98.2 % of the considered damage cases  
 589 (394) and zero false alarms achieved. This achievement has happened in spite of the subtle nature of the  
 590 considered damages causing slight changes on the structural dynamics and the effects of EOCs on the  
 591 dynamics being confused with the effects of the damages.
- 592 • Damaged tendon identification, that is the determination of the specific tendon that is damaged, has been  
 593 achieved for 96.12 % of the damage cases (387). This has been, independent from the fact that there has  
 594 been great similarity in the effects caused to the structural dynamics by the considered damages on the  
 595 different tendons and the difficulty added by the varying EOCs.
- 596 • The mean error in damage precise quantification has been approximately 4% in terms of tendon stiffness  
 597 reduction for both tendons and all considered cases (372). The obtained damage magnitude confidence  
 598 intervals have included in most cases (or they are too close) the actual damage magnitude. Based on this  
 599 along with the previously mentioned difficulties of the subtle damages and the varying EOCs, the  
 600 obtained damage precise quantification results have been judged as very good.
- 601 • This study has confirmed that advanced stochastic methods such as the FMBM can successfully perform  
 602 SHM under varying EOCs and achieve complete diagnosis of damages in FOWTs' tendons, using  
 603 limited (even a single) vibration measurements.

604

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