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## Article

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# Photometry and astrometry with JWST - III. A NIRCam-Gaia DR3 analysis of the open cluster NGC 2506 

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#### Abstract

In the third paper of this series aimed at developing the tools for analysing resolved stellar populations using the cameras on board of the James Webb Space Telescope (JWST), we present a detailed multiband study of the 2 Gyr Galactic open cluster NGC 2506. We employ public calibration data sets collected in multiple filters to: (i) derive improved effective Point Spread Functions (ePSFs) for 10 NIRCam filters; (ii) extract high-precision photometry and astrometry for stars in the cluster, approaching the main sequence (MS) lower mass of $\sim 0.1 \mathrm{M}_{\odot}$; and (iii) take advantage of the synergy between $J W S T$ and Gaia DR3 to perform a comprehensive analysis of the cluster's global and local properties. We derived a MS binary fraction of $\sim 57.5$ per cent, extending the Gaia limit $\left(\sim 0.8 \mathrm{M}_{\odot}\right)$ to lower masses $\left(\sim 0.4 \mathrm{M}_{\odot}\right)$ with $J W S T$. We conducted a study on the mass functions (MFs) of NGC 2506, mapping the mass segregation with Gaia data, and extending MFs to lower masses with the JWST field. We also combined information on the derived MFs to infer an estimate of the cluster present-day total mass. Lastly, we investigated the presence of white dwarfs (WDs) and identified a strong candidate. However, to firmly establish its cluster membership, as well as that of four other WD candidates and of the majority of faint low-mass MS stars, further JWST equally deep observations will be required. We make publicly available catalogues, atlases, and the improved ePSFs.


Key words: techniques: image processing - techniques: photometric - astrometry - Hertzsprung-Russell and colour-magnitude diagrams-Galaxy: open clusters and associations: individual: NGC 2506.

## 1 INTRODUCTION

When we observe a Galactic stellar cluster, whether it is open or globular, it is like looking at a snapshot of stars with different masses but approximately the same initial chemical composition, age, and distance. By studying stellar clusters with varying chemical compositions and ages ranging from a few tens of Myr up to $\sim 10-$ 13 Gyr , we can gain insights into the processes involved in the formation and evolution of stars with different mass and metallicity. Optical and UV studies using data from the Hubble Space Telescope (HST) have led to the discovery of several phenomena that were previously unknown, such as, for example, the existence of multiple stellar populations in globular clusters (see e.g. Bedin et al. 2004; Piotto et al. 2007, 2015), and the unusual shape of some stellar clusters' white dwarf cooling sequences (e.g. Bedin et al. 2008; Bellini et al. 2013). However, with few exceptions (see, e.g.King et al. 2005; Richer et al. 2008; Dieball et al. 2016), observations of open and globular clusters have been primarily focused on main-sequence (MS) stars with masses $\gtrsim 0.1 \mathrm{M}_{\odot}$, and it has been challenging to study stars near the hydrogen burning limit (HBL) and the brown

[^0]dwarf sequence. In this regard, infrared (IR) photometry plays a crucial role in providing information about low-mass (pre-)MS stars ( $M \lesssim 0.1-0.2 \mathrm{M}_{\odot}$ ) and brown dwarfs in stellar clusters (Nardiello, Griggio \& Bedin 2023).

Since July 2022, the JWST (Gardner et al. 2023) has been acquiring a vast amount of IR data through its cameras, revolutionizing our understanding of the Universe. Public Director's Discretionary-Early Release Science and Calibration JWST data constitute a treasure for improving data reduction techniques and at the same time yield scientifically significant results (see e.g. Nardiello et al. 2022; Griggio, Nardiello \& Bedin 2023b, hereafter Paper I and II, respectively). Currently, non-proprietary data in the archive encompass observations of high-redshift galaxies (e.g. Naidu et al. 2022) and galaxy clusters (e.g. Paris et al. 2023), resolved close dwarf galaxies and portions of the Large Magellanic Cloud (LMC; e.g. Paper II; Libralato et al. 2023), Galactic stellar clusters (e.g. Paper I; Ziliotto et al. 2023), individual stars and exoplanets (e.g. Feinstein et al. 2023), and objects of the Solar System (e.g. de Pater et al. 2022).

In this study, we took advantage of the publicly available calibration observations to conduct an IR multiband investigation of the lower MS stars in the open cluster NGC 2506. The data were collected with the JWST Near Infrared Camera (NIRCam, Rieke et al. 2023) as part of the calibration programme CAL-1538 (PI: Gordon). The


Figure 1. The $J W S T$ filters and ePSFs used in this work. Top panel shows the NIRCam $+J W S T$ total throughputs for the 10 filters adopted in this work. The lower panels show the ePSFs in the central region of the detector A1 (SW channel, middle row) and ALONG (LW channel, bottom row) for all the filters used in this work.
primary objective of this programme is to acquire observations of G dwarf stars for the flux calibration of JWST filters. Additionally, we utilized data from the CAL-1476 programme (PI: Boyer) targeting stars in the LMC to derive effective Point Spread Functions for nearly all available NIRCam filters, spanning a wavelength range from $\sim 0.7$ to $\sim 4.5 \mu \mathrm{~m}$.

The open cluster NGC 2506 is particularly interesting since it belongs to the (small) sample of metal-poor $([\mathrm{Fe} / \mathrm{H}] \lesssim-0.1)$, old-age ( $\gtrsim 1$ Gyr) open clusters located at the Galactic anticentre, at $\sim 3 \mathrm{kpc}$ from the Sun (McClure, Twarog \& Forrester 1981; Cantat-Gaudin \& Anders 2020); similar clusters in this category include NGC 2420 and NGC 2243 (Anthony-Twarog, Atwell \& Twarog 2005; AnthonyTwarog et al. 2006). NGC 2506 has been the subject of several studies to determine its age and metallicity (Carretta et al. 2004; Mikolaitis et al. 2011; Anthony-Twarog, Deliyannis \& Twarog 2016; Knudstrup et al. 2020), analyse the evolution of surface lithium abundances (Anthony-Twarog et al. 2018), investigate its structural parameters (Lee, Kang \& Ann 2013; Rangwal et al. 2019; Gao 2020), and identify binary systems and blue straggler stars (Arentoft et al. 2007; Panthi et al. 2022). There have been some discrepancies among these studies regarding the age and metallicity of the cluster members, although all analyses provide an age range between 1 and 3 Gyr and classify the cluster members as highly metal-deficient, with an upper limit of $[\mathrm{Fe} / \mathrm{H}]$ around -0.2 (Netopil et al. 2016). From a
dynamical perspective, NGC 2506 is of significant interest. Several studies suggest that the cluster is dynamically relaxed, displaying clear evidence of mass segregation, evaporation of low-mass stars, and even hints of tidal tails (Lee et al. 2013; Rangwal et al. 2019; Gao 2020).

In this work, we investigate all these aspects of this peculiar open cluster, by combining JWST photometry and astrometry with Gaia DR3 (Gaia Collaboration 2021) and ground-based data. Section 2 reports the technical part of this work; it includes a description of the adopted space and ground-based observations, the description of the procedure to derive the effective point spread functions (ePSFs), and the data reduction. Section 3 describes the photometric and astrometric properties of the stars, while Section 4 includes the derivation of the radial stellar density profile of the cluster and its structural parameters. Section 5 reports in detail the analysis of the MS binary fraction and of the mass functions (MFs) extracted from both JWST and Gaia data, while Section 6 discusses the candidate white dwarfs we found. A summary is reported in Section 7.

## 2 OBSERVATIONS AND DATA REDUCTION

In this section, we report a description of the JWST data used in this work and the procedures adopted to derive ePSFs and the astro-photometric catalogues of NGC 2506. We also describe how


Figure 2. An overview of the improvements in the ePSF models during the different iterations. The top-to-bottom panels display the results for iterations 1,10 , and 30 , respectively. The left and middle columns show the distributions of the pixel phase errors, representing the position residuals of the stars relative to their mean positions as a function of the X/Y pixel phase. The right-hand panels show the ePSF sampling at various distances from the ePSF X centre within a slice of $-0.25<\delta Y<0.25$. In iterations 1 and 10 , a single ePSF model was employed for the entire detector; in iteration 30 , a grid of $5 \times 5$ ePSFs was generated to account for the PSF variations across the detector. The green and red points represent the ePSF sampling for the lower-left and upper-right detector regions, respectively, demonstrating how the PSF peak changes across the detector. The figure showcases the case of the most undersampled filter, F070W, and focuses on modelling the ePSFs of detector A1.
we obtained the catalogues from both ground-based data-sets and selections of the Gaia DR3.

### 2.1 Large Magellanic Cloud JWST data set

We employed the NIRCam@JWST data of the LMC collected during the Calibration Programme CAL-1476 (PI: Boyer) to derive the ePSFs in 10 different filters. Specifically, we used images collected with the Short Wavelength (SW) channel in F070W, F090W, F115W, F150W, and F200W filters, and with the Long Wavelength (LW) channel in F250M, F277W, F356W, F444W, and F460M filters. As detailed in Paper II, nine pointings are available for each filter. Observations in F277W and F356W filters were conducted using the BRIGHT1 readout pattern and an effective exposure time $t_{\text {exp }}=$ 96.631 s (corresponding to 5 groups of 1 averaged frame). For the F460M filter, the BRIGHT2 readout pattern and $t_{\text {exp }}=85.894 \mathrm{~s}(4$ groups of 2 averaged frames) were employed. Images in all the other filters were taken using the RAPID readout patter, with two groups containing one frame ( $t_{\text {exp }}=21.474 \mathrm{~s}$ ). The top panel of Fig. 1 displays the Total System Throughput for each filter.

For our analysis, we utilized the _cal images created by the Stage 2 pipeline calwebb_image2. ${ }^{1}$; we converted the value of each pixel from MJy sr ${ }^{-1}$ into counts by using the header keywords PHOTMJSR and XPOSURE. Additionally, we flagged bad and saturated pixels by using the Data Quality image included in the _cal data cube.

### 2.1.1 Effective PSFs

For each filter and detector, we derived a $5 \times 5$ grid of $4 \times$ oversampled library ePSFs by following the procedure developed by Anderson \& King (2000, AK00) for undersampled PSFs, and employed in many other works (see e.g, Anderson \& King 2004, 2006; Anderson et al. 2015; Anderson 2016; Libralato et al. 2016a,b; Nardiello et al. 2016b; Libralato et al. 2023; Nardiello et al. 2023). Here, we provide a brief description of the ePSF modelling; we refer the reader to Paper I or AK00, for a detailed description of the method.

To obtain a well-sampled PSF model, we need to break the degeneracy between positions and fluxes of the sources which occurs when dealing with images whose PSFs are undersampled. The degeneracy can be broken by constraining the positions and fluxes of a set of stars using an iterative procedure. Initially, we extracted the first-guess positions and fluxes of bright, unsaturated, and isolated stars in each image using the ePSF grids obtained in Paper I. ${ }^{2}$ By employing the geometric distortion (GD) solution derived in Paper II, we determined the six-parameter transformations between the images by cross-matching the stars in common to different images. These transformations were employed to create a catalogue containing the mean positions and fluxes (transformed to a common reference system) of stars that were measured at least three times. This catalogue served as a master catalogue for ePSF modelling: indeed, stars in this catalogue will be adopted to break the degeneracy

[^1][^2]

Figure 3. The left-hand panel shows a three-colour image of a $30 \times 30 \operatorname{arcmin}^{2}$ region centred on NGC 2506, created by stacking $g-, r-, i-$ sloan band images from the PS1 survey. The field of view of the observations obtained with NIRCam Module A and B is indicated by green and red squares, respectively. Additionally, the cyan rectangle represents the field of view of the WFC@INT detector 4 observations employed in this study (see Section 2.4). The right-hand panel shows the three-colour image ( $\mathrm{F} 277 \mathrm{~W}+\mathrm{F} 356 \mathrm{~W}+\mathrm{F} 444 \mathrm{~W}$ ) generated by stacking the images obtained from the JWST observations employed in this work.
position-flux typical of undersampled images and derive the ePSF model.

The following four steps were followed to derive the ePSF model: (1) using the inverse GD solution from Paper II, we transformed the positions of the stars from the master catalogue to the reference system of each individual image; (2) we converted each pixel value within a radius of 25 pixels from each star's centre into an estimate of the ePSF model, projecting the individual point samplings from the original image scale to a grid super-sampled by a factor $4(201 \times 201$ points); (3) in iteration 1 , we calculated the ePSF model as the $3 \sigma$ clipped average of the point sampling within a square by $0.25 \times 0.25$ pixels ${ }^{2}$ in ePSFs $(x, y)$ coordinates. Starting from iteration 2 , we first subtracted from each sampling the corresponding value of the last ePSF model, and then we calculated the $3 \sigma$-clipped average of the residuals in each $0.25 \times 0.25$ pixels $^{2}$ grid point. Mean residuals are then added to the last available ePSF model, and the result was smoothed with a combination of linear, quadratic, and quartic kernels; (4) using the last available ePSF model, we re-measured the positions and fluxes of the sources in the master list in each image, and we performed the transformations described above to obtain an updated master list to use in step (1).

We repeated steps (1)-(4) 10 times assuming a single ePSF model for the entire detector; from iteration 11, we took into account the spatial variation of the ePSFs by dividing the image in sub-regions and calculating the ePSF models using the sources in each region. We gradually increased the number of subregions from $2 \times 2$ (size of each subregion: $1024 \times 1024$ pixel $^{2}$ ) to $5 \times 5$ (size of each subregion: $409 \times 409$ pixel $^{2}$ ).

Fig. 2 illustrates the improvement of the ePSF models for the detector A1 and filter F070W (the most undersampled one) from
the initial iteration to the final iteration (30). The enhancement is particularly evident in the distributions of the pixel phase errors, where the distributions flatten out as the PSF model improves (panels in the left and middle columns). Right column panels show the improvement of the ePSF samplings from iteration 1 to 10 when utilizing a single PSF model for the entire detector, and in the final iteration where 25 different ePSFs are modelled. The ePSF samplings in the lower-left and upper-right regions, represented by green and red points, respectively, demonstrate the significant variation of the PSF peak across the detector (see Appendix A).

Middle and bottom rows of Fig. 1 show the ePSFs in each filter, demonstrating how the ePSF model changes from a filter to another.

We make publicly available these ePSFs, which are improved with respect to our early derivation in Paper I, as at that time an appropriate GD correction was not publicly available. More details are reported in Appendix B.

### 2.2 NGC 2506 JWST observations

Our target open cluster NGC 2506 was observed by JWST with NIRCam on 2022 November 1 over the course of 2 hours, as part of the Calibration Program CAL-1538 (PI: Gordon). The purpose of this programme was to obtain observations of G dwarf stars for the absolute flux calibration of $J W S T$. The observations consisted of a $2 \times 2$ mosaic centred in $(\alpha, \delta)=(120.03775$, -10.78695 ), in which each dither is observed two times with RAPID readout mode (two integrations comprising two groups of one frame, $t_{\text {exp }}=42.947 \mathrm{~s}$ ). Data were collected in the same 10


Figure 4. Overview of the procedure to identify and reject bad measurements in the catalogues produced by the K. 2 routine. Panels ( $\mathrm{a}_{1}$ ), ( $\mathrm{a}_{2}$ ), and ( $\mathrm{a}_{3}$ ) show the distributions of photometric RMS $(\sigma)$, QFIT, and RADXS for the filter F150W, respectively: red lines represent the threshold for good measurements in each parameter distribution, while the azure points are the rejected sources. Panels ( $b_{1}$ ), ( $b_{2}$ ), and ( $b_{3}$ ) show the F150W versus (F070W-F150W) instrumental CMDs of all measured sources, the sources rejected in at least one filter, and the sources that passed the selection criteria in both filters, respectively. Saturated stars are plotted in red. The figure shows the sources in the catalogues obtained from Module A images.
filters ( 8 wide +2 medium) employed in Section 2.1 and shown in Fig. 1.

Fig. 3 illustrates the field of view covered by the NIRCam observations: in the left-hand panel, a three-colour image obtained with PanSTARRS DR1 (PS1) images (Chambers et al. 2016; Magnier et al. 2020; Waters et al. 2020) is shown; green and red squares represent the Modules A and B field of views, respectively, which are also displayed in the right-hand panel. Due to the limited overlap between the two modules and the scarcity of bright stars required for accurate six-parameter transformations, the data associated with the two modules were reduced separately. The final catalogues were combined at the end of the data reduction process.

### 2.2.1 Catalogues

Observations of NGC 2506 were obtained approximately 4 months after the data used to derive the library ePSFs. To account for the time variation of the PSFs, we employed the brightest and most isolated stars in each image to perturb the corresponding library PSFs (for a detailed description of the procedure, refer to Anderson \& King 2006; Anderson et al. 2008; Nardiello et al. 2018b). To perturb the PSFs, we first measured the positions and fluxes of the stars selected for the perturbation with the library ePSF; we modelled and subtracted
these stars from the image and calculated the average of the residuals at different distances from the PSF centre (oversampled by a factor of 4). The mean residuals were utilized to adjust the PSF model. We iterated this procedure five times, using the last perturbed PSF each time.

We used the perturbed ePSFs to extract positions and fluxes of the stars in each image using the NIRCam version of the img2xym software, developed by Anderson et al. (2006) for the Wide Field Imager (WFI) @ESO/MPG 2.2 m telescope. We will refer to this photometry as first-pass photometry. For each filter, we transformed positions and magnitudes to a common reference frame using sixparameter linear transformations and mean photometric zero points. Subsequently, we used the perturbed ePSFs, the images, and the transformations to perform the second-pass photometry with the KS2 software, ${ }^{3}$ developed by J. Anderson (which is a second generation of the software kitchen_sync presented in Anderson et al. 2008).

The KS2 software enables the measurement of positions and fluxes of bright and faint stars with high accuracy through the simultaneous analysis of all the images (see e.g. Sabbi et al. 2016; Bellini et al.

[^3]

Figure 5. Observed and artificial $m_{\mathrm{F} 277 \mathrm{~W}}$ versus $m_{\mathrm{F} 115 \mathrm{~W}}-m_{\mathrm{F} 277 \mathrm{~W}} \mathrm{CMDs}$ for Module A (in green) and B (in red). Panel (a) shows the CMD obtained with real observations; panels (b) and (c) display the input and output AST CMDs.

2017; Nardiello et al. 2018b; Scalco et al. 2021), employing ad-hoc masks for bright and saturated stars (recovered during the first-pass photometry using the frame-0 of each image), and four different iterations in which progressively fainter stars are measured and subtracted from the images. During the first two iterations, we searched for sources in the F277W filter; in the third iteration, we utilized the F356W filter; and in the fourth iteration, we employed the F070W filter to identify faint blue sources that may not be detectable in the red filters.

Since only 45 percent of the field of view of each module is covered by $\geq 3$ images per filter, while the remaining $\sim 55$ per cent is covered by two images (or even just one!) and since our goal is to identify as many weak sources as possible, the final catalogue generated by the KS2 software contains numerous sources that may be identified as noise peaks in individual images. Therefore, it is necessary to perform a 'cleaning' of the catalogue. We adopted the same selection criteria as described in Nardiello et al. (2018b, 2019), which are based on the following parameters: (i) the photometric error (RMS); (ii) the quality-of-fit (QFIT), which assesses the PSF fitting of the source; (iii) the RADXS parameter defined as in Bedin et al. (2008), which enables the distinction between stellar sources, galactic-shaped sources, and cosmic-rays/noise peaks. A detailed description of these parameters is reported in Nardiello et al. (2018b), while an example of the selection process for the F150W filter is illustrated in panels (a) of Fig. 4. Additionally, sources measured only once and heavily contaminated by bright neighbouring stars were excluded from the selections. The lower panels of Fig. 4 display the instrumental F150W versus F070W-F150W colour-magnitude diagrams (CMDs) for all the detected sources [panel ( $\mathrm{b}_{1}$ )], the sources rejected by the selections [panel $\left(b_{2}\right)$ ], and the sources that passed the selections [panel $\left.\left(\mathrm{b}_{3}\right)\right]$. Saturated stars (recovered from the firstpass photometry), which were not subjected to any selection, are highlighted in red.

### 2.2.2 Photometric calibration

We calibrated the catalogues in each filter and module in the VEGAmag system by using the most updated ${ }^{4}$ JWST photometric zero-points reported in the JWST User documentation. ${ }^{5}$ To calibrate the instrumental magnitudes, we first performed aperture photometry (with a radius $r_{\mathrm{ap}}=0.20 \mathrm{arcsec}$ ) of the most isolated bright stars from each _cal image. We transformed the finite-aperture fluxes FLX ( $\left.r_{\text {ap }}=0.20 \operatorname{arcsec}\right)\left[\mathrm{MJy} \mathrm{sr}^{-1}\right]$ into infinite-aperture fluxes using the Encircled Energy distributions reported in the JWST User documentation ${ }^{6}$ as follows:
$\operatorname{FLX}\left(r_{\mathrm{ap}}=\infty\right)[\mathrm{MJy} / \mathrm{sr}]=\operatorname{FLX}\left(r_{\mathrm{ap}}=0.20^{\prime \prime}\right)[\mathrm{MJy} / \mathrm{sr}] / \mathrm{EE}\left(0.20^{\prime \prime}\right)$

We calculated the aperture photometry calibrated magnitudes by using the equation:
$m_{\text {ap,cal }}=-2.5 \times \log \operatorname{FLX}[\mathrm{DN} / \mathrm{s}]+\mathrm{ZP}_{\mathrm{VEGA}}$
where the flux FLX[DN/s] is computed as
$\operatorname{FLX}[\mathrm{DN} / \mathrm{s}]=\operatorname{FLX}\left(r_{\mathrm{ap}}=\infty\right)[\mathrm{MJy} / \mathrm{sr}] /$ P HOTMJSR
and $\mathrm{ZP}_{\mathrm{VEGA}}$ and PHOTMJSR are the photometric zero-points and the conversion factor $\mathrm{MJy} \mathrm{sr}^{-1}$ to $\mathrm{DN} / \mathrm{s}$, respectively, tabulated in the JWST User documentation. ${ }^{7}$

For each filter and module, we cross-matched the aperture photometry calibrated catalogues with the catalogue obtained in the

[^4]

Figure 6. The $G$ versus $G_{\mathrm{BP}}-G_{\mathrm{RP}}$ CMD obtained with the Gaia DR3 catalogue of the stars within 1.5 deg. from the cluster centre. Black and grey stars are the sources identified as bona-fide cluster members and Galactic stars, respectively, based on the MP (threshold 90 per cent); for comparison, a BaSTI-IAC 2 Gyr isochrone is plotted in red by adopting the parameters reported in the panel.

Table 1. Cluster parameters of NGC 2506.

| Parameter | Value | Reference |
| :--- | :---: | :---: |
| $\alpha$ (ICRS, J2015.5) [deg.] | 120.010 | $(1)$ |
| $\delta(\mathrm{ICRS}, \mathrm{J} 2015.5)$ [deg.] | -10.773 | $(1)$ |
| $l(\mathrm{~J} 2015.5)$ [deg.] | 230.56942 | $(1)$ |
| $b(\mathrm{~J} 2015.5)$ [deg.] | +09.93816 | $(1)$ |
| $d$ [pc] | $3100 \pm 175$ | this work |
| $(m-M)_{0}$ | $12.46 \pm 0.12$ | this work |
| $E(B-V)$ | $0.08 \pm 0.01$ | this work |
| $[\mathrm{Fe} / \mathrm{H}]$ [dex] | $-0.36 \pm 0.10$ | $(2)$ |
| $[\alpha / \mathrm{Fe}]$ [dex] | $0.10 \pm 0.10$ | $(2)$ |
| $[\mathrm{M} / \mathrm{H}]$ [dex] | $-0.29 \pm 0.10$ | $(2)$ |
| $\mathrm{t}_{\text {age }}$ [Gyr] | $2.01 \pm 0.10$ | $(2)$ |
| $r_{\mathrm{c}}$ [arcmin] | $2.60 \pm 0.05$ | this work |
| $r_{\mathrm{c}}[\mathrm{pc}]$ | $2.34 \pm 0.05$ | this work |
| $r_{\mathrm{t}}$ [arcmin] | $33.0 \pm 4.3$ | this work |
| $r_{\mathrm{t}}$ [pc] | $29.8 \pm 3.9$ | this work |

(1) Tarricq et al. (2021); (2) Knudstrup et al. (2020)


Figure 7. The $I$ versus $V-I$ CMD obtained with the WFC@INT data. A BaSTI-IAC 2 Gyr isochrone is plotted in red.
previous section, and, for the $N_{\text {stars }}$ stars in common, we calculated the difference
$\delta m^{i}=m_{\mathrm{ap}, \mathrm{cal}}^{i}-m_{\mathrm{inst}, \mathrm{KS} 2}^{i} \quad$ with $i=1, \ldots, N_{\mathrm{stars}}$
where $m_{\text {inst, KS2 }}$ is the magnitude output of the KS2 routine. We then computed the average value of $\delta m$, which represents the photometric zero-point to be added to the instrumental magnitudes.

Due to the errors in the photometric zero-points, which are $\sim 0.02$ mag, we observed slight discrepancies between the CMDs obtained from the stars measured in Module A and Module B images. To align the two modules to a common reference system, we employed the following approach: we used a small sample of stars that were detected in both modules (consisting of 10-25 stars) to determine the mean difference between the magnitudes obtained from the images of Module A and Module B ( $\delta m(\mathrm{~A}-\mathrm{B})$ ). Subsequently, we applied a correction by subtracting (or adding) $\delta m(\mathrm{~A}-\mathrm{B}) / 2$ to the magnitudes of the stars in Module A (or Module B). An example of the achieved results can be seen in panel (a) of Fig. 5.

### 2.2.3 Artificial stars

We employed artificial stars to assess the completeness of our catalogue across different filters (Section 3.2 and Nardiello et al. 2018a for detailed information). For each module, we generated 50000 artificial stars (ASTs) within the F277W magnitude range from 14.5 (near the saturation limit) to 26.5 . We created 40000 ASTs with a flat luminosity function (LFs) in F277W and with colours that lie along the cluster sequence in the different $m_{\mathrm{F} 277 \mathrm{w}}$ versus $m_{\mathrm{X}}-m_{\mathrm{F} 277 \mathrm{~W}} \mathrm{CMDs}$, where X is one of the 10 available


Figure 8. Cluster membership analysis using the WFC@INT and NIRCam@JWST data. Panel (a) shows the distribution of proper motions relative to the cluster's mean motion, as a function of the $m_{\mathrm{F} 070 \mathrm{~W}}-m_{\mathrm{F} 444 \mathrm{~W}}$ colour; panel (b) presents the relative proper motions of the stars common to both data sets. Panel (c) is the $m_{\text {F070W }}$ versus $m_{\text {F070W }}-m_{\text {F444W }}$ CMD of the stars in the fields of the two modules: grey squares are the stars not measured in the WFC@INT data set. Panel (d) showcases the MP distribution; the magenta line denotes the MP threshold used in this work. In all panels, cluster members are represented by black points, while field stars are denoted by azure points.
filters. Additionally, we generated other 10000 ASTs with a flat LF in F277W and with random colours in the different filters, to simulate the field stars. The spatial distribution of the ASTs was uniform across the field of view. The CMD of the input catalogue of ASTs is shown in panel (b) of Fig. 5. We used the KS2 software to add one AST at a time to each image with the appropriate position and flux, adopting the same procedure used for real stars to search and measure the added AST. The software provided output parameters for the ASTs identical to those of real stars. Panel (c) of Fig. 5 showcases the CMD of the ASTs output of KS2 routine.

### 2.3 NGC 2506 from the Gaia archive

We adopted the Gaia DR3 catalogue (Gaia Collaboration 2021, 2023) to obtain information about stars located within a radius of 1.5 degrees from the cluster centre $\left(\alpha_{c}, \delta_{c}\right)=(120.010,-10.773)$ (Tarricq et al. 2021). We calculated the membership probabilities (MPs) using the method outlined in Griggio \& Bedin (2022), which considers the spatial distribution, proper motion, and parallax of the sources. The bona-fide cluster members, with a MP $>90$ per cent,
are denoted in black in Fig. 6. We performed a cross-match between the bona-fide cluster members and the catalogue by Bailer-Jones et al. (2021) and determined the mean distance of the cluster to be $d=3100 \pm 175 \mathrm{pc}$, consistent with the value reported by Knudstrup et al. (2020). Using the Infrared Dust Maps ${ }^{8}$ (Schlegel, Finkbeiner \& Davis 1998; Schlafly \& Finkbeiner 2011), we found a mean reddening $E(B-V)=0.08$ for the cluster. Knudstrup et al. (2020) determined the age, metallicity, and $\alpha$-enhancement of NGC 2506 through the analysis of detached eclipsing binaries, yielding $t_{\text {age }} \sim 2 \mathrm{Gyr},[\mathrm{Fe} / \mathrm{H}] \sim-0.36$, and $[\alpha / \mathrm{Fe}] \sim 0.10$, respectively. Adopting these cluster parameters (reported in Table 1), we plotted a 2 Gyr BaSTI-IAC isochrone (Hidalgo et al. 2018; Pietrinferni et al. 2021, in red) in the $G$ versus $G_{\mathrm{BP}}-G_{\mathrm{RP}}$ CMD. This $\alpha-$ enhanced IAC-BaSTI isochrone has been derived as follows. We have first downloaded from the BaSTI-IAC website solar-scaled and $\alpha$-enhanced $([\alpha / \mathrm{Fe}]=0.4)$ isochrones (including overshooting and atomic diffusion) for $[\mathrm{Fe} / \mathrm{H}]=-0.36$, and then interpolated linearly in $[\alpha / \mathrm{Fe}]$ (between 0 and 0.4 ) to obtain isochrones with $[\mathrm{Fe} / \mathrm{H}]=-0.36$ and $[\alpha / \mathrm{Fe}]=0.1$ (see Table 1 ) - corresponding to a total metallicity $[\mathrm{M} / \mathrm{H}]=-0.29$.

### 2.4 Ground-based observations of NGC 2506

We have also taken advantage of data obtained with the Wide Field Camera (WFC) mounted at the prime focus of the 2.5 m Isaac Newton Telescope (INT) for Programme I9/2003B (PI: Rosenberg). The observations were conducted between 2004 January 21 and 22. The data set includes the following exposures: $3 \times 300 \mathrm{~s}+2 \times 600 \mathrm{~s}$ $V$-Harris images and $1 \times 30 \mathrm{~s}+2 \times 900 \mathrm{~s} i$-Sloan images. All observations were taken at an airmass between 1.32 and 1.48 and the typical seeing was around $1-1.2$ arcsec. For this work, only images associated with CCD\#4, which contains the JWST observations, were used (as shown in Fig. 3).

We reduced the data set by using empirical PSFs and the software developed by Anderson et al. (2006) adapted for WFC@INT images. We corrected the GD by following the procedure adopted by Griggio et al. (2022). We calibrated the $V$, $i$ magnitudes into $V$-Johnson and $I$-Cousins, respectively, by using the homogeneous photometry published by P..B. Stetson ${ }^{9}$ (Stetson 2000).

The resulting $I$ versus $V-I$ CMD from WFC@ INT data is shown in Fig. 7, together with a 2 Gyr BaSTI-IAC isochrone adopting the same chemical composition, reddening, and distance as in the comparison with the Gaia data. The isochrone matches the pattern of the CMD distribution of the observed stars reasonably well for $I$ $\lesssim 19.5$.

## 3 ASTROMETRIC AND PHOTOMETRIC ANALYSES

### 3.1 Proper motions and membership probabilities

To extend the membership study to magnitudes beyond the reach of Gaia (i.e. for stars fainter than $G \simeq 19$ ), we used proper motions derived from JWST and INT positions. We discriminated between cluster members and field stars, following the methodology employed in previous studies by our research group (see e.g. Bedin et al. 2003; Anderson et al. 2006; Bellini et al. 2010; Libralato

[^5]

Figure 9. Analysis of the completeness of our catalogues: the left-hand panels show the completeness as a function of the $m_{\text {F277w }}$ magnitude for Module A (upper panel) and B (bottom panel). Magenta, orange, and dark grey points represent the completeness distribution in the case the stars appear in less than 3, between 2 and 4, and between 4 and 8 images, respectively. The right-hand panel shows the completeness as a function of the position: we calculated the $m_{\mathrm{F} 277 \mathrm{~W}}$ limit magnitude for which the completeness reaches 50 per cent in squares of $15.5 \times 15.5 \mathrm{arcsec}^{2}$, coloured following the colour-bar on the right.
et al. 2014; Nardiello et al. 2015, 2016a). To achieve this, we calculated the displacements of stars between two different epochs after transforming their positions to a common reference system using sixparameter global transformations. The first epoch was represented by the WFC@INT data, with a mean epoch of $t_{\mathrm{I}}=2004.06$, while for the second epoch, we took advantage of the NIRCam catalogues, with $t_{\mathrm{II}}=2022.84$. We determined the relative displacements of the stars, referring them to the average motion of the cluster, over a time span $\Delta t_{\mathrm{II}-\mathrm{I}}=18.78 \mathrm{yr}$.

We computed the MP for each of these faint stars in the catalogues, following an approach similar to that described by Griggio \& Bedin (2022). Only proper motions were considered in the calculation of the MPs, without incorporating spatial and parallax terms. Specifically, the spatial term was neglected due to the limited field of view of JWST observations, which allowed us to assume a uniform distribution of the cluster's stars within the observed area, while parallaxes are not available for these faint stars.

Fig. 8 illustrates the selection of cluster members based on MPs. In the range $16.0<m_{\text {F070w }} \leq 20.5$, stars with MP> 90 per cent were chosen as cluster members. For saturated stars and faint stars with $m_{\text {F070w }}>20.5$, we relaxed the selection criteria and identified cluster members with MP $>50$ per cent and MP $>75$ per cent, respectively, as indicated in panel (d) (magenta line). Relative proper motions are shown in panels (a) (as a function of the colour $m_{\text {F070w }}-m_{\text {F444W }}$ ) and (b), while panel (c) shows the $m_{\text {F070w }}$ versus $m_{\text {F070w }}-m_{\text {F444W }}$ CMD for cluster members (black) and field objects, mainly Galactic field stars (azure).

### 3.2 Completeness

By using the ASTs obtained as described in Section 2.2.3, we determined the completeness in different regions of the field of view and for different magnitudes. The completeness is calculated as the ratio between the number of recovered stars and the number
of injected stars, $N_{\mathrm{rec}} / N_{\mathrm{inj}}$. We considered an AST as recovered if the differences in position satisfy $\left|x_{\text {in }}-x_{\text {out }}\right|<1 \mathrm{px}$ and $\left|y_{\text {in }}-y_{\text {out }}\right|<$ 1 px ; additionally, we applied the following magnitude conditions: $\left|m_{\mathrm{F} 277 \mathrm{~W}, \text { in }}-m_{\mathrm{F} 277 \mathrm{~W}, \text { out }}\right|<0.5$ for stars measured in iteration 1 or 2 , $\left|m_{\mathrm{F} 356 \mathrm{~W}, \text { in }}-m_{\mathrm{F} 356 \mathrm{~W}, \text { out }}\right|<0.5$ for ASTs measured in iteration 3, and $\left|m_{\text {F070W, in }}-m_{\text {F070W, out }}\right|<0.5$ for sources measured in iteration 4. These conditions reflect the procedure used to identify real stars. To account for the rejections described in Section 2.2.1, we applied to the ASTs the same selections used for real stars, and included them in the computation of $N_{\text {rec }}$.

Fig. 9 shows the completeness as a function of the magnitude and position. The left-hand panels demonstrate how completeness varies with magnitude for different image coverages: when stars are observed just once or two times, completeness is lower than 60 per cent, and drops below 50 per cent at $m_{\text {F277W }} \sim 21$ (dark grey points). For stars measured in at least three images the completeness is 20-30 per cent higher, and it is lower than 50 percent at $m_{\text {F277w }}$ $\sim 22.5$ (magenta and orange points). The right-hand panel shows the dependence of completeness on position due to varying image coverage: the blue/azure squares of each module are the regions covered by $\geq 4$ images, and 50 per cent completeness is reached at magnitude $m_{\mathrm{F} 277 \mathrm{~W}} \sim 21.5-22.5$; green/red regions are areas covered by $\leq 2$ images, where completeness reaches 50 per cent at $m_{\text {F277W }} \sim$ 20.0-21.0.

### 3.3 Colour-magnitude diagrams

Fig. 10 shows a rundown of the CMDs with the 10 available filters: grey and black points are the stars that passed the quality and membership selections, respectively. Naturally, these CMDs have different levels of completeness along the MS. As already done in Sections 2.3 and 2.4, we superimposed 2 Gyr BaSTI-IAC isochrones (in red) to the JWST CMDs. The lower mass limit of the isochrones is $0.1 \mathrm{M}_{\odot}$. Some filters combinations, as, for example, $m_{\text {F150w }}$ versus ( $\left.m_{\mathrm{F} 115 \mathrm{~W}}-m_{\mathrm{F} 150 \mathrm{~W}}\right)$ or $m_{\mathrm{F} 150 \mathrm{~W}}$ versus $\left(m_{\mathrm{F} 150 \mathrm{~W}}-m_{\mathrm{F} 356 \mathrm{~W}}\right)$, allow us


Figure 10. Some of the possible CMDs obtained with the available $J W S T$ photometry in different filters: panels in top row show the $m_{\mathrm{F} 070 \mathrm{w}}$ versus ( $m_{\mathrm{F} 070 \mathrm{w}}-$ $m_{\mathrm{X}}$ ) CMDs with X = F090W, F115W, F200W, F250M, F356W, F444W, F460M; panels in the middle row are the $m_{\mathrm{F} 150 \mathrm{~W}}$ versus ( $m_{\mathrm{X}}-m_{\mathrm{F} 150 \mathrm{~W}}$ ) CMDs with $\mathrm{X}=\mathrm{F} 070 \mathrm{~W}, \mathrm{~F} 090 \mathrm{~W}, \mathrm{~F} 115 \mathrm{~W}$, and the $m_{\mathrm{F} 150 \mathrm{~W}}$ versus $\left(m_{\mathrm{F} 150 \mathrm{~W}}-m_{\mathrm{Y}}\right) \mathrm{CMDs}$ with $\mathrm{Y}=\mathrm{F} 250 \mathrm{M}, \mathrm{F} 356 \mathrm{~W}, \mathrm{~F} 444 \mathrm{~W}, \mathrm{~F} 460 \mathrm{M}$; in the bottom row are shown the the $m_{\mathrm{F} 277 \mathrm{~W}}$ versus $\left(m_{\mathrm{X}}-m_{\mathrm{F} 277 \mathrm{~W}}\right)$ CMDs with $\mathrm{X}=\mathrm{F} 070 \mathrm{~W}, \mathrm{~F} 090 \mathrm{~W}, \mathrm{~F} 115 \mathrm{~W}, \mathrm{~F} 150 \mathrm{~W}$, and the $m_{\mathrm{F} 277 \mathrm{~W}}$ versus $\left(m_{\mathrm{F} 277 \mathrm{~W}}-m_{\mathrm{Y}}\right) \mathrm{CMDs}$ with Y $=\mathrm{F} 356 \mathrm{~W}$, F444W, and F 460 M . Also, 2 Gyr BaSTI-IAC isochrones are plotted in red.
to reach a magnitude limit $m_{\text {F150w }} \sim 22$ with SNR $\sim 10$; according to the models, this magnitude limit corresponds to masses below 0.1 $\mathrm{M}_{\odot}$ on the MS.

We investigated the lower MS of NGC 2506 to check the presence of broadening due to chemical variations. The analysis is shown in Fig. 11: we compared the $m_{\text {F150w }}$ versus ( $\left.m_{\text {F115W }}-m_{\text {F150W }}\right)$ CMD of NGC 2506 against the $H S T m_{\text {F160w }}$ versus $\left(m_{\text {F110w }}-m_{\text {F160w }}\right)$ CMD of the old, metal-poor, massive globular cluster NGC 6752 (leftmost panel, Scalco et al. in preparation). As reported by Milone et al. (2019), the multiple lower MSs in NGC 6752 are due to
the variations of Oxygen between the stars belonging to different stellar populations. We shifted the CMD of NGC 6752 in colour and magnitude in such a way that the 'knee' of the MS overlaps the one of the NGC 2506's CMD: the middle panel of Fig. 11 demonstrates that the lower MS of NGC 2506 agrees with a single sequence of NGC6752 and that no chemical variation is expected among the low-mass stars of this cluster. As a further test, we simulated the CMD of a single population by selecting randomly 600 ASTs (about the number of observed stars in the MS) from the sample of ASTs; we also simulated 57.5 per cent MS-MS binaries (with


Figure 11. Comparison between lower MS of NGC 6752 (three stellar populations) and NGC 2506 (single population) is similar IR filters. The left-hand panel shows the $\left.H S T m_{\mathrm{F} 160 \mathrm{~W}}\right)$ versus $\left(m_{\mathrm{F} 110 \mathrm{~W}}-m_{\mathrm{F} 160 \mathrm{~W}}\right)$ CMD of NGC 6752, for which three different low-MSs are well detectable. The middle panel is a comparison between the CMD of NGC 6752 (grey points) and the $m_{\mathrm{F} 150 \mathrm{~W}}$ ) versus ( $m_{\mathrm{F} 115 \mathrm{~W}}-m_{\mathrm{F} 150 \mathrm{~W}}$ ) CMD of NGC 2506 (black points), which demonstrates that the lower-MS of the open cluster agrees with the presence of a single population. This is also demonstrated by the simulated CMD shown in the right-hand panel.
a flat mass-ratio distribution, see Section 5). The simulated CMD is reported in right-hand panel of Fig. 11: it demonstrates that the observed CMD agrees with the simulated CMD of a single stellar population.

## 4 RADIAL DENSITY PROFILE

We computed the radial stellar density profile of NGC 2506 by using the Gaia DR3 catalogue. The results are presented in Fig. 12. To obtain the density profile, we divided the area within a radius of 70 arcmin into a series of annuli with a 1 arcmin width. For each annulus, we computed the number of stars per $\operatorname{arcmin}^{2}\left(\Sigma^{\star}\right)$ and the mean radial distance of the stars from the centre $(R)$. We restricted our analysis to stars with magnitudes between $G=14$ and $G=18$, which - in the average Galactic field - should have a completeness close to 100 per cent (Boubert \& Everall 2020; Everall \& Boubert 2022).

To fit the density profile distributions shown in Fig. 12, we employed a King profile (King 1962), described by the function:

$$
\begin{equation*}
\Sigma^{\star}[R]=k_{\mathrm{b}}+k_{0}\left(\frac{1}{\sqrt{1+R^{2} / r_{\mathrm{c}}^{2}}}-\frac{1}{\sqrt{1+r_{\mathrm{t}}^{2} / r_{\mathrm{c}}^{2}}}\right)^{2} \tag{5}
\end{equation*}
$$

where $k_{\mathrm{b}}$ and $k_{0}$ represent the background and central stellar densities, respectively, $r_{\mathrm{c}}$ is the core radius, and $r_{\mathrm{t}}$ denotes to the cluster tidal radius.

We analysed the density profile of NGC 2506 in three different cases, shown in the three panels in Fig. 12. In case (a), we fitted a density profile that model the contribution of both the cluster stars and the Galactic field stars. In case (b), we subtracted the mean density of background stars from the calculated stellar density in each annulus.

The background density was determined in an annulus ranging from $R=70$ to $R=90$ arcmin from the cluster centre. In case (c), we fitted a density profile in which the contribution of each star is weighted by the MP. Excluding the background density $k_{\mathrm{b}}$, which is higher in case (a) due to the inclusion of Galactic field stars in the fit, the other parameters, such as $k_{0}, r_{\mathrm{c}}$, and $r_{\mathrm{t}}$, show consistent values, and they agree within $3 \sigma$. The weighted mean values we obtained are as
 and $r_{\mathrm{t}}=33.0 \pm 4.3$ arcmin.

The core radius we measured is smaller than the value reported by Rangwal et al. (2019) based on WFI and Gaia DR2 data, although they agree within $3.2 \sigma$. However, our core radius agrees with the value found by Lee et al. (2013) for stars with $V<17$ magnitude. The central density and tidal radius obtained in our study are higher than those reported by Rangwal et al. $\left(2019,16.58\right.$ stars $\operatorname{arcmin}^{-2}$ and 12 arcmin, respectively), with a difference $>10 \sigma$. This discrepancy may be attributed to differences in the selection of the cluster members and/or the different density profile models used in the analysis. Additionally, Lee et al. (2013) found a smaller tidal radius ( $\sim 19$ arcmin). These discrepancies can also be explained by the presence of tidal tails extending out to 1 deg. from the cluster centre, as reported by Gao (2020, even if we did not detect any well defined tail as in this work).

## 5 BINARIES AND MASS FUNCTIONS

By combining Gaia DR3 and JWST data, we performed an analysis to determine the fraction of photometric binaries, as well as the luminosity and MFs for MS stars. This analysis considered stars located at different distances from the cluster centre and within various mass intervals.


Figure 12. Radial stellar density profiles of NGC 2506, calculated for stars with magnitudes between $G=14$ and $G=18$ in the Gaia DR3 catalogue. The profiles are obtained by dividing the cluster region into annuli of 1 arcmin width. The three panels display different approaches: panel (a) shows the density profile modelling both cluster and Galactic field stars; in panel (b), the mean density of background stars is subtracted from the density profile of panel (a); panel (c) showcases the density profile with each star's contribution weighted by MP. The observed density profile is represented by black points, and a King profile function is fitted to the three profiles (blue lines). The vertical dashed lines in red and green denote the core and tidal radii, respectively, with shaded regions representing the corresponding $\pm 1 \sigma$ errors. The parameters of the King profile function are listed within each panel.

### 5.1 Main sequence -photometric binaries

At the distance of NGC 2506, essentially all binaries are unresolved. An unresolved binary system composed of two MS stars with magnitudes $m_{1}$ and $m_{2}$, corresponding to fluxes $F_{1}$ and $F_{2}$, can be treated as a point-like source with a total magnitude given by:
$m_{\text {bin }}=m_{1}-2.5 \log \left(1+\frac{F_{2}}{F_{1}}\right)$
The ratio $F_{2} / F_{1}$ is strongly correlated with the mass ratio $q=M_{2} / M_{1}$, where $M_{1}$ represents the mass of the primary (more massive) star and $M_{2} \leq M_{1}$. In the case of $M_{2}=M_{1}$, the magnitude of the binary system is $\sim 0.75$ mag brighter than that of the primary component. Thus, the $q=1$ case serves as a limit for the redder and brighter section of the MS, where MS-MS binaries are located.

To estimate the fraction of binaries, we employed the JWST and Gaia DR3 catalogues following the approach described by Milone et al. $(2012,2016)$ and Cordoni et al. (2023), and shown in Fig. 13. Briefly, we defined a region $\mathrm{R}_{\mathrm{I}}$ encompassing MS stars and binaries with $q<q^{\text {lim }}$, where $q^{\text {lim }}$ denotes the mass ratio below which is difficult to discriminate between single and binary stars in the CMD. In this study, we used $q^{\text {lim }}=0.6$, represented as an orange line in Fig. 13, which was determined by fitting the BaSTI-IAC isochrones discussed in the previous sections. To define the bluer limit of $\mathrm{R}_{\mathrm{I}}$, we calculated the standard deviation of the colour $\left(\sigma_{\mathrm{col}}\right)$ at various magnitudes along the MS. We considered all the stars whose colour is $>\mathrm{col}_{\mathrm{fid}}-2.5 \sigma_{\mathrm{col}}$, where $\operatorname{col}_{\mathrm{fid}}$ represents the colour of the MS fiducial line. In the case of Gaia CMD, we used the $G_{\mathrm{BP}}-G_{\mathrm{RP}}$ colour, while for the $J W S T$ data we adopted the $m_{\text {F070w }}-m_{\text {F277w }}$ wide colour baseline. The region $\mathrm{R}_{\mathrm{I}}$ is confined within the magnitude intervals $16.15 \leq G_{\mathrm{RP}} \leq 18.15$ in the case of Gaia CMD, and $15.50 \leq$ $m_{\mathrm{F} 277 \mathrm{~W}} \leq 18.50$ for the JWST data. ${ }^{10}$ All the stars in the region $\mathrm{R}_{\mathrm{I}}$ are plotted in red in Fig. 13. The region $\mathrm{R}_{\mathrm{II}}$ is defined as the area between the lines determined by binary systems with $q=0.6$ (represented by the orange line) and $q=1$ shifted by $2.5 \sigma_{\text {col }}$. The faint and bright limits of $\mathrm{R}_{\mathrm{II}}$ correspond to the positions of binary systems with mass ratios $0 \leq q \leq 1$. In Fig. 13, stars located within the region $\mathrm{R}_{\mathrm{II}}$ are shown in green.

In the case of Gaia DR3, we assumed a completeness of the catalogue equal to 100 per cent, and we calculated the fraction of binaries with mass ratios $q \geq 0.6$ using the following formula:
$f_{\text {bin }}^{q \geq 0.6}=\frac{\sum_{i} w_{\mathrm{MP}}^{i}}{\sum_{j} w_{\mathrm{MP}}^{j}} \quad$ with $i=1, \ldots, N_{\mathrm{II}} ; \quad j=1, \ldots, N_{\mathrm{I}}$
where $w_{\mathrm{MP}}$ is a weight ranging from 0 to 1 corresponding to MPs from 0 per cent to 100 per cent, and $N_{\text {I }}$ and $N_{\text {II }}$ represent the number of sources within the region $\mathrm{R}_{\mathrm{I}}$ and $\mathrm{R}_{\mathrm{II}}$, respectively.

In the case of JWST data, we took into account the completeness of our catalogue as well as the effects of photometric errors and blending, which can increase the number of sources in region $\mathrm{R}_{\mathrm{II}}$. To address this issue, we made use of ASTs to simulate a CMD as follows: for each real star in our catalogue that passed the quality selections and had MPs $>90$ per cent, we randomly selected a star from the ASTs catalogue located within a radius $r_{\text {AST }}=3$ arcsec from the target star, with a maximum difference in F 277 W magnitude of $\delta m_{\mathrm{F} 277 \mathrm{~W}, \mathrm{AST}}=1 \mathrm{mag}$. The simulated CMD is shown in the right-hand

[^6]

Figure 13. Procedure employed to determine the MS binary fraction from the Gaia DR3 $G_{\mathrm{RP}}$ versus ( $G_{\mathrm{BP}}-G_{\mathrm{RP}}$ ) CMD (left-hand panel), and the $J W S T$ $m_{\mathrm{F} 277 \mathrm{~W}}$ versus ( $m_{\mathrm{F} 070 \mathrm{~W}}-m_{\mathrm{F} 277 \mathrm{~W}}$ ) CMD (middle and right-hand panels). Each CMD is divided in two regions: (i) $\mathrm{R}_{\mathrm{I}}$ contains the majority of MS and low mass-ratio binary stars (red points); (ii) $\mathrm{R}_{\mathrm{II}}$ includes the binaries with mass ratios between $q=0.6$ and $q=1.0$, while also accounting for the uncertainties in colours and magnitudes (green points). The right-hand panel shows the simulated JWST CMD, which was used to assess the impact of photometric errors and blending on the computation of the binary fraction. The primary mass interval covered in the Gaia DR3 data analysis is $0.75 \lesssim M \lesssim 1.10 \mathrm{M}_{\odot}$, while in the case of $J W S T$ data, we studied binaries in the primary mass interval $0.45 \lesssim M \lesssim 1.05 \mathrm{M}_{\odot}$.
panel of Fig. 13. For the JWST data, we estimated the fraction of MS binaries with mass ratios $q \geq 0.6$ using the following equation:

$$
\begin{align*}
f_{\text {bin }}^{q \geq 0.6} & =\frac{\sum_{i} w_{\mathrm{MP}}^{i} / c^{i}}{\sum_{j} w_{\mathrm{MP}}^{j} / c^{j}}-\frac{N_{\mathrm{II}}^{\mathrm{AST}}}{N_{\mathrm{I}}^{\mathrm{AST}}} \quad \text { with } \\
i & =1, \ldots, N_{\mathrm{II}} ; \quad j=1, \ldots, N_{\mathrm{I}} \tag{8}
\end{align*}
$$

where $w_{\text {MP }}$ is the weight defined earlier, $c$ denotes the completeness associated with each star, and $N_{\mathrm{I}}^{\mathrm{AST}}$ and $N_{\mathrm{II}}^{\mathrm{AST}}$ correspond to the number of simulated stars that fall within $R_{I}$ and $R_{I I}$, respectively. For the region covered by the Gaia DR3 catalogue $(0 \lesssim R \lesssim 35$ arcmin), we obtained $f_{\text {bin }}^{q \geq 0.6}=0.228 \pm 0.016$ in the primary mass interval $0.75 \lesssim M \lesssim 1.10 \mathrm{M}_{\odot}$, while for the region covered by $J W S T$ data ( $0.2 \lesssim R \lesssim 4.6 \mathrm{arcmin}$ ), we measured $f_{\text {bin }}^{q \geq 0.6}=0.236 \pm 0.039$ in the primary mass range $0.45 \lesssim M \lesssim 1.05 \mathrm{M}_{\odot}$. Supposing a flat mass-ratio distribution (Milone et al. 2012), the total fraction of MSMS binary stars with $\mathrm{q}>0$ is $\sim 0.575$.

We investigated the binary fraction as a function of the mass of the primary star. To measure the binary fraction in different mass intervals, we followed the procedure described earlier while adjusting the lower and upper magnitude limits of the $R_{I}$ region. The results are shown in the top panel of Fig. 14 and in Table 2: the binary fraction measured in the entire field using Gaia DR3 data is reported in black for four different mass intervals, the binary fraction measured with Gaia in the overlapping region with JWST is shown in magenta, and the binary fraction calculated using JWST data down to $0.45 \mathrm{M}_{\odot}$ is represented in blue. We performed a $\chi^{2}$ test to assess the flatness of the $f_{\mathrm{bin}}^{q \geq 0.6}$ distribution as a function of the mass of the primary star. Considering all the data points and their corresponding
errors from the top panel of Fig. 14, we constructed a histogram with three bins and calculated the $\chi^{2}$ between the observed and expected frequencies, resulting in $\chi^{2}=0.67$. Subsequently, using the $\chi^{2}$-distribution, we determined the P -value, which represents the probability that the distribution is flat. The obtained P -value was $\sim 72$ per cent.

Furthermore, we computed the radial distribution of the binary fraction for both the Gaia and $J W S T$ data sets, as illustrated in the bottom panel of Fig. 14 and in Table 2. For this distribution, we divided the Gaia and JWST samples into radial bins, each containing an equal number of stars. The three measurements obtained with Gaia are denoted by black squares, while the two measurements from JWST are represented by blue circles. These measurements exhibit a radial trend, with a higher concentration of binaries in the central region. We also examined the consistency between the Gaia and JWST measurements in the overlapping region of the two data sets, displayed by the magenta triangle and orange circle. The P-value test yielded a probability of $\sim 41$ per cent that the distribution is flat, suggesting a plausible radial trend in the binary fraction.

### 5.2 Mass functions and total mass

We computed the LFs of MS stars counting stars in magnitude intervals that contain an equal number of stars and using both the Gaia and the JWST catalogue, and then we converted the LFs to luminosity functions (MFs) by adopting the mass-luminosity relation from the BaSTI-IAC isochrones.

As shown in panels (a) and (b) of Fig. 15, thanks to the synergy between Gaia and JWST data, we are able to cover a mass range


Figure 14. Analysis of the binary fraction as a function of the mass of the primary star (top panel) and of the radial distance from the cluster centre (bottom panel). Black squares, magenta triangles, and blue circles refer to the analysis performed with the entire Gaia DR3 catalogue, the Gaia DR3 catalogue limited to the $J W S T$ region, and the $J W S T$ data, respectively. The orange point in the bottom panel is referred to the analysis performed with JWST in only one radial interval.

Table 2. Analysis of photometric binaries in NGC 2506.

|  | $f_{\text {bin }}^{q \geq 0.6}$ versus $M^{\text {prim }}$ |  |  |
| :--- | :---: | :---: | :---: |
| Region | $\boldsymbol{M}^{\text {prim }}$ interval | Mean $\boldsymbol{M}^{\text {prim }}$ | $f_{\text {bin }}^{q \geq 0.6}$ |
|  | $\left(\mathbf{M}_{\odot}\right)$ | $\left(\mathbf{M}_{\odot}\right)$ |  |
| Gaia (All) | $0.76-0.83$ | 0.79 | $0.203 \pm 0.030$ |
|  | $0.83-0.92$ | 0.87 | $0.155 \pm 0.025$ |
|  | $0.92-1.01$ | 0.96 | $0.213 \pm 0.032$ |
|  | $1.01-1.10$ | 1.05 | $0.240 \pm 0.037$ |
| Gaia (JWST region) | $0.78-0.94$ | 0.86 | $0.249 \pm 0.065$ |
|  | $0.94-1.13$ | 1.04 | $0.287 \pm 0.079$ |
|  | $0.44-0.59$ | 0.51 | $0.143 \pm 0.059$ |
| JWST | $0.59-0.81$ | 0.68 | $0.240 \pm 0.070$ |
|  | $0.81-1.06$ | 0.94 | $0.248 \pm 0.059$ |
|  | $f_{\text {bin }}^{q \geq 0.6}$ versus $R$ |  |  |
| Region | $\boldsymbol{R}$ interval | Mean $\boldsymbol{R}$ | $f_{\text {bin }}^{q \geq 0.6}$ |
|  | $($ arcmin $)$ | $($ arcmin $)$ |  |
| Gaia (All) | $0.08-4.00$ | 2.38 | $0.273 \pm 0.035$ |
|  | $4.00-8.58$ | 5.98 | $0.185 \pm 0.025$ |
|  | $8.58-40.48$ | 12.97 | $0.233 \pm 0.028$ |
| Gaia (JWST region) | $0.24-4.61$ | 2.37 | $0.289 \pm 0.053$ |
| JWST (1 bin) | $0.24-4.61$ | 2.51 | $0.237 \pm 0.040$ |
| JWST (2 bin) | $0.24-2.26$ | 1.64 | $0.313 \pm 0.075$ |
|  | $2.26-4.61$ | 3.03 | $0.191 \pm 0.045$ |
|  |  |  |  |

from $\sim 0.1$ to $\sim 1.4 \mathrm{M}_{\odot}$, encompassing the very low mass stars and extending up to the MS turn-off.

Panels (c) and (d) of Fig. 15 show the MFs obtained with the Gaia catalogue. They are also reported in Table 3. To calculate the LFs, we accounted for the contribution of each star in a given magnitude interval weighted by its MP to be a cluster member, as already done in the previous sections. We focused on MS stars with magnitudes between $G_{\mathrm{RP}}=14.50$ and $G_{\mathrm{RP}}=18.25$, corresponding to a mass interval between $M=0.74 \mathrm{M}_{\odot}$ and $M=1.46 \mathrm{M}_{\odot}$. Initially, we considered the present day MF as described by the equation:
$\frac{\mathrm{d} N}{\mathrm{~d} M} \propto M^{\alpha}$
which is a straight line in the logarithmic form:
$\log \left(\frac{\mathrm{d} N}{\mathrm{~d} M}\right)=\beta+\alpha \log (M)$
Panel (c) illustrates the MFs calculated in three radial bins containing an equal number of MS stars. We fitted a straight line to each MF within each radial bin using a weighted least square fit, with the inverse square of the MF errors serving as the weights. We obtained three estimates of the present-day local MF. For the inner region $(R$ $<3.85 \mathrm{arcmin}$ ), we derived a slope $\alpha=-0.99 \pm 0.25$; in the middle region $(3.85 \leq R<8.33 \mathrm{arcmin})$ the slope is $\alpha=-2.22 \pm 0.19$. Finally, for the outermost region $(8.33 \leq R<33.00 \mathrm{arcmin})$ the slope measured is $\alpha=-2.80 \pm 0.24$. We also calculated the slope of the MF using a single interval $(0.00 \leq R<33.00$ arcmin $)$, and found $\alpha=-2.04 \pm 0.14$; i.e. a proxy for the present-day global MF. The change in slope with radial distance from the centre is attributed to the mass segregation effect resulting from the cluster dynamical evolution, as previously noted by Lee et al. (2013) and Rangwal et al. (2019).

To determine the contribution to the cluster mass from stars with $M \geq 0.74 M_{\odot}$, we utilized the MF shown in panel (d) of Fig. 15. Our analysis yielded $M_{\text {cluster }}\left[0.74 \mathrm{M}_{\odot} \leq M \leq 1.46 \mathrm{M}_{\odot}\right]=$ $2077 \pm 67 \mathrm{M}_{\odot}$. We also performed the same computation by using the three MFs shown in panel (c) of Fig. 15: summing the single total mass contributions in each radial bin, we obtained a mass $M_{\text {cluster }}\left[0.74 \mathrm{M}_{\odot} \leq M \leq 1.46 \mathrm{M}_{\odot}\right]=2054 \pm 69 \mathrm{M}_{\odot}$. This result aligns with the previously determined value, confirming that mass segregation does not significantly impact the estimate of the cluster mass obtained by integrating the global MF rather than using local MFs.

We calculated the MFs in the area covered by the JWST data set, spanning approximately $20 \operatorname{arcmin}^{2}$ between 0.24 and 4.61 arcmin from the cluster centre. The results are presented in Table 3 and in panel (e) of Fig. 15. First, we calculated the MF for stars with masses between 0.74 and $1.46 \mathrm{M}_{\odot}$ using Gaia DR3 following the procedure previously described (black points). For the JWST data, we adopted two different approaches to compute the MFs. The first approach involved the use of proper motions and was limited to stars with masses between 0.37 and $0.93 \mathrm{M}_{\odot}$ (as ground-based INT images do not reach magnitudes as faint as the JWST data, see Section 2.4). In this case, we followed a similar procedure as for the Gaia data, weighting the MFs with MPs and correcting for completeness (blue points in panel (e) of Fig. 15). To extend the MF to lower masses, we performed a statistical decontamination of the LFs to account for the contribution of field stars. We selected stars in the Gaia catalogue located in the JWST region with magnitudes 16.5 $\leq G_{\mathrm{RP}} \leq 17.5$, corresponding to a mass range between 0.84 and $1.03 \mathrm{M}_{\odot}$ on the MS. Within this mass interval, which corresponds to the magnitude range $15.67 \leq m_{\mathrm{F} 277 \mathrm{~W}} \leq 16.42$, we calculated the


Figure 15. An overview of the procedure to calculate the MS MFs from Gaia DR3 and $J W S T$ data. Panels (a) and (b) show the $G_{\mathrm{RP}}$ versus ( $G_{\mathrm{BP}}-G_{\mathrm{RP}}$ ) and $m_{\mathrm{F} 277 \mathrm{~W}}$ versus ( $m_{\mathrm{F} 115 \mathrm{~W}}-m_{\mathrm{F} 277 \mathrm{~W}}$ ) CMDs, respectively, with superimposed in red the BaSTI-IAC isochrones marking the mass intervals on the MS. Panels (c) and (d) show the MFs calculated in three radial intervals and over the whole field, respectively, using the Gaia DR3 data set; slopes ( $\alpha$ ) of the fitted straight lines are reported inside the panels. Panels (e) and (f) show the MF obtained using the stars in the JWST region and combining Gaia and JWST data. For JWST data, we adopted two different approaches based on the PMs and statistical decontamination. In panel (e), the MF is fitted with three different straight lines ( $\alpha$ slopes are reported in the panel) corresponding to different mass intervals. In panel (f), we adopted a logistic function (see text for details).
weighted sum of the number of stars considering the non-MPs as weights. Next, we determined the mean number of expected field stars per unit F277W magnitude by dividing the sum by 0.75 (the F277W magnitude range). We obtained a contamination factor of 22.8 stars/F277W magnitude. We subtracted this value appropriately from the number of stars counted in each magnitude interval used to construct the LFs. The resulting MF is represented by orange squares in panel (e) of Fig. 15. Since the total MF does not conform to a single power law, we fitted three straight lines to the $\mathrm{d} N / \mathrm{d} M$ versus $M$ distribution in different mass intervals: for the mass range $0.8 \mathrm{M}_{\odot}<M \leq 1.4 \mathrm{M}_{\odot}$, we obtained a power-law exponent $\alpha=$ $-1.74 \pm 0.22$; for masses $0.3 \mathrm{M}_{\odot}<M \leq 0.8 \mathrm{M}_{\odot}$, the best-fit was
obtained for $\alpha=-0.82 \pm 0.17$; finally, in the low-mass regime $0.1 \mathrm{M}_{\odot} \leq M \leq 0.3 \mathrm{M}_{\odot}$ we measured $\alpha=-0.18 \pm 0.10$.

We computed the total mass for stars in the JWST region with masses in the interval $0.10 \mathrm{M}_{\odot} \leq M \leq 1.46 \mathrm{M}_{\odot}$, and obtained $M_{\text {cluster, JWST }}\left[0.10 \mathrm{M}_{\odot} \leq M \leq 1.46 \mathrm{M}_{\odot}\right]=601 \pm 21 \mathrm{M}_{\odot}$, of which $\sim 50$ per cent is due to stars with masses between 0.74 and $1.46 \mathrm{M}_{\odot}$. We found that the combined MF obtained from JWST and Gaia data can be well described by the logistic function:
$\log \left(\frac{\mathrm{d} N}{\mathrm{~d} M}\right)=\frac{c}{1+a \exp (-b \log M)}$

Table 3. MFs of MS stars in NGC 2506.

| Global MF from Gaia DR3 catalogue |  |  |  |
| :---: | :---: | :---: | :---: |
| $\mathbf{R}$ interval (arcmin) | $\begin{gathered} M \text { interval } \\ \left(\mathrm{M}_{\odot}\right) \end{gathered}$ | $\begin{gathered} \text { Mean } \boldsymbol{M} \\ \left(\mathrm{M}_{\odot}\right) \end{gathered}$ | (dN/ $\Delta M$ ) |
| 0.00-33.00 | 0.74-0.79 | 0.77 | $5168 \pm 335$ |
|  | 0.79-0.84 | 0.81 | $4175 \pm 288$ |
|  | 0.84-0.88 | 0.86 | $4699 \pm 331$ |
|  | 0.88-0.94 | 0.91 | $3505 \pm 244$ |
|  | 0.94-0.99 | 0.97 | $3846 \pm 274$ |
|  | 0.99-1.06 | 1.02 | $2938 \pm 209$ |
|  | 1.06-1.14 | 1.10 | $2474 \pm 178$ |
|  | 1.14-1.23 | 1.18 | $2132 \pm 151$ |
|  | 1.23-1.34 | 1.29 | $1765 \pm 126$ |
|  | 1.34-1.46 | 1.40 | $1526 \pm 109$ |
| Local MFs from Gaia DR3 catalogue |  |  |  |
| $\mathbf{R}$ interval (arcmin) | $\begin{gathered} M \text { interval } \\ \left(\mathrm{M}_{\odot}\right) \end{gathered}$ | $\begin{gathered} \text { Mean } \boldsymbol{M} \\ \left(\mathrm{M}_{\odot}\right) \end{gathered}$ | (dN/ $\Delta M$ ) |
| 0.00-3.85 | 0.74-0.79 | 0.76 | $1026 \pm 149$ |
|  | 0.79-0.84 | 0.82 | $1254 \pm 158$ |
|  | 0.84-0.88 | 0.86 | $1094 \pm 160$ |
|  | 0.88-0.94 | 0.91 | $763 \pm 114$ |
|  | 0.94-0.99 | 0.97 | $1307 \pm 160$ |
|  | 0.99-1.06 | 1.02 | $1012 \pm 123$ |
|  | 1.06-1.14 | 1.10 | $810 \pm 102$ |
|  | 1.14-1.23 | 1.19 | $798 \pm 92$ |
|  | 1.23-1.34 | 1.29 | $725 \pm 81$ |
|  | 1.34-1.46 | 1.41 | $636 \pm 70$ |
| 3.85-8.33 | 0.74-0.79 | 0.77 | $1939 \pm 205$ |
|  | 0.79-0.84 | 0.81 | $1263 \pm 158$ |
|  | 0.84-0.88 | 0.86 | $1642 \pm 196$ |
|  | 0.88-0.94 | 0.91 | $1181 \pm 142$ |
|  | 0.94-0.99 | 0.96 | $1075 \pm 145$ |
|  | 0.99-1.06 | 1.02 | $893 \pm 115$ |
|  | 1.06-1.14 | 1.10 | $926 \pm 109$ |
|  | 1.14-1.23 | 1.18 | $652 \pm 83$ |
|  | $1.23-1.34$ | 1.29 | $593 \pm 73$ |
|  | 1.34-1.46 | 1.39 | $456 \pm 60$ |
| 8.33-33.00 | 0.74-0.79 | 0.77 | $2043 \pm 211$ |
|  | 0.79-0.84 | 0.81 | $1532 \pm 174$ |
|  | 0.84-0.88 | 0.86 | $1891 \pm 210$ |
|  | 0.88-0.94 | 0.91 | $1526 \pm 161$ |
|  | 0.94-0.99 | 0.97 | $1399 \pm 165$ |
|  | 0.99-1.06 | 1.02 | $971 \pm 120$ |
|  | 1.06-1.14 | 1.09 | $735 \pm 97$ |
|  | 1.14-1.23 | 1.17 | $657 \pm 84$ |
|  | 1.23-1.34 | 1.30 | $438 \pm 63$ |
|  | 1.34-1.46 | 1.39 | $427 \pm 58$ |
| Local MFs from Gaia DR3 \& JWST catalogues ( $0.24 \leq R \leq 4.61$ arcmin) |  |  |  |
| Region | $\begin{gathered} M \text { interval } \\ \left(\mathrm{M}_{\odot}\right) \end{gathered}$ | $\begin{gathered} \text { Mean } \boldsymbol{M} \\ \left(\mathrm{M}_{\odot}\right) \end{gathered}$ | (dN/ $\Delta M$ ) |
| JWST stat. decont. | 0.10-0.16 | 0.14 | $1816 \pm 179$ |
|  | 0.16-0.28 | 0.21 | $1570 \pm 114$ |
|  | 0.28-0.37 | 0.32 | $1549 \pm 131$ |
|  | 0.37-0.46 | 0.42 | $1022 \pm 106$ |
|  | 0.46-0.58 | 0.52 | $999 \pm 93$ |
|  | 0.58-0.93 | 0.74 | $787 \pm 47$ |
| JWST PMs decont. | 0.37-0.55 | 0.46 | $939 \pm 73$ |
|  | 0.55-0.74 | 0.63 | $715 \pm 61$ |
|  | 0.74-0.93 | 0.82 | $724 \pm 61$ |
| Gaia DR3 | 0.74-0.85 | 0.79 | $559 \pm 73$ |
|  | 0.85-0.96 | 0.91 | $511 \pm 68$ |
|  | 0.96-1.10 | 1.02 | $396 \pm 53$ |
|  | 1.10-1.25 | 1.19 | $393 \pm 52$ |
|  | $1.25-1.46$ | 1.35 | $254 \pm 34$ |

as shown in panel (f) of Fig. 15. The best-fitting parameters were determined as $a=0.231 \pm 0.020, b=-3.436 \pm 0.531$, and $c=$ $3.290 \pm 0.048$. By integrating this function, we obtained a total mass $M_{\text {cluster, JWST }}\left[0.10 \mathrm{M}_{\odot} \leq M \leq 1.46 \mathrm{M}_{\odot}\right]=614 \pm 77 \mathrm{M}_{\odot}$, in agreement with the value found by using three power laws.

We used this just derived information on the MFs within the JWST region to obtain an estimate for the present-day total mass of the stellar cluster NGC 2506 based only on stars with masses ranging between 0.1 and $1.46 \mathrm{M}_{\odot}$. In this calculation we assume that the relative number of stars of different mass in the entire cluster is the same as that observed within the annulus covered by JWST, i.e. within $0.24 \leq R \leq 4.61$ arcmin. We then calculated the total mass of the cluster in this annulus and scaled it to the total region occupied by the cluster. We obtained $M_{\text {cluster, } 0.24-4.6 \text { larcmin }}=M_{\text {cluster, JWST }} \times$ $A($ annulus $) / A(\mathrm{JWST})=2021 \pm 150 \mathrm{M}_{\odot}$ where $A($ annulus $) / A(\mathrm{JWST})$ is the ratio between the area of the annulus and the area covered by JWST observations. We then calculated the cluster mass in an annulus between $4.61 \leq R \leq 33.00$ arcmin using stars with masses between 0.74 and $1.46 \mathrm{M}_{\odot}$ included in the Gaia catalogue; we found a mass of $1223 \pm 47 \mathrm{M}_{\odot}$, which is $\sim 59$ per cent of the total mass previously calculated for this mass range. Supposing that the mass distribution is the same in the two radial bins, we calculated a total mass equal to $\sim 5863 \mathrm{M}_{\odot} .{ }^{11}$ This must be considered as a lower limit of the present-day total mass because it does not take into account, i.e. of the evolved stars (giant stars, white dwarfs, etc.), of stars with masses $<0.1 \mathrm{M}_{\odot}$, and of the brown dwarfs.

## 6 WHITE DWARFS IN NGC 2506

We investigated the presence of white dwarfs (WDs) in the JWST CMDs of NGC 2506 using the bluer, higher SNR filters, i.e. F070W, F090W, and F150W, where WDs are expected to be more prominent. The results are presented in Fig. 16 and Table 4. The left-most panel shows the $m_{\text {F090W }}$ versus ( $m_{\text {F070w }}-m_{\text {F150W }}$ ) CMD of the stars that passed the selection and membership criteria in grey and black, respectively. The isochrone of WDs with an age of 2 Gyr is depicted in red. This WD isochrone has been calculated as described in Griggio et al. (2023a) using the BaSTI-IAC WD cooling models by Salaris et al. (2022) for progenitors with initial $[\mathrm{M} / \mathrm{H}]=-0.40$. We obtain essentially the same isochrone if we use cooling models from progenitors with $[\mathrm{M} / \mathrm{H}]=-0.20$, the other metallicity in the WD BaSTI-IAC database close to the cluster $[\mathrm{M} / \mathrm{H}]$. The green square shows the only WD with a high-MP ( 92.1 per cent), as consistently located along the WD cooling sequence. According to the initial-final mass relation adopted in the calculation of the isochrone (Cummings et al. 2018) the mass of this WD is $\sim 0.62 \mathrm{M}_{\odot}$.

This same star (WD1, $V=22.74 \pm 0.08, I=23.07 \pm 0.03$ ) is also displayed in the $V$ versus $(V-I)$ CMD obtained with the WFC@INT data set, where it also closely matches the WD isochrone within the measurement errors. The azure squares in the left-most panel represent other sources near the WD isochrone but without proper motion measurements, which should be considered as candidate WDs. A suitable astrometric second epoch appears as the most efficient way to confirm as members these WD candidates. We visually examined these five sources using three-colour stacked images obtained with the same filters employed for the CMDs.

[^7]

Figure 16. The left-hand panels show the $m_{\mathrm{F} 090 \mathrm{~W}}$ versus ( $m_{\mathrm{F} 070 \mathrm{~W}}-m_{\mathrm{F} 150 \mathrm{~W}}$ ) and the $V$ versus $(V-I)$ CMDs of NGC 2506 obtained with the NIRCam@JWST and WFC@INT data sets. In the left-most panel the grey and black points are stars that passed the selection and membership criteria, respectively. Green and azure squares represent the sources that, based on their membership and/or position on the CMDs, may be considered candidate WDs. In red are reported the 2 Gyr WD isochrones; dotted lines represent the isochrone boundaries considering the errors on the distance modulus and reddening. The finding charts of the candidate WDs are shown in the right-hand panels. The field of view of $J W S T$ finding charts is $1.2 \times 1.2 \operatorname{arcsec}^{2}$, while the WFC finding chart is $6.5 \times 6.5$ $\operatorname{arcsec}^{2}$. Sources WD1, WD2, and WD3 appear as point-like stars, while WD4 and WD5 should be noisy peaks.

Table 4. Candidate WDs identified in NGC 2506.

| WD | $\alpha$ <br> $($ deg. $)$ | $\delta$ <br> $(\mathrm{deg})$. | $m_{\mathrm{F} 090 \mathrm{~W}}$ | $m_{\mathrm{F} 070 \mathrm{~W}}$ |
| :--- | :---: | :---: | :---: | :---: |
| 1 | 120.0166589 | -10.8069775 | $22.95 \pm 0.05$ | $22.79 \pm 0.06$ |
| 2 | 120.0102662 | -10.8069270 | $23.13 \pm 0.06$ | $22.94 \pm 0.03$ |
| 3 | 120.0571064 | -10.7940803 | $23.98 \pm 0.02$ | $23.50 \pm 0.06$ |
| 4 | 120.0296222 | -10.7618422 | $25.40 \pm 0.04$ | $25.11 \pm 0.03$ |
| 5 | 120.0466738 | -10.8187002 | $25.52 \pm 0.01$ | $24.71 \pm 0.14$ |

The results are presented in the right-hand panels: candidate WDs 1,2 , and 3 appear as clear point-like sources in both the JWST and WFC@INT images. On the other hand, WD4 and WD5 likely correspond to noisy peaks that passed the selection criteria. However, with deeper data collected by either HST or JWST in the future, this ambiguity may be resolved.

## 7 SUMMARY

In this work we have exploited JWST non-proprietary calibration data to: (i) derive accurate effective PSFs for ten filters (8 wide +2 medium), spanning a wavelength interval from 0.7 to $4.5 \mu \mathrm{~m}$; (ii) extract high-precision photometry and astrometry from 'shallow' NIRCam images for stars located in the region that encompasses a portion of the 2 Gyr open cluster NGC 2506 ; (iii) calculate the proper motions for MS stars with masses $\gtrsim 0.3 \mathrm{M}_{\odot}$ by adopting ground-based data collected with the INT a taking advantage of the large temporal baseline ( $\sim 18.8$ yr) between JWST and INT data; (iv)
carry-out an in-depth analysis of the cluster properties by leveraging the synergy between JWST data and the Gaia DR3 catalogue.

We have calculated the radial stellar density profile by using the Gaia DR3 catalogue, fitted with a King profile. From the fitting, we derive the central stellar density $\left(k_{0}=28.1 \pm 0.9{\left.\text { stars } \operatorname{arcmin}^{-2}\right) \text {, }}_{\text {d }}\right.$, the core radius ( $r_{\mathrm{c}}=2.60 \pm 0.05 \mathrm{arcmin}$ ), and the tidal radius ( $r_{\mathrm{t}}=$ $33.0 \pm 4.3$ arcmin).

From the combination of JWST and Gaia DR3 data, we calculated the fraction of MS binaries with mass ratio $q \geq 0.6$, equal to $\sim 23$ percent. This synergy allowed us to extend the study of the MS binary fraction down to $\sim 0.4 \mathrm{M}_{\odot}$, well below the Gaia limit ( $\sim 0.8 \mathrm{M}_{\odot}$ ). Our findings reveal no dependence of the binary fraction on the primary mass within a mass range between 0.44 and 1.13 $\mathrm{M}_{\odot}$. However, we observed a hint of a radial trend in the radial distribution of the MS binary fraction between the cluster centre and approximately $2 r_{\mathrm{c}}$.

Similarly, by leveraging the synergy between JWST and Gaia DR3, we computed MFs of MS stars within the mass interval from $\sim 0.10$ to $\sim 1.45 \mathrm{M}_{\odot}$. First, we examined the MFs using solely Gaia DR3
data. Our analysis confirmed the influence of mass segregation on the MFs calculated in various radial bins for masses ranging from $\sim 0.7$ to $\sim 1.4 \mathrm{M}_{\odot}$. By integrating these MFs, we determined that the total mass of stars within the range from 0.74 to $1.46 \mathrm{M}_{\odot}$ is $\sim 2065 \mathrm{M}_{\odot}$. We then focused on the region covered by JWST data ( $0.24 \leq R \leq 4.61$ arcmin). We found that the MF for stars with masses between $\sim 0.1$ and $\sim 1.4 \mathrm{M}_{\odot}$ is well represented by a logistic function. By calculating the total mass of stars within this region $\left(\sim 600 \mathrm{M}_{\odot}\right)$ and assuming a homogeneous mass distribution, we estimated the total mass within $R \leq 4.61 \mathrm{arcmin}$ to be $\sim 2021 \mathrm{M}_{\odot}$. We used this number to put a lower limit on the total mass of the cluster, which is estimated to be about $6000 \mathrm{M}_{\odot}$.

Finally, using the bluest JWST available filters, we identified five candidate white dwarfs. Among them, WD1 stands out as the strongest candidate due to its relatively high brightness, the high MP and alignment with the theoretical 2 Gyr white dwarf cooling sequence (also on the ground-based CMD). A preliminary estimate suggests that the mass of WD1 is $\sim 0.62 \mathrm{M}_{\odot}$. However, to resolve the ambiguity surrounding these candidates, it will be necessary to acquire new, deeper data using instruments such as $H S T$ or JWST.

As a by-product of this work, we release the derived ePSFs and the JWST catalogues and atlases of NGC 2506 (see Appendix B).

This study has demonstrated the potential of using JWST's publicly available calibration images in combination with the Gaia catalogue, to conduct a pioneering multiband analysis of stellar populations in open clusters within the IR wavelength range. With a minimum effort of observing time, we were able to probe the faint end of the MS in this peculiar, old, and distant open cluster. Future NIRCam deeper observations of different open clusters, spanning multiple years, will enable us to easily explore their brown dwarf sequence, study the MFs and evaporation effects of low-mass stars ( $<0.2 \mathrm{M}_{\odot}$ ), the internal kinematic via proper-motions, as well as investigate their white dwarf cooling sequences, advancing our understanding of stellar populations in star clusters and shedding light on the diverse phenomena within these systems.

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## DATA AVAILABILITY

The data underlying this article are publicly available in the Mikulski Archive for Space Telescopes at https://mast.stsci.edu/. The catalogues underlying this work are available in the online supplementary material of the article.

## REFERENCES

Anderson J., 2016, Empirical Models for the WFC3/IR PSF, Instrument Science Report WFC3 2016-12, p. 42
Anderson J., King I. R., 2000, PASP, 112, 1360
Anderson J., King I. R., 2004, Multi-filter PSFs and Distortion Corrections for the HRC, Instrument Science Report ACS 2004-15. p. 51
Anderson J., King I. R., 2006, PSFs, Photometry, and Astronomy for the ACS/WFC, Instrument Science Report ACS 2006-01. 34
Anderson J., Bedin L. R., Piotto G., Yadav R. S., Bellini A., 2006, A\&A, 454, 1029
Anderson J. et al., 2008, AJ, 135, 2114
Anderson J., Bourque M., Sahu K., Sabbit E., Viana A., 2015, A Study of the Time Variability of the PSF in F606W Images taken with the WFC3/UVIS, Instrument Science Report WFC3 2015-08. p. 19
Anthony-Twarog B. J., Atwell J., Twarog B. A., 2005, AJ, 129, 872
Anthony-Twarog B. J., Tanner D., Cracraft M., Twarog B. A., 2006, AJ, 131, 461
Anthony-Twarog B. J., Deliyannis C. P., Twarog B. A., 2016, AJ, 152, 192
Anthony-Twarog B. J., Lee-Brown D. B., Deliyannis C. P., Twarog B. A., 2018, AJ, 155, 138
Arentoft T. et al., 2007, A\&A, 465, 965
Bailer-Jones C. A. L., Rybizki J., Fouesneau M., Demleitner M., Andrae R., 2021, AJ, 161, 147
Bedin L. R., Piotto G., King I. R., Anderson J., 2003, AJ, 126, 247
Bedin L. R., Piotto G., Anderson J., Cassisi S., King I. R., Momany Y., Carraro G., 2004, ApJ, 605, L125
Bedin L. R., King I. R., Anderson J., Piotto G., Salaris M., Cassisi S., Serenelli A., 2008, ApJ, 678, 1279

Bellini A. et al., 2010, A\&A, 513, A50
Bellini A., Anderson J., Salaris M., Cassisi S., Bedin L. R., Piotto G., Bergeron P., 2013, ApJ, 769, L32

Bellini A., Anderson J., Bedin L. R., King I. R., van der Marel R. P., Piotto G., Cool A., 2017, ApJ, 842, 6

Boubert D., Everall A., 2020, MNRAS, 497, 4246
Cantat-Gaudin T., Anders F., 2020, A\&A, 633, A99
Carretta E., Bragaglia A., Gratton R. G., Tosi M., 2004, A\&A, 422, 951
Chambers K. C. et al., 2016, preprint (arXiv:1612.05560)
Cordoni G. et al., 2023, A\&A, 672, A29
Cummings J. D., Kalirai J. S., Tremblay P. E., Ramirez-Ruiz E., Choi J., 2018, ApJ, 866, 21
de Pater I. et al., 2022, in AAS/Division for Planetary Sciences Meeting Abstracts. Bulletin of the American Astronomical Society, Vol. 54, p. 306.07

Dieball A., Bedin L. R., Knigge C., Rich R. M., Allard F., Dotter A., Richer H., Zurek D., 2016, ApJ, 817, 48

Everall A., Boubert D., 2022, MNRAS, 509, 6205
Feinstein A. D. et al., 2023, Nature, 614, 670
Gaia Collaboration, 2021, A\&A, 649, A1
Gaia Collaboration et al., 2023, A\&A, 674, A1
Gao X., 2020, ApJ, 894, 48
Gardner J. P. et al., 2023, PASP, 135, 068001
Griggio M., Bedin L. R., 2022, MNRAS, 511, 4702
Griggio M. et al., 2022, MNRAS, 515, 1841

Griggio M. et al., 2023a, MNRAS, 524, 108
Griggio M., Nardiello D., Bedin L. R., 2023b, Astron. Nachr., 344, e20230019 (Paper II)
Hidalgo S. L. et al., 2018, ApJ, 856, 125
King I., 1962, AJ, 67, 471
King I. R., Bedin L. R., Piotto G., Cassisi S., Anderson J., 2005, AJ, 130, 626
Knudstrup E. et al., 2020, MNRAS, 499, 1312
Lee S. H., Kang Y. W., Ann H. B., 2013, MNRAS, 432, 1672
Libralato M., Bellini A., Bedin L. R., Piotto G., Platais I., Kissler-Patig M., Milone A. P., 2014, A\&A, 563, A80
Libralato M., Bedin L. R., Nardiello D., Piotto G., 2016a, MNRAS, 456, 1137
Libralato M. et al., 2016b, MNRAS, 463, 1780
Libralato M. et al., 2023, ApJ, 950, 101
Magnier E. A. et al., 2020, ApJS, 251, 3
McClure R. D., Twarog B. A., Forrester W. T., 1981, ApJ, 243, 841
Mikolaitis Š., Tautvaišienė G., Gratton R., Bragaglia A., Carretta E., 2011, MNRAS, 416, 1092
Milone A. P. et al., 2012, A\&A, 540, A16
Milone A. P. et al., 2016, MNRAS, 455, 3009
Milone A. P. et al., 2019, MNRAS, 484, 4046
Naidu R. P. et al., 2022, ApJ, 940, L14
Nardiello D., Milone A. P., Piotto G., Marino A. F., Bellini A., Cassisi S., 2015, A\&A, 573, A70
Nardiello D., Libralato M., Bedin L. R., Piotto G., Ochner P., Cunial A., Borsato L., Granata V., 2016a, MNRAS, 455, 2337
Nardiello D., Libralato M., Bedin L. R., Piotto G., Borsato L., Granata V., Malavolta L., Nascimbeni V., 2016b, MNRAS, 463, 1831
Nardiello D. et al., 2018a, MNRAS, 477, 2004
Nardiello D. et al., 2018b, MNRAS, 481, 3382
Nardiello D., Piotto G., Milone A. P., Rich R. M., Cassisi S., Bedin L. R., Bellini A., Renzini A., 2019, MNRAS, 485, 3076
Nardiello D., Bedin L. R., Burgasser A., Salaris M., Cassisi S., Griggio M., Scalco M., 2022, MNRAS, 517, 484 (Paper I)
Nardiello D., Griggio M., Bedin L. R., 2023, MNRAS, 521, L39
Netopil M., Paunzen E., Heiter U., Soubiran C., 2016, A\&A, 585, A150
Panthi A., Vaidya K., Jadhav V., Rao K. K., Subramaniam A., Agarwal M., Pandey S., 2022, MNRAS, 516, 5318
Paris D. et al., 2023, ApJ, 952, 20
Pietrinferni A. et al., 2021, ApJ, 908, 102
Piotto G. et al., 2007, ApJ, 661, L53
Piotto G. et al., 2015, AJ, 149, 91
Rangwal G., Yadav R. K. S., Durgapal A., Bisht D., Nardiello D., 2019, MNRAS, 490, 1383
Richer H. B. et al., 2008, AJ, 135, 2141
Rieke M. J. et al., 2023, PASP, 135, 028001
Sabbi E. et al., 2016, ApJS, 222, 11
Salaris M., Cassisi S., Pietrinferni A., Hidalgo S., 2022, MNRAS, 509, 5197
Scalco M. et al., 2021, MNRAS, 505, 3549
Schlafly E. F., Finkbeiner D. P., 2011, ApJ, 737, 103

Schlegel D. J., Finkbeiner D. P., Davis M., 1998, ApJ, 500, 525
Stetson P. B., 2000, PASP, 112, 925
Tarricq Y. et al., 2021, A\&A, 647, A19
Waters C. Z. et al., 2020, ApJS, 251, 4
Ziliotto T. et al., 2023, ApJ, 953, 62

## SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.
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## APPENDIX A: PSF VARIATIONS ACROSS THE DETECTORS

Given the great level of accuracy of our here-derived secondgeneration PSFs, significantly improved (if compared with the PSFs from Paper I) thanks to the available GD corrections (derived only in Paper II), we can now provide the community with an independent determination of the average spatial properties of the PSFs. Indeed, it would be particularly useful to know precisely where to place a target to obtain the highest possible angular resolution with NIRCam@JWST observations. Given the dependency of the angular resolution on the wavelength for a diffraction-limited 'optical' (actually, IR) system, the bluest filters are those expected to show the maxima spatial variations, as they would amplify relative differences. Furthermore, the undersampled nature of NIRCam PSFs of bluest filters makes the PSFs of the filters F070W/F090W/F115W the hardest PSFs to solve for.

In Fig. A1, we show the spatial determination of PSFs's peaks in the most undersampled filter F070W, obtained by interpolating the $5 \times 5$ perturbed PSF arrays of all the images. PSFs values are normalized to 1 within an area of $5.25 \times 5.25$ physical pixels. So a value of 0.47 , meaning that the central pixels, of a source centred at the centre of a pixels, contain 47 per cent of the normalized flux. Fig. A1 reveals that Module A (on the left) has a sharpest'sweet spot' in a region between the four detectors, where targets that need the highest angular resolution (full width at half-maximum $\sim 35$ mas, containing 47 per cent of the light in its central pixel) should be placed. Also Module B shows a slightly less-peaked sweet spot than Module A, and relatively off-centre, mainly within B4.

These differences between PSFs at different spatial position within NIRCam field of view, become less and less important moving to redder wavelengths.


Figure A1. Variation across the detector of the peak of the PSF in F070W filter.

## APPENDIX B: ELECTRONIC MATERIAL

The catalogues of NGC 2506 extracted in this work will be released as supporting material to this paper. We will release two catalogues, one for each field of view covered by Module A and B, that contain information on the position of the stars, the VEGAmag calibrated magnitudes in the 10 JWST filters, the quality parameters described in Section 2.2.1, the quality flag of the selections described in

Section 2.2.1; the proper motions and the MPs, and the completeness associated to each star. We will also make publicly available the ePSFs and the stacked images in each filter derived in this work at the website: https://web.oapd.inaf.it/bedin/fil es/PAPERs_eMATERIALs/JWST/. At the same website we will upload the NGC 2506 catalogues.

This paper has been typeset from a $\mathrm{T}_{\mathrm{E}} \mathrm{X} / \mathrm{ET} \mathrm{T}_{\mathrm{E}} \mathrm{X}$ file prepared by the author.


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[^1]:    ${ }^{2}$ For each filter, the 'closest' PSF set in terms of wavelength was utilized.

[^2]:    ${ }^{1}$ https://jwst-pipeline.readthedocs.io/

[^3]:    ${ }^{3}$ In this work, we utilized a modified private copy of the KS2 software specifically adapted to NIRCam images.

[^4]:    ${ }^{4}$ Version 5, November 2022
    ${ }^{5}$ https://jwst-docs.stsci.edu/jwst-near-infrared-camera/nircam-performance /nircam-absolute-flux-calibration-and-zeropoints
    ${ }^{6}$ https://jwst-docs.stsci.edu/jwst-near-infrared-camera/nircam-performance /nircam-point-spread-functions
    ${ }^{7}$ https://jwst-docs.stsci.edu/files/182256933/182256934/1/1669487685625 /NRC_ZPs_0995pmap.txt

[^5]:    ${ }^{8}$ https://irsa.ipac.caltech.edu/applications/DUST/
    ${ }^{9}$ https://www.cadc-ccda.hia-iha.nrc-cnrc.gc.ca/en/community/-STETSON /homogeneous/

[^6]:    ${ }^{10}$ It is worth noting that $m_{\text {F277W }}=18.50$ was chosen as the faint end due to the rapid decline in completeness in the F070W filter at fainter magnitudes, making it nearly impossible to measure the binary fraction using other filter combinations where the MS is vertical.

[^7]:    ${ }^{11}$ In this calculation, we excluded the central region $0.00 \leq R \leq 0.24$ arcmin, because in the Gaia catalogue only seven cluster members are present, and it was not possible to calculate the MF. We considered the contribution of this region negligible compared to the errors on the total mass.

