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# Insights into refinement mechanism of primary $M_7C_3$ carbide by $La_2O_3$ via experiments and first-principles calculations

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## ABSTRACT

This study is dedicated to summarize refinement mechanism of the primary  $M_7C_3$  carbide by rare earth oxide  $La_2O_3$ . The  $La_2O_3$  was added into hypereutectic Fe–27Cr–4C alloy, and its microstructure was observed and analyzed by optical microscope (OM), X-ray diffractometer (XRD) and scanning electron microscope (SEM). The lattice mismatch degrees of  $La_2O_3/M_7C_3$  interfaces were calculated. The interface properties of  $La_2O_3/M_7C_3$  were calculated by the first principles. The effectiveness of  $La_2O_3$  as the heterogeneous nucleus of the primary  $M_7C_3$  carbide in the alloy was analyzed. The results show that the primary  $M_7C_3$  carbide can be refined by  $La_2O_3$  in this alloy. The lattice mismatch degree between  $La_2O_3(111)$  plane and  $M_7C_3(0001)$  plane is 2.36%, which indicates that  $La_2O_3$  as the heterogeneous nucleus of  $M_7C_3$  is the most effective.  $La_2O_3(111)$  plane and  $M_7C_3(0001)$  plane were chosen to construct the interface models. Two surface models, such as La-termination and O1-termination on  $La_2O_3(111)$  plane were constructed, which converge to 26 and 21 layers, and their surface energies are 5.256 J/m<sup>2</sup> and 2.029 J/m<sup>2</sup>, respectively. The surface model of  $M_7C_3(0001)$  plane converges to 17 layers, and its surface energy is 3.199 J/m<sup>2</sup>. Among La- $M_7C_3$  and O1- $M_7C_3$  interfaces, the adhesion work (16.162 J/m<sup>2</sup>) of O1- $M_7C_3$  is larger than that (1.731 J/m<sup>2</sup>) of La- $M_7C_3$ . However, the interface energy (–10.910 J/m<sup>2</sup>) of O1- $M_7C_3$  is smaller than that (6.725 J/m<sup>2</sup>) of La- $M_7C_3$ , which indicates that O1- $M_7C_3$  interface has the best interface bonding property and the lowest interface nucleation resistance. Therefore,  $La_2O_3$  can serve as the heterogeneous nucleus of  $M_7C_3$  and tends to form an O1- $M_7C_3$  heterogeneous nucleation interface.

## 1. Introduction

Hypereutectic Fe–Cr–C alloy coating has excellent wear resistance, which has been widely applied in additive manufacturing industry [1,2]. The primary  $M_7C_3$  carbide is the strengthening phase of the coating. The service life of the workpieces manufactured by the hypereutectic Fe–Cr–C alloy is determined by large number of the dispersed primary  $M_7C_3$  carbide [3,4]. During the solidification process, the primary  $M_7C_3$  carbides precipitate directly from the liquid metal and grow rapidly. Until the eutectic reaction occurs, the precipitation process of the primary  $M_7C_3$  carbide ends, which exist with large size and polygon in the eutectic matrix [5]. During the service of the workpieces manufactured by this coating, the primary  $M_7C_3$  carbides tend to peel off from the

surface of the workpieces, so as to reduce its service life [6,7]. Therefore, it is the significant to refine the primary  $M_7C_3$  carbide for improving the service performance of the hypereutectic Fe–Cr–C alloy coating.

In recent years, with its high melting point and stability, the typical rare earth oxide  $La_2O_3$  has been directly applied into various alloys to improve the microstructure and enhance the mechanical property, corrosion resistance and wear resistance [8,9]. Chen et al. [10] investigated the addition of  $La_2O_3$  on grain refinement of additive manufactured Ti-6.5Al-3.5Mo-1.5Zr-0.3Si titanium alloy. The results show that the  $La_2O_3$  can significantly refine the prior  $\beta$  grains. Zhou et al. [11] analyzed the effect of  $La_2O_3$  addition on microstructure and mechanical properties of TiC-based cermets. It can be seen that the toughness and density are increased as a result of the well-developed grey rims around

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the black cores and the wettability between the ceramic and metallic phases is improved. Qu et al. [12] studied the corrosion and wear properties of TB2 titanium alloy borided by pack boriding with  $\text{La}_2\text{O}_3$ . It was found that the wear and corrosion resistances of TB2 alloy are enhanced by boriding with  $\text{La}_2\text{O}_3$ .

Currently, it is intriguing to add  $\text{La}_2\text{O}_3$  into the hypereutectic Fe–Cr–C alloy coating to refine the primary  $\text{M}_7\text{C}_3$  carbide. Yang et al. [13] studied the microstructure and wear resistance of the hypereutectic Fe–Cr–C alloy coating with different  $\text{La}_2\text{O}_3$  additives. It was found that with the increase of the  $\text{La}_2\text{O}_3$  addition, the dimension of the primary  $\text{M}_7\text{C}_3$  carbide in the coating is decreased gradually and its wear resistance is increased firstly then decreased and reaches the most excellent when the  $\text{La}_2\text{O}_3$  addition is 0.78 wt%. However, the mechanism of the primary  $\text{M}_7\text{C}_3$  carbide was refined by  $\text{La}_2\text{O}_3$  in this coating has not been reported. Moreover, it is difficult to determine the interfacial properties between  $\text{La}_2\text{O}_3$  and  $\text{M}_7\text{C}_3$  carbide by experimental method, so as to reveal whether  $\text{La}_2\text{O}_3$  can be as the heterogeneous nucleus of the primary  $\text{M}_7\text{C}_3$  carbide.

At present, the first principles methods have been widely applied to study the surface and interface for different material, and explain the bonding characteristics among atoms from the electronic structure [14, 15]. Jiao et al. [16] calculated on the  $\gamma\text{-Fe}/\text{La}_2\text{O}_3$  interface properties by first-principles and analyzed the austenite refinement mechanism by  $\text{La}_2\text{O}_3$ . Lu et al. [17] studied the influence of solute elements (Cr, Mo, Fe, Co) on the binding properties of WC/Ni interface by using the first-principles method, and found that element Mo would reduce the binding strength of WC/NiMo interface, while the addition of elements Cr and Mo would enhance the binding strength of the interface. Therefore, it is feasible to investigate the interfacial structure and bonding strength between  $\text{La}_2\text{O}_3$  and  $\text{M}_7\text{C}_3$  carbide at atomic scale by first principles calculation, and explain the mechanism of the primary  $\text{M}_7\text{C}_3$  carbide refined by  $\text{La}_2\text{O}_3$ .

In this paper, the microstructure of the hypereutectic Fe–27Cr–4C alloy coating with  $\text{La}_2\text{O}_3$  was observed and analyzed by optical microscope (OM), X-ray diffractometer (XRD) and scanning electron microscope (SEM). The lattice mismatch degrees of  $\text{La}_2\text{O}_3//\text{M}_7\text{C}_3$  interfaces were calculated. The interface properties of  $\text{La}_2\text{O}_3//\text{M}_7\text{C}_3$  interfaces were also calculated by the first principles. The effectiveness of  $\text{La}_2\text{O}_3$  as the heterogeneous nucleus of the primary  $\text{M}_7\text{C}_3$  carbide in hypereutectic Fe–Cr–C alloy coating was analyzed.

## 2. Experimental materials and method

### 2.1. Experimental materials

In this paper, the hypereutectic Fe–27Cr–4C alloy coating was designed and prepared by adding  $\text{La}_2\text{O}_3$ , and the additions of  $\text{La}_2\text{O}_3$  were 0 wt% and 0.80 wt%, respectively. Firstly, Axiovert 200 MAT optical microscope (OM), Hitachi S4800 field emission scanning electron microscope (FESEM) with energy dispersive spectrometer (EDS) were used to visualize the microstructure and carbide morphology of the coatings. Then, the phase structure and orientation of the coatings were determined by D/Max-2500/PC X-ray diffractometer (XRD). The coating specimens were smoothed and polished before testing to ensure the reliability of the test data. The X-ray source was Cu-K $\alpha$  target, the range of measurement angle was 20–120°, and the measurement step was 2°/min. The morphology, size and distribution of the carbide in the coatings were quantitatively analyzed by Image-Pro Plus software. Finally, the Talos F200X transmission electron microscope (TEM) was used to observe the crystal structure of the coatings. Model691 precision argon ion thinning instrument (Model691 PIPS) was applied in the ion thinning process for coating specimen preparation.

### 2.2. Computational details

In this paper, the Vienna Ab Initio Simulation Package (VASP) [18]

based on density functional theory was used to optimize the bulk phase structure of  $\text{M}_7\text{C}_3$  and  $\text{La}_2\text{O}_3$ , and their surface and interface properties were calculated. The generalized gradient approximation (GGA) functional modified by Perdew, Burke and Ernzerhof (PBE) was used to calculate and correct the exchange correlation energy [19]. Projection augmented wave (PAW) was used to describe the interaction between ionic nuclei and valence electrons [20]. The suitable plane wave cutoff energy ( $E_{\text{cut}}$ ) and Brillouin K-point grid ( $K_{\text{mesh}}$ ) are selected by convergence test, and the convergence test criteria were as follows. The energy change value was less than  $1 \times 10^{-5}$  eV/atom, the maximum force acting on each atom was less than 0.02 eV/Å, and the maximum displacement was less than  $1.0 \times 10^{-3}$  Å. Therefore,  $E_{\text{cut}}$  was set as 500 eV, and  $K_{\text{mesh}}$  was set as  $5 \times 5 \times 5$  in the optimization of the bulk structure of  $\text{M}_7\text{C}_3$ . When the  $\text{La}_2\text{O}_3$  bulk structure was optimized, the  $E_{\text{cut}}$  was 400 eV and the  $K_{\text{mesh}}$  was  $8 \times 8 \times 8$ . When the surface properties of  $\text{M}_7\text{C}_3$  was calculated,  $E_{\text{cut}}$  was selected as 500 eV and  $K_{\text{mesh}}$  was  $5 \times 5 \times 1$ , which is same as the experimental value [21]. When the interface properties of  $\text{La}_2\text{O}_3$  were calculated,  $E_{\text{cut}}$  was selected as 500 eV and  $K_{\text{mesh}}$  was  $5 \times 5 \times 1$ , which is same as the experimental value [22]. Finally, when their interface properties were calculated, the  $E_{\text{cut}}$  was selected as 500 eV and the  $K_{\text{mesh}}$  was  $5 \times 5 \times 1$ .

## 3. Experimental characterization

### 3.1. Effect of $\text{La}_2\text{O}_3$ on size of the primary $\text{M}_7\text{C}_3$ carbide

The microstructures of the hypereutectic Fe–Cr–C alloy coating with and without  $\text{La}_2\text{O}_3$  are shown in Fig. 1.

Fig. 1(a) is that of the coating with 0.80 wt% addition of  $\text{La}_2\text{O}_3$ . It can be seen that the primary  $\text{M}_7\text{C}_3$  carbides present irregular polygonal distribution. According to the carbide size statistics, the average size of the primary  $\text{M}_7\text{C}_3$  carbides in the coating with  $\text{La}_2\text{O}_3$  is 25  $\mu\text{m}$ . The size change of the primary  $\text{M}_7\text{C}_3$  carbide is not obvious, and the primary  $\text{M}_7\text{C}_3$  carbide are distributed uniformly. Fig. 1(b) is that of the coating without  $\text{La}_2\text{O}_3$ . It can be clearly seen that its average size is 28  $\mu\text{m}$ , and they are not distributed uniformly.

### 3.2. Nucleation analysis

#### 3.2.1. FESEM analysis

The FESEM of the primary  $\text{M}_7\text{C}_3$  carbide with  $\text{La}_2\text{O}_3$  is shown in Fig. 2. It can be clearly seen that there is obvious bright spot on the surface of the polygon and large block primary  $\text{M}_7\text{C}_3$  carbide, which is marked as EDS Spot 1 in Fig. 2, and EDS analysis results are listed in Table 1. From Table 1, a certain amount of element La is detected in the bright spot, which indicates that when  $\text{La}_2\text{O}_3$  is added into the hypereutectic Fe–Cr–C alloy coating,  $\text{La}_2\text{O}_3$  maybe the heterogeneous nucleus of the primary  $\text{M}_7\text{C}_3$  carbide, which can be refined.

The random spot marked as Selected Area 1 on the surface of the primary  $\text{M}_7\text{C}_3$  carbide is shown in Fig. 2, too, and the approximate atomic ratio of the primary  $\text{M}_7\text{C}_3$  carbide can be obtained by EDS analysis, as listed in Table 2. It can be seen that the atomic number ratio of the elements Fe, Cr and C accords with the relationship of 3:4:3, which means that the primary  $\text{M}_7\text{C}_3$  carbide is  $\text{Fe}_3\text{Cr}_4\text{C}_3$  one. Zhang et al. [23] calculated the formation energy of various  $\text{M}_7\text{C}_3$  carbide composed with different Fe and Cr atomic proportions, and found that the formation energy of  $\text{Fe}_3\text{Cr}_4\text{C}_3$  is the lowest, which indicates that it is the most stable. According to the analysis of the experimental results, it is found that the atomic composition of the primary  $\text{M}_7\text{C}_3$  carbide is consistent with the proportion of  $\text{Fe}_3\text{Cr}_4\text{C}_3$ . Therefore, the structure of  $\text{Fe}_3\text{Cr}_4\text{C}_3$  is adopted in the subsequent calculation to simulate that of  $\text{M}_7\text{C}_3$  carbide in this paper.

#### 3.2.2. TEM observation

The TEM bright field image of the coating with  $\text{La}_2\text{O}_3$  is shown in Fig. 3. It can be clearly seen that the region A with significantly different



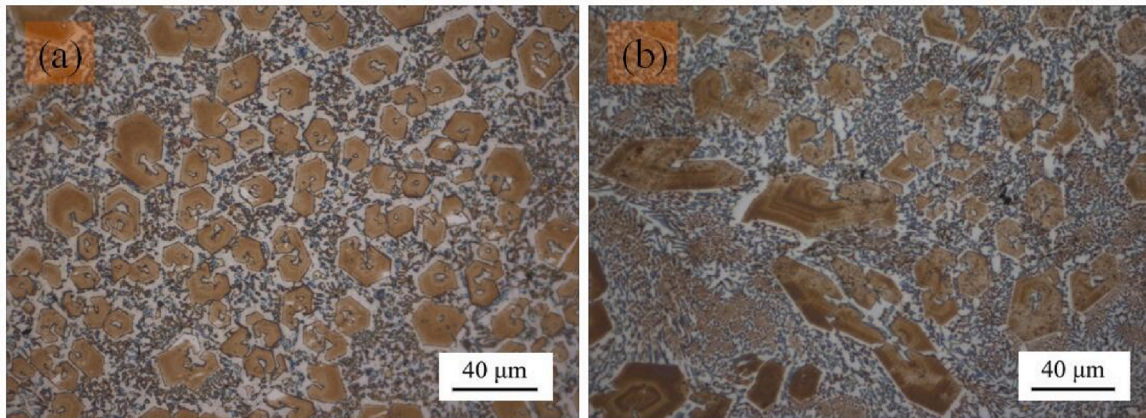


Fig. 1. Microstructures of hypereutectic Fe–Cr–C alloy coating with and without  $\text{La}_2\text{O}_3$ . (a) 0.80 wt%; (b) 0 wt%.

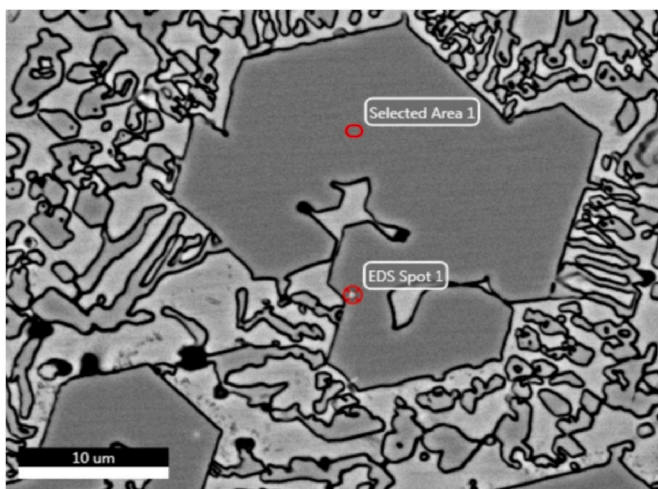


Fig. 2. FESEM of the primary  $\text{M}_7\text{C}_3$  carbide with  $\text{La}_2\text{O}_3$ .

Table 1

Proportion of elements contained in EDS Spot 1.

| Element           | Fe    | Cr    | C     | La   |
|-------------------|-------|-------|-------|------|
| Proportion (at.%) | 20.98 | 24.08 | 32.98 | 4.70 |

Table 2

Proportion of elements contained in Selected Area 1.

| Element           | Fe    | Cr    | C     |
|-------------------|-------|-------|-------|
| Proportion (at.%) | 29.05 | 43.16 | 27.79 |

contrast and the region B growing around the region A.

In order to distinguish the element composition of each region, a face scan was performed on Fig. 3, which is shown in Fig. 4.

Fig. 4(a)–(d) are the distributions of the elements C, Cr, Fe and La, respectively. It can be clearly seen that region A and region B are dependent on each other. The elements C, Cr and Fe mainly gather in the region B, while the element La obviously gather in the region A.

In order to determine the species and crystal structure of the region A and region B, the diffraction spots were collected and calibrated, as shown in Fig. 5. Fig. 5(a) is the diffraction pattern of region A, the crystal plane spacing of (010), (100) and (110) are equal to 3.42 Å, which is generated by the diffraction of the [001] zone axis. The PDF card

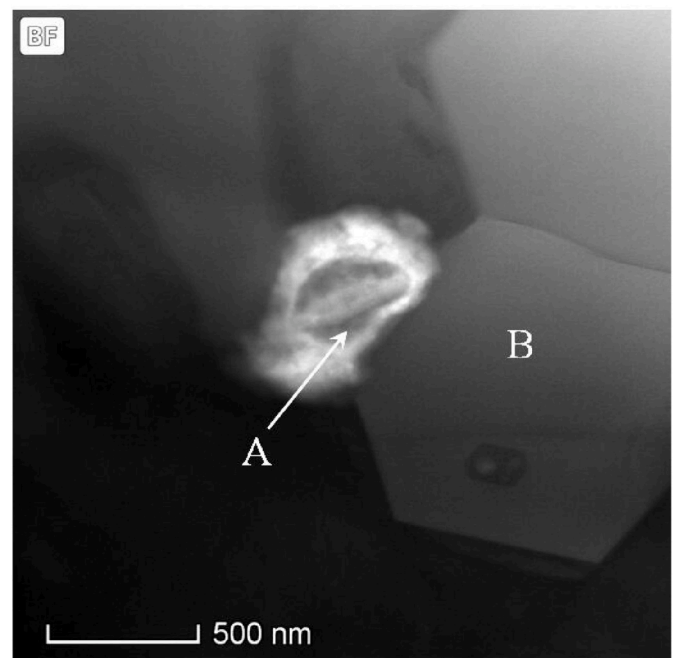


Fig. 3. TEM bright field image of the coating with  $\text{La}_2\text{O}_3$ .

information was found in Jade 6, and compared with the diffraction pattern in Fig. 5(a). It is determined to be  $\text{La}_2\text{O}_3$  and the space group is P-3m1 (164). Fig. 5(b) is the diffraction pattern of region B, the crystal plane spacing of (1 $\bar{1}$ 00), (10 $\bar{1}$ 0) and (01 $\bar{1}$ 0) are 6.05 Å, which is generated by the diffraction of the [0001] zone axis. Since the structure of  $\text{M}_7\text{C}_3$  is obtained by Cr atoms replacing part of Fe atoms in  $\text{Fe}_7\text{C}_3$ , it is found from the PDF card of Jade 6 that the crystal plane spacing of  $\text{Fe}_7\text{C}_3$  and  $\text{Cr}_7\text{C}_3$  is 5.96 Å and 6.07 Å respectively, which is similar to the results in Fig. 5(b). Therefore, it is determined to be  $\text{M}_7\text{C}_3$  and its space group is P63mc (186).

#### 4. Lattice mismatch degree between $\text{La}_2\text{O}_3$ and $\text{M}_7\text{C}_3$

According to Bramfitt two-dimensional lattice mismatch theory [24], the lattice mismatch degree between  $\text{M}_7\text{C}_3$  and  $\text{La}_2\text{O}_3$  must meet the following requirements:  $\text{La}_2\text{O}_3$  cannot be used as the heterogeneous nucleation nucleus when the mismatch degree is larger than 12%, while when the mismatch degree is between 6% and 12%, it belongs to the range of medium effective nucleation, and when the mismatch degree is



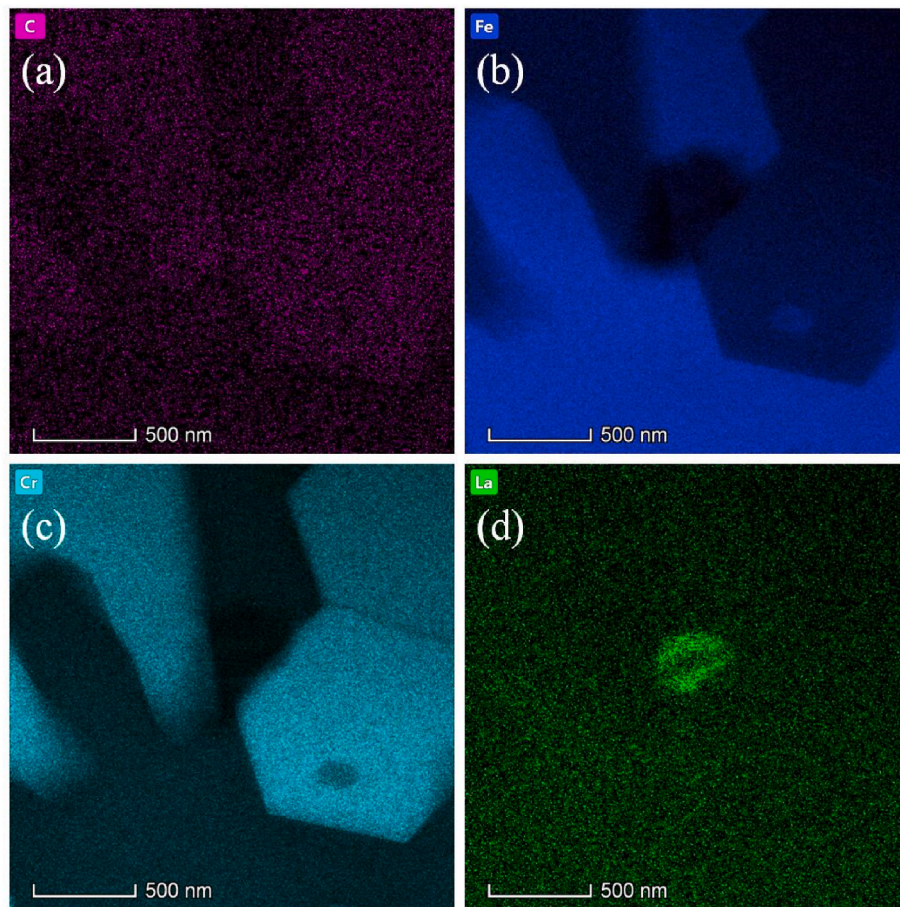


Fig. 4. Element mapping images of the  $M_7C_3$  carbide with  $La_2O_3$ . (a) C; (b) Fe; (c) Cr; (d) La.

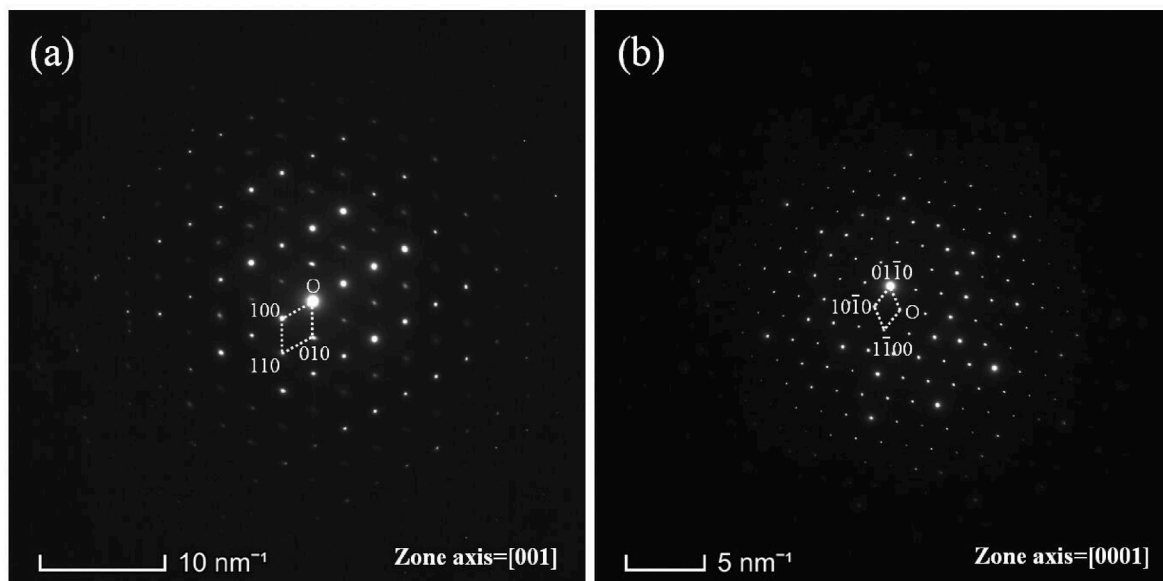


Fig. 5. Diffraction spot images of region A and region B. (a) Region A; (b) Region B.

within 6%, it belongs to the range of effective nucleation. The formula of two-dimensional lattice mismatch degree is as follows [24].

$$\delta_{(hkl)_n}^{(hkl)_s} = \sum_{i=1}^3 \left[ \frac{(|d_{[uvw]_s}^i \cos \theta - d_{[uvw]_n}^i|}{d_{[uvw]_n}^i})}{3} \right] \times 100\% \quad (1)$$

where  $(hkl)_s$  is a low-index plane of the matrix;  $[uvw]_s$  is a low-index direction on  $(hkl)_s$ ;  $d_{[uvw]_s}$  is the atomic spacing along the  $[uvw]_s$  direction;  $(hkl)_n$  is a low-index plane of the crystalline phase;  $[uvw]_n$  is a low-index direction on  $(hkl)_n$ ;  $d_{[uvw]_n}$  is the atomic spacing along the  $[uvw]_n$  direction;  $\theta$  is the angle between the  $[uvw]_s$  and  $[uvw]_n$ ;  $i$  is the

value of the three low-index directions on the three low-index planes of the crystal phase.

The lattice mismatch degrees between  $M_7C_3$  and  $La_2O_3$  are listed in Table 3. It can be seen that the lattice mismatch degree between  $M_7C_3$  (0001) plane and  $La_2O_3$  (111) plane is 2.36%, which is the most effective heterogeneous nucleation one. Therefore,  $M_7C_3$  (0001) plane and  $La_2O_3$  (111) plane are chosen to construct coherent interface models.

## 5. Nucleation interface analysis

### 5.1. Crystal structure and bulk phase properties of $La_2O_3$ and $M_7C_3$

The crystal structures of  $La_2O_3$  and  $M_7C_3$  are shown in Fig. 6. Fig. 6(a) is the crystal structure of  $La_2O_3$ , whose optimized lattice constants are  $a = b = 3.93 \text{ \AA}$  and  $c = 6.12 \text{ \AA}$ . Fig. 6(b) is that of  $M_7C_3$ , whose optimized lattice constants are  $a = b = 6.98 \text{ \AA}$  and  $c = 4.27 \text{ \AA}$ .

The calculated band structure and density of state of  $La_2O_3$  are shown in Fig. 7. Among them, Fig. 7(a) is the band structure of  $La_2O_3$ , and the red dashed line is the Fermi level. It can be clearly seen that the energy band of  $La_2O_3$  does not pass through the Fermi level, while there is a certain band gap between the valence band and the conduction band, and its band gap energy is 3.86 eV, which indicates that it embodies certain semiconductor properties. Fig. 7(b) is the density of state of  $La_2O_3$ . It can be clearly seen that the O-s orbital resonates with the La-p orbital, which indicates there is a covalent bond between them. The gravity center of orbital state density between La-d and O-p orbitals is inconsistent, which indicates that there is a strong ionic bond. It can be seen that covalent and ionic bonds are exist at the  $La_2O_3$  phase structure.

The calculated band structure and density of state of  $M_7C_3$  are shown in Fig. 8. Among them, Fig. 8(a) is the band structure of  $M_7C_3$ . It can be seen that there are energy bands passing through the Fermi level, and electrons in the valence band can easily transition to the conduction band, which indicates that  $M_7C_3$  has metallic properties. Fig. 8(b) is the density of state of  $M_7C_3$ . The presence of electrons at the Fermi level is consistent with the band structure and reflects the metallic properties of  $M_7C_3$ , which has metallic bonds within it. It can be found that the similar waveforms at  $-7.5$  to  $-4.3$  eV appear among the Fe-d, Cr-d and C-p orbitals, and they all contribute to the density of states, which indicates that there are covalent bonds between them. However, the gravity center of the orbital state density between Fe-d, Cr-d and C-p orbitals are inconsistent, which indicates that there is an ionic bond. It can be seen that metallic, covalent and ionic bonds are exist at the  $M_7C_3$  phase structure.

### 5.2. Surfaces convergence of $La_2O_3$ and $M_7C_3$

According to the lattice mismatch degrees between  $M_7C_3$  and  $La_2O_3$  in Table 3.  $M_7C_3$  (0001) plane and  $La_2O_3$  (111) plane are selected to construct coherent interface model.

The surface models of  $La_2O_3$  (111) plane and  $M_7C_3$  (0001) plane are shown in Fig. 9.  $La_2O_3$  (111) plane is a polar surface. In the surface model construction of  $La_2O_3$  (111) plane, the difference in the starting position of the cut layer will lead to the difference in the atomic type of the end surface. Therefore, the surface models of three different termination ones for  $La_2O_3$  (111) plane can be obtained, namely, O1-Terminated, La-Terminated, and O2-Terminated models, as shown in Fig. 9(a)–(c). The surface model of  $M_7C_3$  (0001) plane is shown in Fig. 9(d).

The surface energy converges gradually with the increase of atomic

**Table 3**

Calculated lattice mismatch degrees between  $M_7C_3$  and  $La_2O_3$ .

| Matching plane | $M_7C_3(0001)//La_2O_3(111)$ | $M_7C_3(0001)//La_2O_3(001)$ | $M_7C_3(0001)//La_2O_3(110)$ |
|----------------|------------------------------|------------------------------|------------------------------|
| $\delta$ (%)   | 2.36                         | 12.38                        | 17.60                        |

layers number. Botteger formula [25] was used to calculate the surface energy of  $La_2O_3$  (111) and  $M_7C_3$  (0001) planes.

The surface energy formula of  $La_2O_3$  (111) plane is as follows:

$$\sigma_{La_2O_3(111)} = \frac{1}{2A} [E_{slab} - N_{La}\mu_{La} - N_O\mu_O] \quad (2)$$

where  $\sigma_{La_2O_3(111)}$  is the surface energy of  $La_2O_3$  (111) plane;  $A$  is the surface area of  $La_2O_3$  (111) plane;  $E_{slab}$  is the total energy of  $La_2O_3$  (111) plane;  $N_{La}$  and  $N_O$  are the number of La atoms and O atoms of  $La_2O_3$  (111) plane, respectively;  $\mu_{La}$  and  $\mu_O$  are the chemical potential of La atoms and O atoms, respectively.

For  $La_2O_3$  phase structure, the formula is as follows:

$$\mu_{La_2O_3}^{bulk} = 3\mu_O + 2\mu_{La} \quad (3)$$

where  $\mu_{La_2O_3}^{bulk}$  is the energy of  $La_2O_3$  phase structure.

Combining Eqs. (2) and (3), the surface energy of  $La_2O_3$  (111) plane is obtained as follows:

$$\sigma_{La_2O_3(111)} = \frac{1}{2A} \left[ E_{slab} - \frac{1}{2} N_{La} \mu_{La}^{bulk} + \left( \frac{3}{2} N_{La} - N_O \right) \mu_O \right] \quad (4)$$

The calculated surface energies of  $La_2O_3$  (111) plane are listed in Table 4. It can be seen that the O1-Terminated model converges to 21 layers, and its surface energy is 2.029 J/m<sup>2</sup>. The La-Terminated model converges to 26 layers, and its surface energy is 5.256 J/m<sup>2</sup>. The O2-Terminated model can never converge within this range, which indicates that the surface of the terminated model is not stable within this range of layers.

The surface energy of  $M_7C_3$  (0001) plane can be expressed as follows:

$$\sigma_{M_7C_3(0001)} = \frac{1}{2A} [E_{slab} - N_{Fe}\mu_{Fe} - N_{Cr}\mu_{Cr} - N_C\mu_C] \quad (5)$$

where  $\sigma_{M_7C_3(0001)}$  is the surface energy of  $M_7C_3$  (0001) plane;  $A$  is the surface area of  $M_7C_3$  (0001) plane;  $E_{slab}$  is the total energy of  $M_7C_3$  (0001) plane;  $N_{Cr}$ ,  $N_C$  and  $N_{Fe}$  are the numbers of Cr, C and Fe atoms of  $M_7C_3$  (0001) plane, respectively;  $\mu_{Cr}$ ,  $\mu_C$  and  $\mu_{Fe}$  are the chemical potential of Cr, C and Fe atoms, respectively.

For  $M_7C_3$  phase structure, the formula is as follows:

$$\mu_{M_7C_3}^{bulk} = 3\mu_{Fe} + 4\mu_{Cr} + 3\mu_C \quad (6)$$

In the surface model of  $M_7C_3$  (0001) plane constructed by cell superposition, the formula can be expressed as follows:

$$N_{Fe} = N_C = \frac{3}{4} N_{Cr} \quad (7)$$

Combining Eqs. (5)–(7), the surface energy of  $M_7C_3$  (0001) plane is obtained as follows:

$$\sigma_{M_7C_3(0001)} = \frac{1}{2A} \left[ E_{slab} - \frac{N_{Cr}}{8} \mu_{Fe_3Cr_4C_3}^{bulk} + \left( \frac{3}{4} N_{Cr} - N_{Fe} \right) \mu_{Fe} \right] \quad (8)$$

The calculated surface energies of  $M_7C_3$  (0001) plane are listed in Table 5. It can be seen that the surface model of  $M_7C_3$  (0001) plane converges to 17 layers, and its surface energy is 3.199 J/m<sup>2</sup>.

### 5.3. Interface properties of $La_2O_3//M_7C_3$

#### 5.3.1. Interface structure

From the above calculation results, it can be seen that the surface model of  $M_7C_3$  (0001) plane converges to 17 layers, and those of La-termination and O1-termination surface models of  $La_2O_3$  (111) plane converge to 26 layers and 21 layers, respectively. Therefore, the 26 layer La-termination and 21 layer O1-termination surface models of the  $La_2O_3$  (111) planes are used to construct interface models with 17 layers model of  $M_7C_3$  (0001) plane, and they are named as La- $M_7C_3$  interface and O1- $M_7C_3$  interface, respectively, which are shown in Fig. 10. The dashed

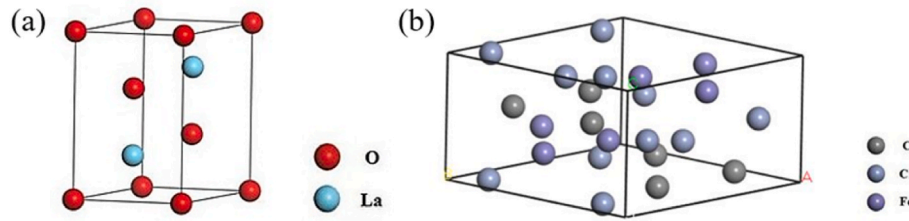


Fig. 6. Crystal structures of La<sub>2</sub>O<sub>3</sub> and M<sub>7</sub>C<sub>3</sub>. (a) La<sub>2</sub>O<sub>3</sub>; (b) M<sub>7</sub>C<sub>3</sub>.

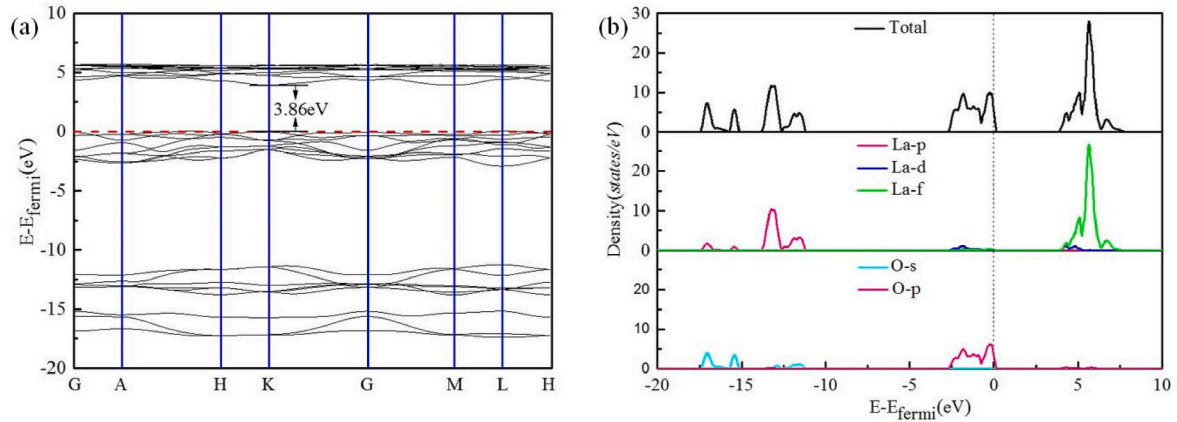


Fig. 7. Band structure and density of states of La<sub>2</sub>O<sub>3</sub>. (a) Band structure; (b) Density of states.

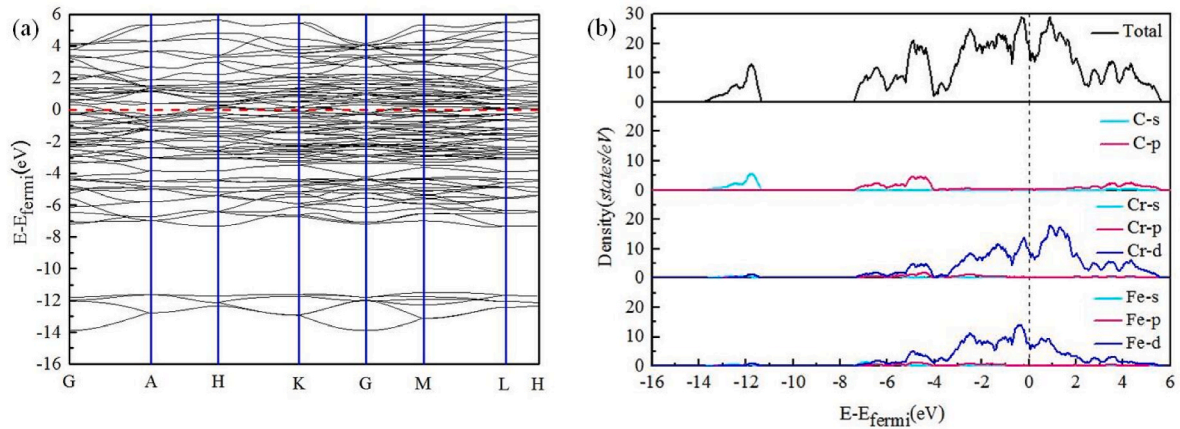


Fig. 8. Band structure and density of states of M<sub>7</sub>C<sub>3</sub>. (a) Band structure; (b) Density of states.

lines are the interface positions.

### 5.3.2. Interfacial stability

Adhesion work ( $W_{ad}$ ) of an ideal interface is the reversible work done to separate an interface into two free surfaces per unit area. The higher the interfacial bonding work is, the higher the probability of interfacial formation is, and the stronger the interatomic bonding at the interface is.

The  $W_{ad}$  of M<sub>7</sub>C<sub>3</sub>(0001)/La<sub>2</sub>O<sub>3</sub>(111) interface can be calculated by the following equation [26].

$$W_{ad} = \frac{1}{A} (E_{La_2O_3} + E_{M_7C_3} - E_{La_2O_3/M_7C_3}) \quad (9)$$

where  $W_{ad}$  is the adhesion work of interface;  $A$  is the interface area;  $E_{M_7C_3}$  and  $E_{La_2O_3}$  are the total energy of the M<sub>7</sub>C<sub>3</sub> (0001) plane and La<sub>2</sub>O<sub>3</sub> (111) plane, respectively;  $E_{La_2O_3/M_7C_3}$  is the total energy of the interface model.

The  $W_{ad}$  of La-M<sub>7</sub>C<sub>3</sub> and O1-M<sub>7</sub>C<sub>3</sub> interfaces were calculated, and the results are listed in Table 6. It can be seen that the  $W_{ad}$  (16.162 J/m<sup>2</sup>) of O1-M<sub>7</sub>C<sub>3</sub> interface is much larger than that (1.731 J/m<sup>2</sup>) of La-M<sub>7</sub>C<sub>3</sub> interface, which indicates that the O1-M<sub>7</sub>C<sub>3</sub> interface provides the strongest interface combination capability.

Interfacial energy ( $\gamma$ ) is another criterion to evaluate the stability of the interface. The smaller the interface is, the higher the probability of the interface formation is, and the more stable it is.

The  $\gamma$  of M<sub>7</sub>C<sub>3</sub>(0001)/La<sub>2</sub>O<sub>3</sub>(111) interfaces can be calculated by the following equation [27].

$$\gamma = \sigma_{La_2O_3} + \sigma_{M_7C_3} - W_{ad} \quad (10)$$

where  $\gamma$  is the interfacial energy of interface;  $\sigma_{M_7C_3}$  and  $\sigma_{La_2O_3}$  are the surface energies of M<sub>7</sub>C<sub>3</sub> (0001) plane and La<sub>2</sub>O<sub>3</sub> (111) plane, respectively.

The  $\gamma$  of La-M<sub>7</sub>C<sub>3</sub> and O1-M<sub>7</sub>C<sub>3</sub> interfaces were calculated, and the



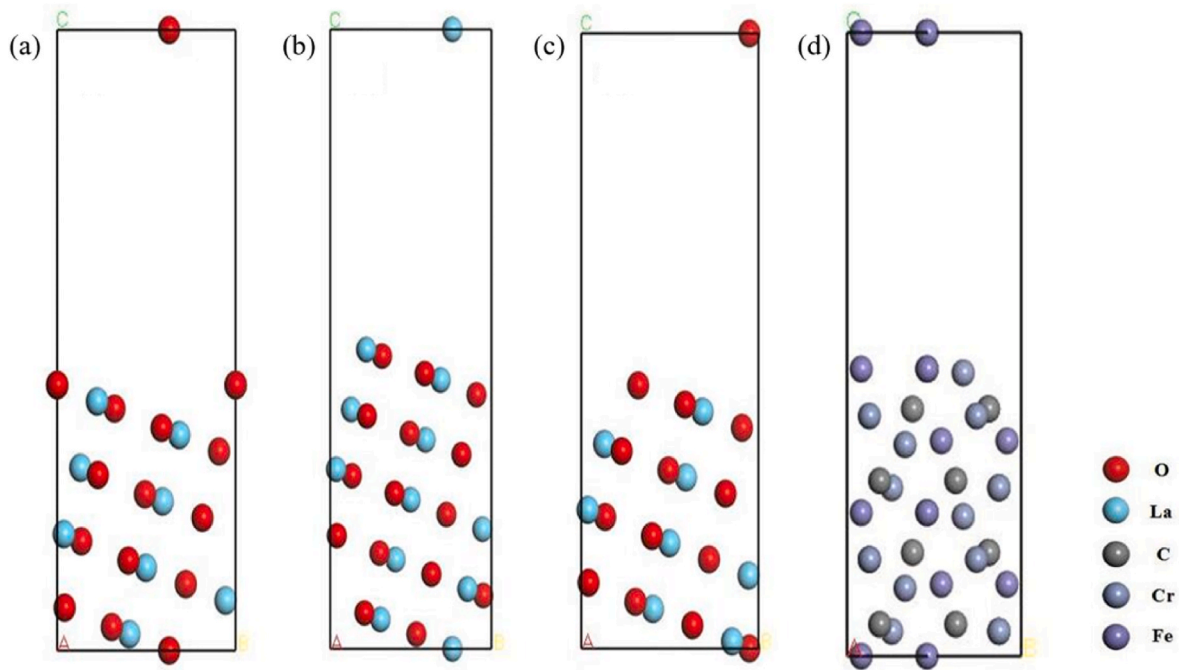


Fig. 9. Surface models of  $\text{La}_2\text{O}_3$  (111) and  $\text{M}_7\text{C}_3$  (0001) planes. (a) O1-Terminated; (b) La-Terminated; (c) O2-Terminated; (d)  $\text{M}_7\text{C}_3$ (0001).

Table 4

Calculated surface energies of  $\text{La}_2\text{O}_3$ (111) plane.

| Layers                                  | 6     | 11    | 16    | 21    | 26    | 31    |
|---|-------|-------|-------|-------|-------|-------|
| O1-Terminated ( $\text{J}/\text{m}^2$ ) | 2.017 | 1.820 | 1.861 | 2.029 | 2.053 | 2.088 |
| La-Terminated ( $\text{J}/\text{m}^2$ ) | 4.560 | 4.816 | 5.128 | 5.068 | 5.256 | 5.273 |
| O2-Terminated ( $\text{J}/\text{m}^2$ ) | 1.661 | 1.736 | 1.771 | 1.658 | 2.330 | 2.449 |

Table 5

Calculated surface energies of  $\text{M}_7\text{C}_3$  (0001) plane.

| Layers  | 9     | 17    | 25    | 33    |
|---|-------|-------|-------|-------|
| $\text{M}_7\text{C}_3$ (0001) ( $\text{J}/\text{m}^2$ ) | 3.132 | 3.199 | 3.209 | 3.229 |

results are listed in Table 7. It can be seen that the  $\gamma$  ( $-10.910 \text{ J}/\text{m}^2$ ) of O1- $\text{M}_7\text{C}_3$  interface is much smaller than that ( $6.725 \text{ J}/\text{m}^2$ ) of La- $\text{M}_7\text{C}_3$ , which indicates that the O1- $\text{M}_7\text{C}_3$  interface provides the lowest nucleation resistance.

### 5.3.3. Interface electronic structure

Charge density and differential charge density were used to analyze the charge density at the interface and the bonding mechanism between atoms. Among them, the differential charge density is calculated as follows [27].

$$\rho_d = \rho_{tot} - \rho_{\text{La}_2\text{O}_3} - \rho_{\text{M}_7\text{C}_3} \quad (11)$$

where  $\rho_{tot}$  is the total charge density of the interface models;  $\rho_{\text{La}_2\text{O}_3}$  and  $\rho_{\text{M}_7\text{C}_3}$  are the charge density of separate  $\text{La}_2\text{O}_3$  (111) plane and  $\text{M}_7\text{C}_3$  (0001) plane in the same interface models.

The charge densities of  $\text{M}_7\text{C}_3$ (0001)/ $\text{La}_2\text{O}_3$ (111) interface are shown in Fig. 11, and the dotted lines represent the interface position. As shown on the right side of the scale, the charge density gradually rises from blue to red, and the positions of each atom are marked by different colored spheres. Fig. 11(a) is the charge density front view of the La- $\text{M}_7\text{C}_3$  interface. It can be seen that the charge of the Fe atom at the top of the interface is transferred to the O atom at the bottom of the interface,

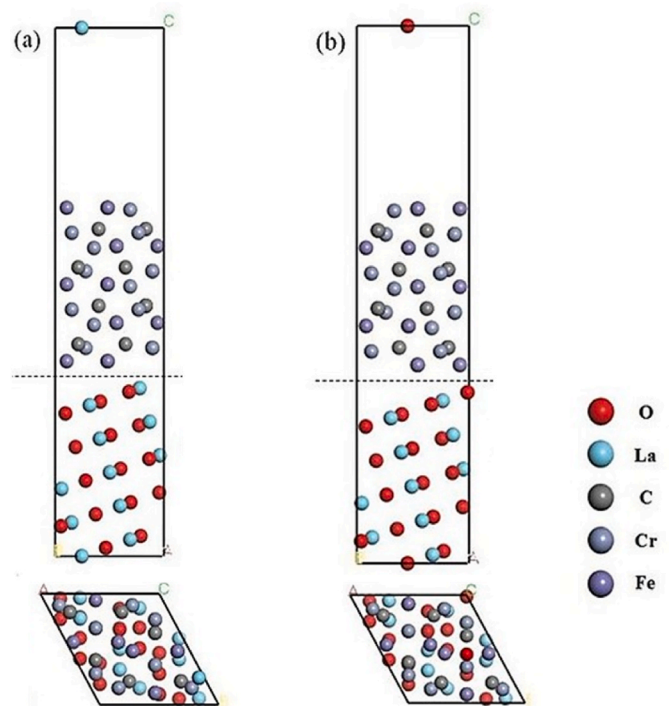


Fig. 10. Interface models of  $\text{La}_2\text{O}_3$ (111)/ $\text{M}_7\text{C}_3$ (0001) interfaces. (a) La- $\text{M}_7\text{C}_3$ ; (b) O1- $\text{M}_7\text{C}_3$ .

Table 6

Adhesion work of  $\text{M}_7\text{C}_3$ (0001)/ $\text{La}_2\text{O}_3$ (111) interface.

|  | $E_{\text{La}_2\text{O}_3}$ | $E_{\text{M}_7\text{C}_3}$ | $E_{\text{La}_2\text{O}_3/\text{M}_7\text{C}_3}$ | $W_{ad}$ |
|--|-----------------------------|----------------------------|--|----------|
| O1- $\text{M}_7\text{C}_3$ ( $\text{J}/\text{m}^2$ ) | -10.46                      | -23.16                     | -36.71   | 16.162   |
| La- $\text{M}_7\text{C}_3$ ( $\text{J}/\text{m}^2$ ) | -13.11                      | -23.16                     | -36.55   | 1.731    |

**Table 7**Interfacial energy of  $M_7C_3(0001)//La_2O_3(111)$  interface.

|                                  | $\sigma_{La_2O_3}$ | $\sigma_{M_7C_3}$ | $\gamma$ |
|----------------------------------|--------------------|-------------------|----------|
| O1- $M_7C_3$ (J/m <sup>2</sup> ) | 2.053              | 3.199             | -10.910  |
| La- $M_7C_3$ (J/m <sup>2</sup> ) | 5.256              | 3.199             | 6.725    |

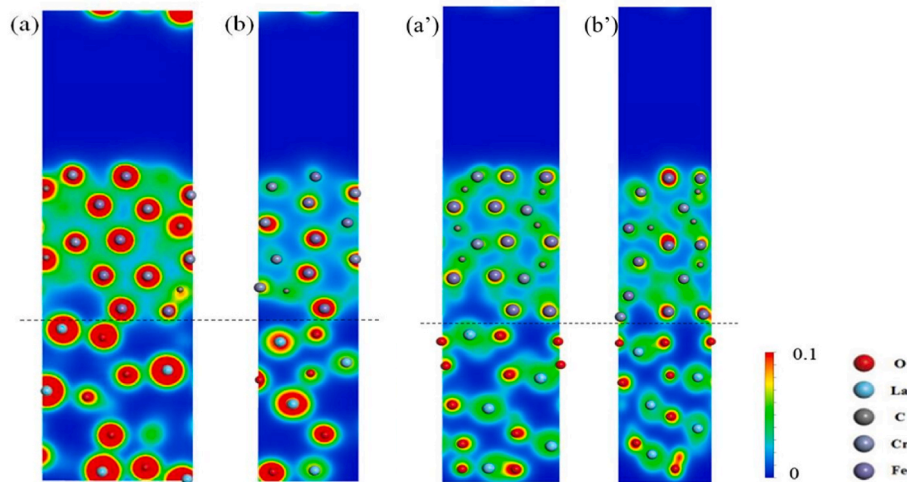
which indicates that there is a strong bond between the Fe atom and the O atom. Fig. 11(b) is the charge density side view of La- $M_7C_3$  interface. It can be seen that the charge of the C atom in the second layer above the interface also shifts significantly to the direction of O atom, which means that there is also a strong chemical bond between the C atom and the O atom. The charge of Cr atom in the fourth layer above the interface tends to shift to the lower left, which indicates that it is also affected by bonding. Therefore, it can be clearly observed that there are bonds near the interface to Fe–O, C–O, and Cr–O atoms.

Fig. 11(a') is the charge density front view of the O1- $M_7C_3$  interface. It can be seen that the charge of the Fe atom in the upper center of the interface is obviously transferred to the O atom below, and the Fe atom in the third layer above is also affected by the O atom below the interface directly below it, which indicates that the bonding between Fe atom and O atom is very strong. Fig. 11(b') is the charge density side view of O1- $M_7C_3$  interface. It can be seen that the charge of the Cr atom on the left of

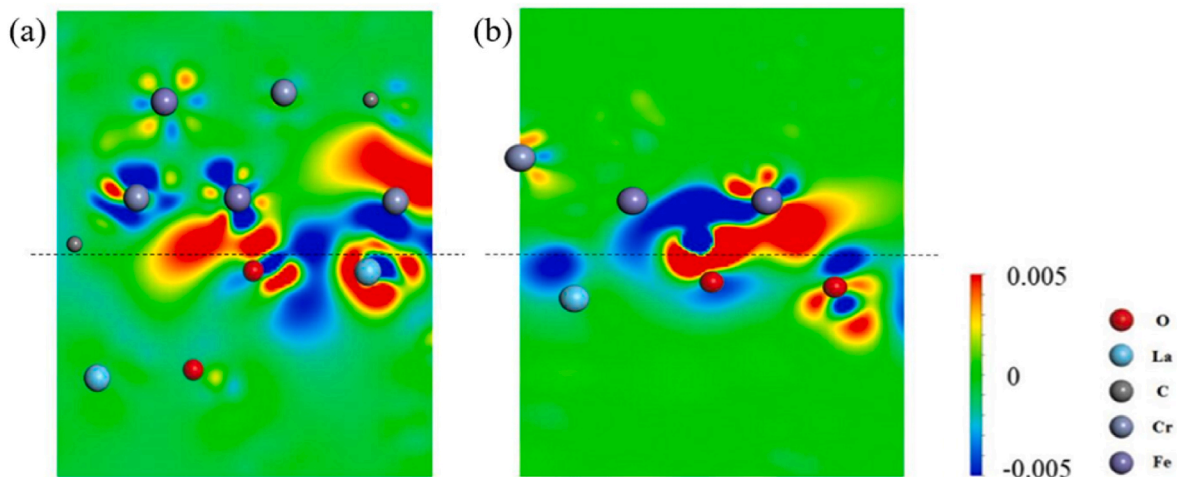
the upper part of the interface is transferred to the O atom below, the charge of the Fe atom on the right is also transferred to the O atom below it, and the charge of the Cr atom above the Fe atom on the right is also transferred downward. Therefore, it can observe a large number of Fe–O and Cr–O bonds at the O1- $M_7C_3$  interface.

It can be seen that the charge transfer phenomenon near the interface is very obvious of two different terminating interfaces, which indicates that there are many strong bonds near the interface. Therefore, the interface bonding property of O1- $M_7C_3$  interface is large.

The differential charge densities of  $M_7C_3(0001)//La_2O_3(111)$  interface are shown in Fig. 12, and the dotted lines represent the interface position, in which, the blue represents areas where charge is missing, red represents areas where charge is concentrated, and the positions of each atom are marked by different colored spheres. Fig. 12(a) is the differential charge density of La- $M_7C_3$  interface. It can be found that there are a large number of charge accumulation regions between the C atom on the left side of the interface and the O atom on the middle side of the interface, and there are obvious electron missing on the other sides of the O atom and C atoms, which indicates that a polar covalent bond is formed between C atom and O atom. However, in the upper left of this large charge accumulation region, there is Cr atom with a large loss of surrounding charges, which indicates that Cr atom and O atom formed an ionic bond. The Fe atom above the O atom in the middle of the



**Fig. 11.** Charge density of  $La_2O_3(111)//M_7C_3(0001)$  interface. La- $M_7C_3$  interface of (a) the front view; (b) the side view; O1- $M_7C_3$  interface of (a') the front view; (b') the side view.



**Fig. 12.** Differential charge density of  $La_2O_3(111)//M_7C_3(0001)$  interface. (a) La- $M_7C_3$ ; (b) O1- $M_7C_3$ .

interface is observed, and it is found that there is also ionic bond between Fe atom and O atom. There is a charge missing region on the upper right side of Cr atom near the interface side, and the charge accumulation between the Cr atom and the C atom on the deviating interface side, which indicates that there are covalent and ionic bonds between Cr atom and C atom.

Fig. 12(b) is the differential charge density of O1-M<sub>7</sub>C<sub>3</sub> interface. It shows that there is a charge accumulation area in the middle region of the interface, while there is a charge missing area around the two Fe atoms at the top, and the charge of the Fe atom at the top left is transferred to the O atom at the lower side of the interface, which indicates that it forms an ionic bond between Fe atom and O atom. The Fe atom on the right has both charge missing and charge accumulation regions around it, which indicates that it has polar covalent and ionic bonds with the two O atoms below.

## 6. Conclusion

- (1) The hypereutectic Fe–27Cr–4C alloy coating with and without La<sub>2</sub>O<sub>3</sub> was prepared. La<sub>2</sub>O<sub>3</sub> can refine the primary M<sub>7</sub>C<sub>3</sub> carbide in the coating, which indicates that La<sub>2</sub>O<sub>3</sub> can be as the heterogeneous nucleation nucleus of the primary M<sub>7</sub>C<sub>3</sub> carbide.
- (2) The lattice mismatch degree between La<sub>2</sub>O<sub>3</sub> (111) plane and M<sub>7</sub>C<sub>3</sub> (0001) plane is 2.36%, which indicates that La<sub>2</sub>O<sub>3</sub> is the most effective nucleation nucleus of primary M<sub>7</sub>C<sub>3</sub> carbide.
- (3) The La-terminating and O1-terminating surface models of La<sub>2</sub>O<sub>3</sub> (111) plane converge to 26 layers and 21 layers respectively, whose surface energies are 5.256 J/m<sup>2</sup> and 2.029 J/m<sup>2</sup>. The surface model of M<sub>7</sub>C<sub>3</sub> (0001) plane converges to 17 layers, whose surface energy is 3.199 J/m<sup>2</sup>.
- (4) Among La-M<sub>7</sub>C<sub>3</sub> and O1-M<sub>7</sub>C<sub>3</sub> interfaces, the adhesion work (16.162 J/m<sup>2</sup>) of O1-M<sub>7</sub>C<sub>3</sub> interface is larger than that (1.731 J/m<sup>2</sup>) of La-M<sub>7</sub>C<sub>3</sub>. Meanwhile, the interface energy (–10.910 J/m<sup>2</sup>) of O1-M<sub>7</sub>C<sub>3</sub> interface is smaller than that (6.725 J/m<sup>2</sup>) of La-M<sub>7</sub>C<sub>3</sub> interface, which indicates that the O1-M<sub>7</sub>C<sub>3</sub> interface has the best interface bonding property and the lowest interface nucleation resistance.

## Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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