

# The ALMA-CRISTAL Survey

## Spatial extent of [C II] line emission in star-forming galaxies at $z = 4-6$

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Received 6 August 2024 / Accepted 11 December 2024

### ABSTRACT

We investigate the spatial extent and structure of the [C II] line emission in a sample of 34 galaxies at  $z = 4 - 6$  from the [C II] Resolved ISM in STar-forming galaxies with ALMA (CRISTAL) Survey. By modeling the distribution of the [C II] line emission in the interferometric visibility data directly, we derive the effective radius of [C II] line emission assuming an exponential profile. These measurements comprise not only isolated galaxies but also interacting systems that were identified thanks to the high spatial resolution of the data. The [C II] line radius ranges from 0.5 to 3.5 kpc with an average value of  $\langle R_{e,[CII]} \rangle = 1.90$  kpc. We compare the [C II] sizes with the sizes of rest-frame ultraviolet (UV) and far-infrared (FIR) continua, which were measured from the HST F160W images and ALMA Band-7 continuum images, respectively. We confirm that the [C II] line emission is more spatially extended than the continuum emission, with average size ratios of  $\langle R_{e,[CII]}/R_{e,UV} \rangle = 2.90$  and  $\langle R_{e,[CII]}/R_{e,FIR} \rangle = 1.54$ , although about half of the FIR-detected sample shows a comparable spatial extent between the [C II] line and the FIR continuum emission ( $R_{e,[CII]} \approx R_{e,FIR}$ ). The residual visibility data of the best-fit model do not show statistical evidence of flux excess, indicating that the [C II] line emission in star-forming galaxies can be characterized by an extended exponential disk profile. Overall, our results suggest that the spatial extent of [C II] line emission can primarily be explained by photodissociation regions associated with star formation activity, while the contribution from diffuse neutral medium (atomic gas) and the effects of past merger events may further expand the [C II] line distributions, causing their variations among our sample. Finally, we report the negative correlation between the [C II] surface density ( $\Sigma_{[CII]}$ ) and the Ly $\alpha$  equivalent width ( $EW_{Ly\alpha}$ ), and a possible negative correlation between  $R_{e,[CII]}/R_{e,UV}$  and  $EW_{Ly\alpha}$ , which may be in line with the scenario that atomic gas component largely contributes to the extended [C II] line emission. Future three-dimensional analysis of Ly $\alpha$  and H $\alpha$  lines will shed light on the association of the extended [C II] line emission with atomic gas and outflows.

**Key words.** galaxies: evolution – galaxies: formation – galaxies: high-redshift – galaxies: ISM

### 1. Introduction

Understanding the interplay between gas, dust, and stars in galaxies in the early Universe is one of the biggest topics in modern extragalactic astronomy. In particular, the cold interstellar medium (ISM), which can be interpreted as a direct fuel for forming stars, is essential as it becomes the dominant contributor to the baryonic mass toward high redshift (Tacconi et al. 2020). In this context, far-infrared (FIR) fine-structure lines have been known as an effective probe for star formation and the ISM of galaxies.

The [C II]  $^2P_{3/2} - ^2P_{1/2}$  fine-structure line emission ( $\nu_{\text{rest}} = 1900.537$  GHz, hereafter [C II] line), emitted from ionized carbon (C<sup>+</sup>), is one of the main coolants of the ISM among the FIR emission lines and has been the most popular tracer with which to study the cool gas component in high-redshift galaxies ( $z \gtrsim 4$ ; Carilli & Walter 2013), as its redshifted millimeter wavelength is accessible through the atmospheric windows. Ionized carbon is excited by photoelectric heating of gas, whereby electrons are emitted from small dust grains or polycyclic aromatic

hydrocarbons (PAHs) that absorb far-ultraviolet (FUV) photons from star-forming regions. Therefore, it has been suggested that [C II] line emission can be used as a good tracer of photodissociation regions (PDRs; Hollenbach & Tielens 1999; Wolfire et al. 2022), as well as a star formation rate (SFR) indicator from nearby star-forming galaxies (SFGs; e.g., Stacey et al. 1991; Pineda et al. 2014; Kapala et al. 2015; De Looze et al. 2014; Herrera-Camus et al. 2015; Lapham et al. 2017; Bigiel et al. 2020; but see Díaz-Santos et al. 2013 for starburst galaxies) to high-redshift galaxies (e.g., Vallini et al. 2015; Carniani et al. 2018; Schaerer et al. 2020; Liang et al. 2024). At the same time, [C II] line emission is also used as a tracer of molecular gas (e.g., Madden et al. 1997; Langer et al. 2014; Zanella et al. 2018; Dessauges-Zavadsky et al. 2020; Madden et al. 2020; Vizgan et al. 2022a; Aravena et al. 2024) and atomic gas (e.g., Heintz et al. 2021, 2022; Vizgan et al. 2022b), which may be compatible with the SFR tracer if the Kennicutt-Schmidt relation (Kennicutt 1998) holds. However, it has been known that the [C II] line emission can originate from multiple phases of ISM beyond PDRs, such as ionized gas, making the interpretation of [C II] line emission less straightforward. With these potential capabilities, a large number of recent studies focusing on ISM

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conditions in high-redshift galaxies ( $z \gtrsim 4$ ) rely on observations of [C II] line emission, thanks to the capability of the Atacama Large Millimeter/submillimeter Array (ALMA) and the Northern Extended Millimeter Array (NOEMA) interferometer.

If the majority of [C II] line emission indeed originates from PDRs, one would expect its spatial extent in galaxies to also trace the region where active star formation takes place, which is bright in rest-frame ultraviolet (UV) continuum emission from young stellar populations. In contrast to this expectation, one remarkable feature of the [C II] line emission in high-redshift galaxies is that they are more spatially extended than what is observable through optical/near-infrared wavelengths.

Several studies have reported comparisons of spatial extent between [C II] line emission and the rest-frame UV continuum observed by the Hubble Space Telescope (HST) for galaxies at  $z > 4$ , both for individual galaxies (e.g., Carniani et al. 2018; Fujimoto et al. 2020) and for stacked images (e.g., Fudamoto et al. 2022), providing the general picture that at high redshift the [C II] sizes are larger than the UV sizes by a factor of more than two. Furthermore, Fujimoto et al. (2019) report the detection of a 10 kpc scale “[C II] halo” with a beam-convolved radius of 10 kpc ( $R_{e,[CII]} = 5.6 \pm 0.1$  kpc), which can be characterized by a two-component structure in the radial profile, by stacking 18 SFGs at  $z = 5 - 7$ . With the detection of 75 [C II] line emission from the ALPINE Survey (Le Fèvre et al. 2020; Béthermin et al. 2020; Faisst et al. 2020), Ginolfi et al. (2020b) found evidence of the “[C II] halo” through the stacking analysis and the broad spectral feature for a subsample of galaxies with higher SFRs, indicative of ongoing star-formation-driven outflows. Although a visual classification based on morphology and kinematics was conducted (Le Fèvre et al. 2020), the studies referred to above cannot rule out the possibility that [C II] line emission from close pairs or mergers is blended due to low spatial resolution ( $\sim 1''$ ).

A handful of studies have also compared [C II] line emission with the underlying FIR continuum emitted from dust grains heated by star formation or active galactic nuclei (AGNs; e.g., Gullberg et al. 2018; Venemans et al. 2020; Díaz-Santos et al. 2021; Izumi et al. 2021a,b; Umehata et al. 2021; Pozzi et al. 2024; Bischetti et al. 2024; Wang et al. 2024), although these sources tend to be biased toward submillimeter galaxies or quasars due to their brightness in the FIR continuum. These studies show that the [C II] line emission is comparable to or more extended than the FIR continuum emission, but the differences are not as significant as those for the rest-frame UV emission. Through the stacking analysis of 27 quasars at  $z \gtrsim 6$ , Novak et al. (2020) found a comparable spatial extent between [C II] line and FIR continuum emission extending up to  $\sim 10$  kpc with no sign of broad line wings in stacked [C II] line spectra.

Extended [C II] line emission beyond the rest-frame UV and/or FIR continua directly implies the presence of metal-enriched gas up to a circumgalactic medium (CGM) scale even in the early Universe, and has been a matter of debate in recent years, given that cosmological zoom-in simulations could not reproduce such extended [C II] line emission (Fujimoto et al. 2019; Arata et al. 2020). Multiple scenarios have been proposed, such as satellite galaxies, extended star formation activity, cold streams, and outflows. Recent semi-analytical models support that the two-component halo structure in [C II] line emission can be explained by cold outflows (Pizzati et al. 2020, 2023), but none of the above scenarios are observationally conclusive yet. There are two reasons why it is difficult to elucidate the origin of such extended [C II] line emission. First, [C II] line emission can originate from multiple gas phases (ionized or neutral, atomic

or molecular, PDR or H II regions, and shocked gas); thus, integrated [C II] line emission is likely to trace a mixture of them. Second, previous [C II] line observations were mostly performed with a spatial resolution of  $\sim 1''$  ( $\sim 6$  kpc in a physical scale at  $z = 5$ ), hampering the measurements of accurate sizes and the study of morphology below this scale.

Therefore, to narrow down the origin of [C II] line emission at high redshift, it is necessary to study galaxies at high resolution and compare them with other tracers. In fact, several studies have attempted to follow up the [C II] line at high resolution with improved sensitivity, and have demonstrated that ALMA is capable of characterizing the [C II] line in typical SFGs at  $z = 4 - 7$  down to a kiloparsec scale (Herrera-Camus et al. 2021; Akins et al. 2022; Lambert et al. 2023; Posses et al. 2023). Spatially resolved studies of [C II] line emission have recently been reported for two systems (Solimano et al. 2024; Posses et al. 2024) as a part of the [C II] Resolved ISM in STar-forming galaxies with ALma (CRISTAL) Survey (Herrera-Camus et al. in prep.)<sup>1</sup>. Solimano et al. (2024) discovered an elongated [C II] line feature associated with the J1000+0234 system, composed of a dusty star-forming galaxy and a Lyman-break galaxy (CRISTAL-01a), while several scenarios (e.g., a conical outflow, a cold accretion stream) are possible for its origin. Posses et al. (2024) analyzed CRISTAL-05, which was previously claimed as a “[C II] halo” (Fujimoto et al. 2020), and found a complex kinematical structure, implying that CRISTAL-05 is likely to be a merging system. Both studies exemplify the diverse characteristics of [C II] line emission after the Epoch of Reionization and the necessity of high-resolution ALMA observations to understand their intrinsic morphology and structure. Nonetheless, each study stated above remains a case study, and it is difficult to draw general conclusions even by compiling these samples. A systemic census of deep and high-resolution [C II] line observations with a larger and homogeneous sample is needed to provide a more general picture.

In this paper, we report on the size measurement and search for an extended halo component of the [C II] line emission in SFGs at  $z = 4 - 6$ . To analyze pure signals obtained from the interferometer without any processes of Fourier transform – that is, synthesis imaging – we focus on the analysis of interferometric visibility data throughout this paper. We first describe the CRISTAL Survey, the galaxy sample, and the archival data that we used in this study in Section 2. Section 3 presents the analysis of visibility modeling, including the classification based on multiplicity in either [C II] line or rest-frame UV emission. We report the main results and discussions on the extended [C II] line emission and correlation with other galaxy properties in Section 4 and summarize this study in Section 5.

Throughout this paper, we assume a standard  $\Lambda$ CDM cosmology with  $H_0 = 70$  km s<sup>-1</sup> Mpc<sup>-1</sup>,  $\Omega_M = 0.3$ , and  $\Omega_\Lambda = 0.7$ . We refer to the term “[C II] halo” as a secondary structure which is more extended than the primary [C II] line emission in the central regions. We use the notation of  $R_{e,X}$  as a *circularized* effective radius of a tracer X, a product of the major-axis effective radius and a square root of the minor-to-major axis ratio (denoted as  $q$ ), unless otherwise noted.

## 2. Data

### 2.1. The CRISTAL Survey

In this study, we use the data taken from the CRISTAL Survey, an ALMA Cycle 8 Large Program (Project ID:

<sup>1</sup> <https://sites.google.com/view/alma-cristal>

#2021.1.00280.L, PI: R. Herrera-Camus). The observations were carried out during ALMA Cycle 8 and 9, and were completed in April 2023. The primary aim of the survey is to spatially resolve both [C II] line and FIR continuum emission on  $\sim 1$  kpc scales with ALMA Band 7 observations for 19 star-forming main sequence galaxies at  $z = 4 - 6$ . The targets were drawn from the ALPINE Survey (Le Fèvre et al. 2020). Targets were mass-selected with the selection of  $\log(M_*/M_\odot) \geq 9.5$  and were also required to have observations in the HST/Wide Field Camera 3 (WFC3) F160W filter. These HST images were primarily obtained through observations of the CANDELS Survey (Grogin et al. 2011) as well as the COSMOS-DASH Survey (Momcheva et al. 2017; see more details in Faisst et al. 2020 and Herrera-Camus et al. in prep). Here, we summarize aspects of the ALMA observations that are relevant to the analysis of this study.

The combination of multi-configuration observations is essential to achieve both sufficiently large maximum recoverable scale (MRS) and high spatial resolution. Therefore, each target was observed using multiple configurations of the ALMA 12 m array, one with compact (C43-1/2/3) and another with extended (C43-4/5/6) array configuration. The former covers low spatial frequencies ( $uv$  distance  $\lesssim 150 - 300$  k $\lambda$ )<sup>2</sup> in the visibility plane that are sensitive to large-scale structure ( $\theta_{\text{beam}} = 0''.29 - 1''.00$ ,  $\theta_{\text{MRS}} = 5''.28 - 9''.79$ ), while the latter covers high spatial frequencies ( $uv$  distance  $\gtrsim 350 - 1500$  k $\lambda$ , depending on the target) that are sensitive to small-scale structure ( $\theta_{\text{beam}} = 0''.07 - 0''.35$ ,  $\theta_{\text{MRS}} = 1''.15 - 5''.15$ ).

We used the ALMA correlators of the 1.875 GHz width spectral windows (SPWs) with the frequency division mode (FDM). The observing [C II] frequency for each object was adjusted in the middle of two adjacent SPWs in the upper sideband unless the [C II] line emission was not detected in the ALPINE Survey (Béthermin et al. 2020).

## 2.2. ALMA archive

### 2.2.1. The ALPINE Survey

To search for faint extended emission, deep integration in the more compact array configuration, covering short spatial frequencies, is particularly important. Therefore, we combined the data from the ALPINE Survey (#2017.1.00428.L) with the CRISTAL data to achieve better sensitivity to the extended structure.

Contrary to the CRISTAL Survey, the ALPINE Survey adopts the Time Division Mode for the SPW setup, in which the edges of 2 GHz bandwidth are severely affected by low power. We find that in three sources the [C II] lines spread across the two adjacent SPWs with insufficient overlapping frequencies (CRISTAL-06, CRISTAL-08, and CRISTAL-23c), and therefore for these fields we decided not to combine the ALPINE data in our analysis. Also, we did not include the ALPINE data of CRISTAL-07c, a serendipitously detected galaxy at  $z = 5.16$ , as it is located at the edge of the Band-7 field of view (FoV) with the primary beam gain level of  $\sim 0.3$ , while in the CRISTAL Survey, the FoV is adjusted to have comparable sensitivity in both CRISTAL-07a/07b and CRISTAL-07c.

### 2.2.2. The CRISTAL+ Sample

In addition to the main targets of the CRISTAL survey, there exist several programs that used ALMA to observe [C II] line emission with similar resolutions and sensitivities. This includes six galaxies: HZ4, HZ7, HZ10, DEIMOS\_COSMOS\_818760, DEIMOS\_COSMOS\_873756, and vuds\_cosmos\_8326. We have included these archival data as the supplementary sample of the CRISTAL Survey and hereafter refer to these six targets as CRISTAL-20 to CRISTAL-25 (Herrera-Camus et al. in prep.). The [C II] line emission of the first three was initially reported by Capak et al. (2015) and followed up by individual projects for high-resolution data (#2018.1.01605.S; Herrera-Camus et al. 2021, #2018.1.01359.S; Lambert et al. 2023, #2019.1.01075.S; Villanueva et al. 2024 and Telikova et al. 2024). CRISTAL-20 was also observed in the ALPINE Survey as DEIMOS\_COSMOS\_494057. The latter three are the three brightest objects in [C II] line emission among the sample of the ALPINE Survey (Béthermin et al. 2020) and followed up at higher resolution under the ALMA Cycle 7 program (#2019.1.00226.S; Devereaux et al. 2024). We combine the data taken by the ALPINE Survey with these follow-up observations, similar to the CRISTAL main targets.

In summary, the data set of this study comprises 24 ALMA Band-7 fields, containing 35 main-sequence SFGs and two dusty star-forming galaxies (DSFGs) detected in [C II] line at  $z = 4 - 6$ . We excluded CRISTAL-18 from the analysis because we do not detect [C II] line emission from this source. We present the list of our sample cross-matched to the other names presented in previous studies in Table A.1.

## 3. Analysis

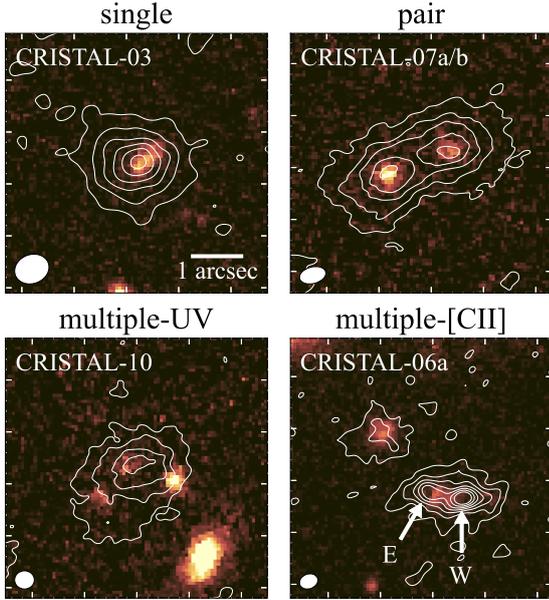
### 3.1. Classification based on multiplicity

By virtue of a kiloparsec-scale resolution in [C II] line emission and ancillary multi-wavelength data of our sample, we can compare the spatial extent between [C II] line and UV continuum emission including complex systems such as interacting galaxies. One possible origin of extended [C II] line emission is the presence of tidal features or gas removal caused by mergers (Solimano et al. 2024; Posses et al. 2024). Therefore, we first classified the sample based on whether each galaxy is likely to be physically associated with other galaxies. Mitsuhashi et al. (2024) classified the CRISTAL sample into single and multiple sources solely based on the multiplicity in HST/WFC3 F160W images. In this study, we take a step forward to add information from the [C II] line distribution to visually classify the CRISTAL sample into four categories:

- single – an isolated galaxy with a single component of the [C II] line emission. We classify 17 sources ( $\sim 50\%$ ) of the CRISTAL sample as single.
- pair – a pair of [C II] line detections with a projected angular separation of less than  $\sim 3$  arcsec. The velocity offset among the pair is confirmed to be small ( $< 300$  km/s) so that there is an overlap of [C II] line frequencies. We classify nine sources ( $\sim 30\%$ ) as pair.
- multiple-UV – a system comprising of multiple compact blobs in the UV continuum with overlapping extended [C II]

<sup>2</sup> However, we note that a synthesized dirty beam created using multiple array configurations frequently deviates from a single Gaussian profile and exhibits an elongated feature toward larger scales. Thus, we caution the reader that most of the dirty images presented in this paper are convolved with a point spread function (PSF) elongated than a single Gaussian.

<sup>2</sup> We use a term of ‘ $uv$  distance’ as a radial distance of visibility data in the  $(u, v)$  plane in units of k $\lambda$ , defined as  $uv$  distance =  $\sqrt{u^2 + v^2}$ .



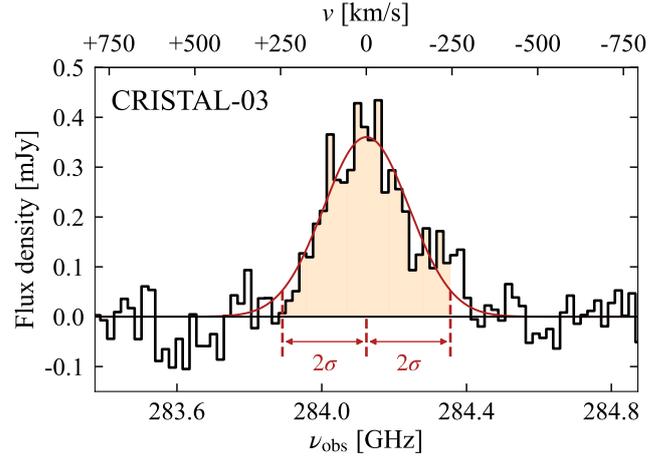
**Fig. 1.** Classification of the galaxies based on a multiplicity of [C II] line (with contours) and rest-frame UV (background, HST/WFC3 F160W) emission. A  $5'' \times 5''$  region is shown in each panel. The contours start at  $2\sigma$  and increase in steps of  $3\sigma$  until  $20\sigma$ . The Gaussian FWHM fit from the synthesized dirty beam is shown as a white ellipse in the lower-left corner of each panel<sup>3</sup>. Two arrows shown in a panel of multiple-[C II] (CRISTAL-06a) correspond to two [C II] line components (denoted as ‘W’ and ‘E’) that are visually identified.

line emission. Such systems are likely to be complex merging systems instead of unevenly dust-obscured systems, since their FIR continuum emission is either faint ( $S/N < 5$ ) or entirely overlapping the UV blobs (Mitsuhashi et al. 2024). The difference from the pair systems is that the [C II] line emission cannot be resolved into each UV counterpart with the existing data. We classified five sources (CRISTAL-01a, CRISTAL-01b, CRISTAL-02, CRISTAL-10, and CRISTAL-13) into this category.

- (d) multiple-[C II] – a system in which multiple peaks in [C II] line emission can be found around a single UV component. Only CRISTAL-06a exhibits this feature.

Figure 1 summarizes our classification, showcasing examples of the [C II] line and rest-frame UV distributions for each class. We note, however, that this is still a crude classification, as we do not consider the dynamical state of each galaxy obtained from kinematical analysis. For example, we classify CRISTAL-05 as single from its appearance. A detailed kinematical analysis of the [C II] line revealed that it is actually a complex galaxy pair projected along the line of sight (Posses et al. 2024).

We also find that three galaxies (CRISTAL-11, CRISTAL-15, and CRISTAL-17) classified as single have pair-like morphology when looked with sharper images taken by James Webb Space Telescope (JWST; Lines et al. 2024). However, the resolution of the [C II] line emission is coarser than the separation of two clumps identified by JWST, and thus it would be difficult to characterize their sizes and perform the one-to-one comparison. We thus decide to rely on the classification based on rest-frame UV morphology primarily due to the data homogeneity, and we note that the discussions and conclusions we present in the following would not significantly be affected by the choice of our classification, because the sizes of the continuum emission are not constrained for two out of these three galaxies (Table B.2).



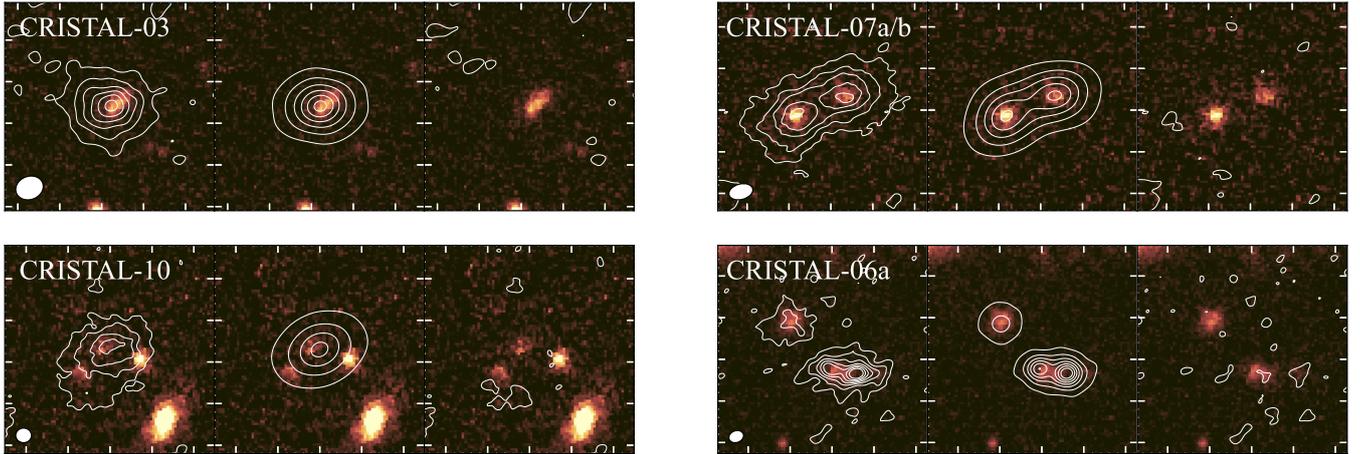
**Fig. 2.** [C II] line spectrum of CRISTAL-03 extracted from a 1-arcsec aperture. The best-fit Gaussian is shown as a solid red curve. We bin the frequency range of the filled region for the [C II] size measurements, which corresponds to  $\pm 2\sigma$  from the central frequency.

## 3.2. Size measurements

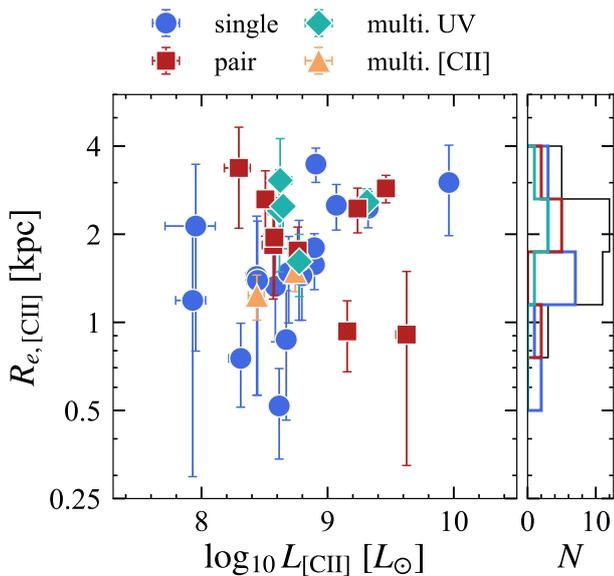
### 3.2.1. [C II] line emission

The data from the CRISTAL Survey with a kiloparsec-scale resolution allows us to robustly quantify the sizes of [C II] line emission. While the majority of the sample has a sufficient signal-to-noise ratio ( $S/N$ ) to perform size measurements in the image domain, several sources have a moderate  $S/N$  of  $5 \lesssim S/N \lesssim 10$ . In such cases, the measured sizes in the image domain could be overestimated, because either the best-fit model takes noise into account, or the smearing effect of the clean beam affects the fittings (Tadaki et al. 2020; Mitsuhashi et al. 2024). In addition, the images created through the CLEAN algorithm may overestimate the flux densities outside the CLEAN masks due to the deviation of the synthesized dirty beam from a single Gaussian. To avoid these issues, we consistently perform our [C II] size measurements by modeling interferometric visibility data. The visibility analysis is also favorable assessing faint extended features in [C II] line emission, as the imaging procedure requires several parameters to be considered (e.g., weighting of visibility data, threshold, size of the masked region for the CLEAN algorithm) and therefore complicates the optimization of the best parameter sets (Jones et al. 2023).

As a first step of the [C II] size measurements, we define the velocity range ( $\Delta\nu$ ) of [C II] line emission. To perform a quantitatively fair comparison of [C II] sizes among our sample in terms of velocity width range, we took the following steps to define the line width of the [C II] line emission and create a form of visibility data optimized for size measurements: (1) extract spectrum with a 1-arcsec aperture from the data cube (20 km/s width per channel). Here, we used the data cube of the [C II] line emission, produced by the CASA/tclean task (CASA Team 2022). The tclean task was performed with auto-multi thresh algorithm and cleaned down to  $1\sigma$  (Herrera-Camus et al. in prep). We adopted the robust parameter of either Briggs ( $R = 0.5$ ) or Natural ( $R = 2.0$ ) weighting that creates the synthesized beam size of  $\theta_{\text{beam}} = 0''.3 - 0''.5$ , (2) fit the extracted spectrum with a single Gaussian  $f(\nu) \propto \exp[(\nu - \nu_0)^2 / 2\sigma^2]$  using the curve\_fit function within the scipy package (Virtanen et al. 2020). From the best-fit Gaussian function, we adopted the spectral range that contains 95% ( $= [2.5\%, 97.5\%]$ ) of the total [C II] line flux, corresponding to  $4\sigma$  ( $\pm 2\sigma$  from the central frequency  $\nu_0$ ) width



**Fig. 3.** Visualization of the visibility modeling of the [C II] line emission (white contours) in four systems that we showed in Figure 1. The left panel shows the dirty image of a single cube used for the visibility modeling (Section 3.2). The Gaussian FWHM fit from the dirty beam is shown as a white ellipse in the lower-left corner. The middle and right panel show the best-fit exponential disk model and the residual created by subtracting the model from the data, respectively. The contours start at  $2\sigma$  and increase in steps of  $3\sigma$  until  $20\sigma$ . The residual maps do not show any peaks above the  $2\sigma$  level around the rest-frame UV counterpart, which indicates that the observed emission is characterized by the best-fit model well. The rest of the sample is shown in Figure A.1 and A.2.



**Fig. 4.** [C II] luminosity-size relation of the CRISTAL sample. Symbols are based on the classification defined in Section 3.1. Each component of the pair/multiple-[C II] systems are shown separately. The right panel shows the histogram of [C II] sizes among categories with matched colors. We omit a histogram of multiple-[C II] because of the small sample size ( $N = 2$ ). A histogram with a solid black line shows the size distribution of the entire CRISTAL sample. The [C II] sizes show the diversity at fixed [C II] luminosity, in which relatively compact sizes ( $R_{e,[CII]} \lesssim 1$  kpc) were challenging to be measured in the previous low-resolution data.

of Gaussian ( $\approx 1.7$  Gaussian FWHM). We show a spectrum of CRISTAL-03 as an example in Figure 2. The  $\pm 2\sigma$  velocity range includes almost all of the [C II] line emission, which assures that the [C II] size measurements will be performed by fitting the representative velocity range of the emission. (3) Finally, we created a visibility measurement set that contains only information on the spectral range calculated above. Here, we used the visibility data where the FIR continuum emission was subtracted

by using CASA/uvcontsub task. The fitting of continuum slope was performed in the spectral range avoiding the [C II] frequency of each object. We then binned the visibilities into a single channel by specifying  $nchan = 1$  in the CASA/mstransform task. As an exceptional case, we fit the [C II] spectrum of CRISTAL-22a, which shows a clear double-peaked line profile, with a double Gaussian. This exceptionally broad and complex [C II] spectrum of CRISTAL-22a is likely due to a combination of merger and complex kinematical structure of the central component of CRISTAL-22a, which are verified from both [O III] 5007Å line emission map (Jones et al. 2024) and detailed kinematical analysis of the [C II] line emission (Telikova et al. 2024).

We used the UVMULTIFIT (Martí-Vidal et al. 2014) to model the visibilities of the [C II] line emission in the CRISTAL sample. The UVMULTIFIT implements simultaneous fitting of multiple components, which is useful for characterizing pair galaxies. We assumed a two-dimensional (2-D) exponential disk model ( $n = 1$ ) for all of the [C II] components and first allow six parameters (RA, Dec, total flux density, major-axis FWHM, minor-to-major axis ratio, and position angle of major axis) free. Some of the fittings fail to converge when the peak S/N of the [C II] line emission is not high enough (typically  $S/N < 8$ ). In this case, we fixed the projected minor-to-major axis ratio to unity.

The fit components were determined based on the classification described in Section 3.1. For single and multiple-UV classes, we adopt one-component modeling, and otherwise, we adopt two-component modeling. We show the images of the visibility data, the best-fit model, and the residual in Figure 3 for four systems that we showed in Figure 1. We show the rest of the sample in Figures A.1 and A.2. As can be seen in Figure 3, the best-fit model characterizes the observed [C II] line emission well and no signal greater than  $2\sigma$  significance level is present in the central  $2''$ -region, securing the validity of the fitting. Our analysis yielded structural parameters of a total number of 34 [C II] line components, including J1000+0234 (Capak et al. 2008), a massive submillimeter galaxy ( $S_{870\mu m} = 8.03$  mJy; Solimano et al. 2024) located in the proximity to CRISTAL-01a.

Finally, we convert the fitting outputs of the total flux density and major-axis FWHM into the total [C II] luminosity ( $L_{[CII]}$ ) and the effective radius ( $R_{e,[CII]}$ ), respectively. For a 2-D expo-

nential disk model, the major axis FWHM and major axis effective radius can be related as  $R_{e,\text{major}} = 1.21 \times \text{FWHM}$ , therefore we obtained a circularized effective radius by calculating  $R_{e,[\text{CII}]} = 1.21 \times \text{FWHM} \sqrt{q}$ , where  $q$  is the minor-to-major axis ratio. We estimate the uncertainty by using error propagation. For the uncertainty of each parameter (FWHM and  $q$ ), we adopt the output from the UVMULTIFIT, which is estimated from the post-fit covariance matrix (Martí-Vidal et al. 2014). We summarize our fitting results in Table B.1. We calculate an average value and standard deviation of the [C II] sizes of  $\langle R_{e,[\text{CII}]} \rangle = 1.90 \pm 0.77$  kpc. To fairly compare with the fitting results from the low-resolution archival data alone, we iterate the above procedure by only using the data taken in the ALPINE Survey. We present the results and discussion in Appendix C. In brief, we find a good agreement between two measurements for the [C II] fluxes and sizes ( $R_{e,[\text{CII}]} \gtrsim 1$  kpc). On the other hand, we find that the axis ratios tend to be poorly constrained when only the ALPINE data is used.

In Figure 4, we show a [C II] luminosity-size relation of the CRISTAL sample. To see the dependence of multiplicity, symbols are distinguished based on the classification presented in Section 3.1. Although we expect to find larger [C II] sizes in pair and multiple-UV systems compared to single systems, we were unable to statistically distinguish their size distributions by performing the Kolmogorov-Smirnov test (with  $p$  values of 0.23 and 0.12 for the pair and multiple-UV, respectively), largely due to our limited sample size. Overall, Figure 4 showcases the diversity of [C II] sizes at fixed [C II] luminosity, and we find that low-resolution data used in previous studies were unable to measure relatively compact sizes ( $R_{e,[\text{CII}]} \lesssim 1$  kpc).

### 3.2.2. Rest-frame UV and FIR continuum emission

To evaluate the spatial extent of [C II] line emission, we refer to two continuum size measurements (observing wavelengths of  $1.6 \mu\text{m}$  and  $870 \mu\text{m}$ ), which were both performed in Mitsuhashi et al. (2024). The rest-frame UV sizes ( $R_{e,\text{UV}}$ ) are measured with GALFIT (Peng et al. 2002) using the HST/WFC3 F160W images. A single Sérsic model with an index of  $n = 1$  is assumed (except for CRISTAL-13), and nearby objects seen in the HST images are masked by using SExtractor (Bertin & Arnouts 1996). The rest-frame FIR sizes ( $R_{e,\text{FIR}}$ ) are measured from the ALMA Band-7 continuum visibilities with the same method using UVMULTIFIT described in Section 3.2.1.

Mitsuhashi et al. (2024) classify the CRISTAL galaxies into either single or multiple systems based on the multiplicity in the HST/WFC3 F160W images. The multiple systems correspond to either pair, multiple-UV, or multiple-[C II] classified in Section 3.1 of this study. Unlike [C II] line emission, all of the FIR continuum emission was fit in a single exponential disk component due to the lower S/N detection compared to the [C II] line emission. While this hampers the fair comparison between FIR and [C II] line sizes for multiple-UV, or multiple-[C II] systems, we find that the FIR continuum is detected in either one of the pair systems (e.g., CRISTAL-04a, CRISTAL-07a), and hence we adopt the FIR sizes of these galaxies in this study.

## 4. Results and discussion

### 4.1. Size comparison

We start by comparing the measured effective radii among different tracers (rest-frame UV and FIR continua) to characterize

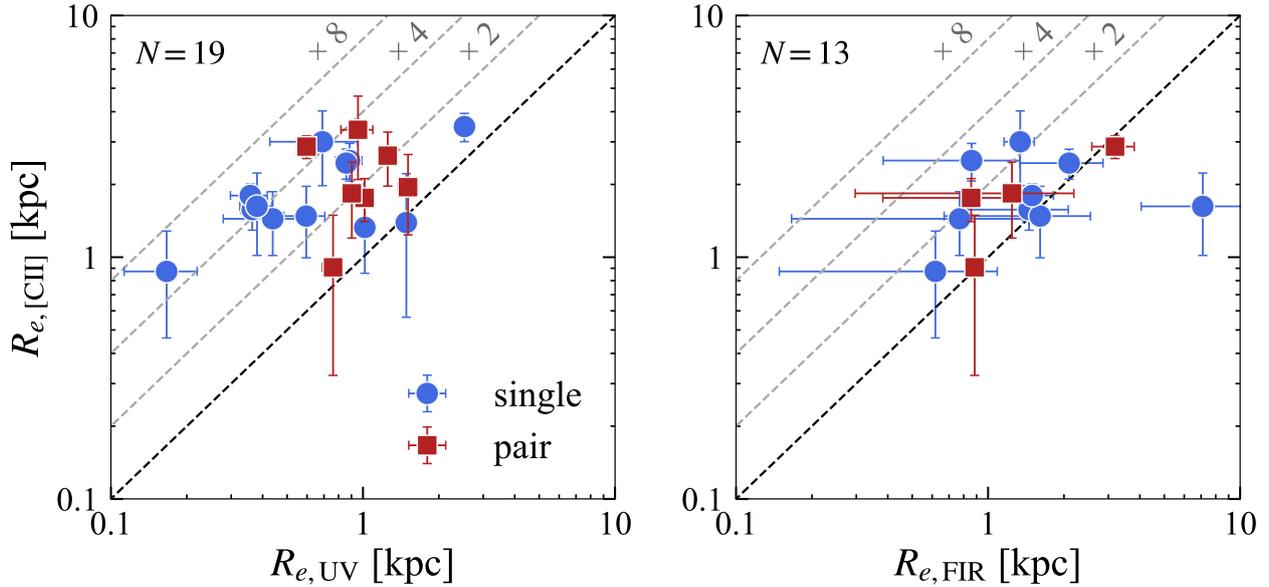
the spatial extent of the [C II] line emission in the context of star formation activity. In Table B.2, we list the sizes and size ratios discussed below.

The left panel of Figure 5 shows a comparison between the [C II] line and rest-frame UV continuum radii. From Figure 5 (left), we find that the [C II] line emission is systematically more extended than the rest-frame UV emission, which is well consistent with the previous findings (Carniani et al. 2018; Fujimoto et al. 2020; Fudamoto et al. 2022). The size ratio ( $R_{e,[\text{CII}]} / R_{e,\text{UV}}$ ) ranges from 0.94 (CRISTAL-16) to 5.03 (CRISTAL-20) with the average value and standard deviation of  $\langle R_{e,[\text{CII}]} / R_{e,\text{UV}} \rangle = 2.90 \pm 1.40$ . We note that the median (average) positional offset between the [C II] line and rest-frame UV continuum emission is 0.11 (0.14) arcsec ( $\sim 0.5$  kpc in a physical scale), which is smaller than the typical synthesized beam size of the CRISTAL data. We interpret this as them having consistent peak positions.

We exclude multiple-UV and multiple-[C II] systems in this diagram, because each [C II] line or UV component may arise from multiple galaxies for these classes, making the interpretation difficult. Among the multiple-UV systems, the central UV component in CRISTAL-01a and CRISTAL-01b was successfully modeled by GALFIT, whereas the remaining multiple-UV systems failed to converge due to contamination from nearby UV sources. We determine [C II]-to-UV size ratios of 3.0 and 3.8 for CRISTAL-01a and CRISTAL-01b, respectively, which are both slightly larger than the average value. Bowler et al. (2017) report larger UV sizes in bright UV galaxies with clumpy structures ( $M_{\text{UV}} \lesssim -21.5$  mag), suggesting a similar effect may influence the [C II] line emission in these multiple-UV systems (Figure A.1).

In the right panel of Figure 5, we show the size comparison between the [C II] line and FIR continuum emission. The latter was measured in visibility modeling with a circular exponential disk model (Mitsuhashi et al. 2024; Section 3.2.2). The best-fit central positions of the [C II] line and FIR continuum emission are in good agreement, with the median (average) offset of 0.09 (0.12) arcsec, again smaller than the beam size of the CRISTAL data. Similarly to the comparison with the UV continuum emission, we find that the [C II] line emission is comparable to, or more extended than the FIR continuum emission. One galaxy that is well below the one-to-one line is CRISTAL-21, which has an unreliable FIR size measurement due to the insufficient S/N of the visibility data, particularly at short  $uv$  distances. Therefore, hereafter, we do not include the results of CRISTAL-21 when the FIR radius is related to the discussions. We calculate the average size ratio and standard deviation of  $\langle R_{e,[\text{CII}]} / R_{e,\text{FIR}} \rangle = 1.54 \pm 0.63$ . Within the uncertainty, this size ratio suggests that the [C II] line radius is consistent with the FIR continuum radius. In fact, we find that two-thirds of the sample (eight out of 12) shown in Figure 5 have comparable FIR continuum radius with [C II] line radius ( $R_{e,[\text{CII}]} / R_{e,\text{FIR}} < 1.5$ ).

Three recent studies have independently reported similar results. Romano et al. (2024) performed a stacking analysis of [C II] line, FIR continuum ( $160 \mu\text{m}$ ), and near-UV (NUV;  $2300 \text{ \AA}$ ) continuum emission in local dwarf galaxies considered as analogs of high-redshift galaxies. They discovered that the [C II] line and FIR emission is more extended than the NUV emission. The single Sérsic fittings of [C II] line and FIR continuum show an excellent agreement in effective radius with a Gaussian-like profile (Sérsic index  $n \sim 0.5$ ). Pozzi et al. (2024) reported the same comparison for four galaxies drawn from the ALPINE Survey resulting in a median (average) size ratio of  $R_{e,[\text{CII}]} / R_{e,\text{FIR}} = 1.29 \pm 0.14$  ( $1.24 \pm 0.19$ ), which is slightly



**Fig. 5.** Comparisons of the effective radii of the [C II] line and the continuum emission. (Left) Effective radius of [C II] line emission compared to the rest-frame UV continuum emission (HST/WFC3 F160W). Symbols are the same as in Figure 4. The dashed black line indicates the one-to-one relation between  $R_{e,[\text{CII}]}$  and  $R_{e,\text{UV}}$ , and three dashed gray lines above this line represent  $R_{e,[\text{CII}]} / R_{e,\text{UV}} = 2, 4, 8$ . (Right) Same as the left panel, but [C II] line radius is compared to the rest-frame FIR emission, measured from the ALMA Band-7 continuum images (Mitsunashi et al. 2024). On average, the [C II] sizes are larger than the rest-frame UV sizes by a factor of 2.90; compared to the rest-frame FIR sizes, they tend to be larger by a factor of 1.54 although with large uncertainties.

smaller than our measurements. Two out of four galaxies are CRISTAL-24 and CRISTAL-25, and we confirm that the measurements are consistent with ours within uncertainties. Given that both the average size ratio and its standard deviation derived from the CRISTAL sample are larger than the values reported by Pozzi et al. (2024), we are probing more diverse populations in terms of spatial relation between [C II] line and FIR continuum emission, likely due to the improved spatial resolution and sensitivity of the CRISTAL data. Finally, Díaz-Santos et al. (2021) reported an average size ratio of  $\langle R_{e,[\text{CII}]} / R_{e,\text{FIR}} \rangle = 1.61 \pm 0.10$  for four dust-obscured quasars at  $z \approx 3.0 - 4.6$ , which are a few orders of magnitude brighter in the IR luminosity compared to our sample (see also Venemans et al. 2020). All these studies imply that the range of [C II]-to-FIR size ratios at high redshift is relatively narrow ( $1 \lesssim R_{e,[\text{CII}]} / R_{e,\text{FIR}} \lesssim 2$ ), compared to that of [C II]-to-UV size ratios which can be affected by dust obscuration.

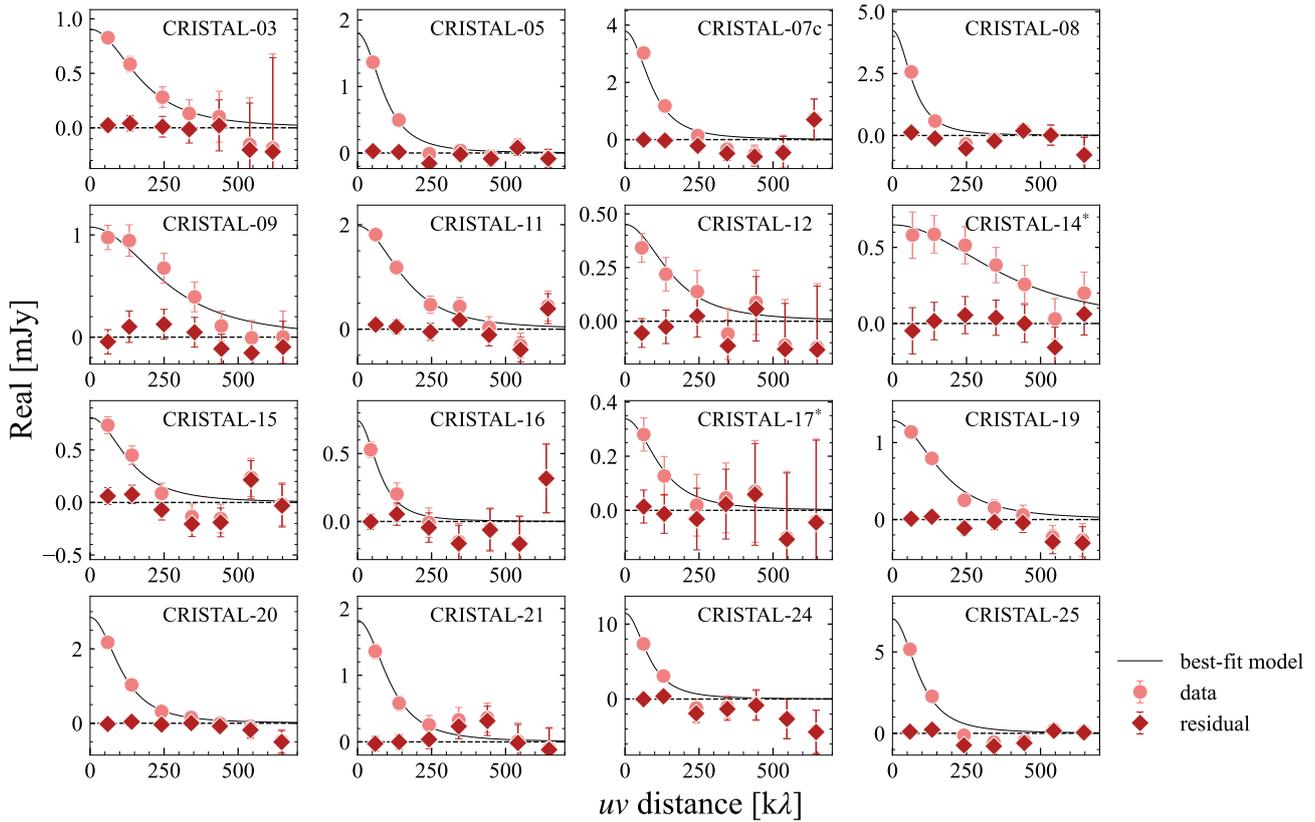
One possible origin of extended [C II] line emission is ongoing merging activity. When diffuse carbon-rich gas is morphologically disturbed, or taken away from the stellar component, the [C II] line emission can become more extended compared to the rest-frame UV continuum. Such a phenomenon has been exemplified in the case of vuds\_cosmos\_5101209780 (Ginolfi et al. 2020a) and CRISTAL-05 (Posses et al. 2024) as well as a larger sample of merging galaxies in the ALPINE sample (Di Cesare et al. 2024). Ginolfi et al. (2020a) and Di Cesare et al. (2024) report that  $\sim 25\text{--}50\%$  of the total [C II] line emission is coming from a diffuse gas envelope. The fraction of [C II] line emission originating from the envelope is defined by subtracting the [C II] line flux of the “galaxy” component from the total [C II] line flux, characterized by spectra extracted from regions above  $1\sigma$  or  $2\sigma$  significance level in the moment-0 maps. These studies highlight the impact of early metal-enrichment at large radii, though the definition depends on the sensitivity of the observations. In particular, extended line

flux with low S/N may not be CLEANed if the stopping threshold of  $\tau_{\text{clean}}$  is higher than this flux, potentially leading to an overestimation of the extended and diffuse flux. For galaxies classified as single, we derive  $\langle R_{e,[\text{CII}]} / R_{e,\text{UV}} \rangle = 3.21 \pm 1.42$  and  $\langle R_{e,[\text{CII}]} / R_{e,\text{FIR}} \rangle = 1.62 \pm 0.69$ , while for pair systems we find  $\langle R_{e,[\text{CII}]} / R_{e,\text{UV}} \rangle = 2.38 \pm 1.22$  and  $\langle R_{e,[\text{CII}]} / R_{e,\text{FIR}} \rangle = 1.36 \pm 0.45$ . Given the large uncertainties of these size ratios, we refrain from claiming an ongoing physical effect from galaxy interactions. Thus, we tentatively conclude that we do not find differences in size ratios between isolated galaxies classified as single and mergers classified as pair systems.

Since there is a tight correlation between [C II] luminosity and SFR, [C II] line emission has been used as an indicator of star formation activity. However, the size differences between [C II] line and continuum (rest-frame UV and FIR) emission suggests that the [C II] line emission is not completely spatially coupled to star formation activity, which might be at odds with studies of nearby galaxies (Pineda et al. 2014; Kapala et al. 2015; Herrera-Camus et al. 2015). Given the average size ratios of 2.9 and 1.5, we infer that the [C II] line emission is approximately two times more extended than the star formation activity traced by continuum emission. We shall further discuss this point in Section 4.3.

#### 4.2. Constituent of [C II] line emission

In this section, we assess whether [C II] line emission in the SFGs has a halo structure as a secondary component. If such a halo structure is confirmed, the physical origin would be different from the central [C II] component associated with star-forming ISM (e.g., star-formation-driven outflow, cold stream). Therefore, the identification of [C II] halo gives us an important insight into the origin of the extended [C II] line emission.



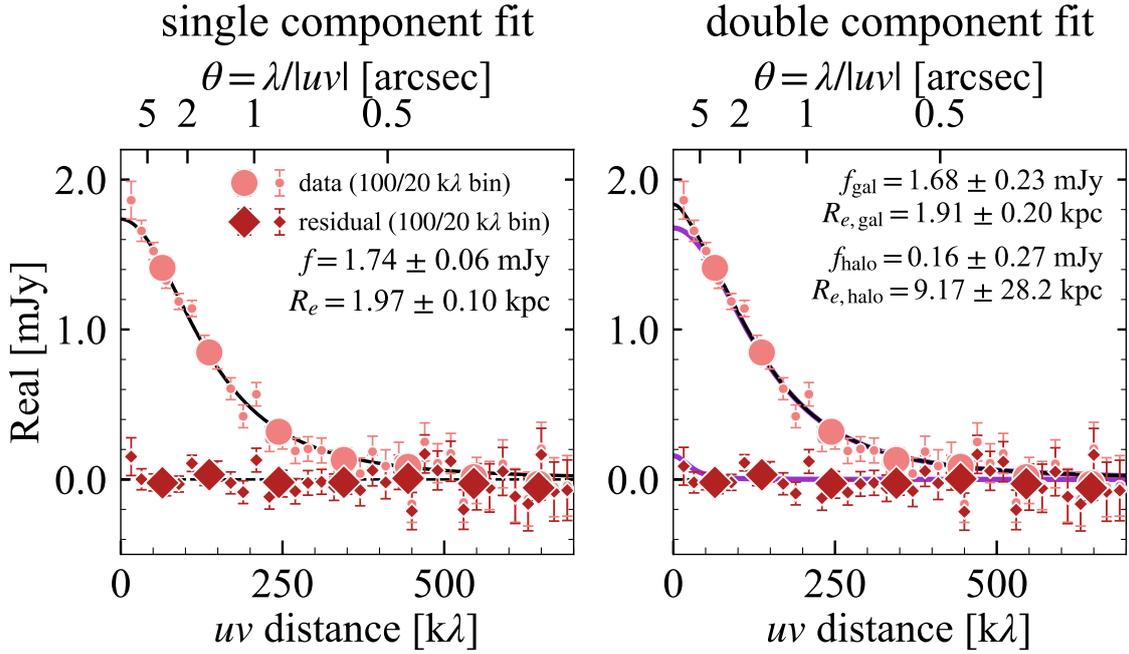
**Fig. 6.** Flux density in the form of the real part of the visibility, as a function of  $uv$  distances along the minor axis. Each data point represents the mean value per  $100\text{ k}\lambda$  bin. The galaxies that were fit in a circular exponential disk model are marked in an asterisk. The uncertainties represent the standard deviation. Both the data (circle) and the residual (diamond) visibilities are shown. The residuals are created by subtracting the best-fit model (solid black line) from the data.

Because [C II] halo is expected to have low-surface density at large radii, most of the previous studies needed to rely on the stacking analysis to confirm such structure (Fujimoto et al. 2019; Ginolfi et al. 2020b; Novak et al. 2020). To date, the only case in an individual [C II] halo has been confirmed as an extended secondary component structure is A1689-zD1, a strongly lensed galaxy at  $z = 7.13$  (Akins et al. 2022). As observations of the CRISTAL Survey are deeper than the previous observations, we can now assess whether such structure can be confirmed individually. To eliminate the possibility that [C II] line emission from satellite galaxies contaminates the halo component, we focus on 16 single galaxies, which we classified in Section 3.1. We do not include CRISTAL-23c since the galaxy might be in a phase of triple-merger (Jones et al. 2020).

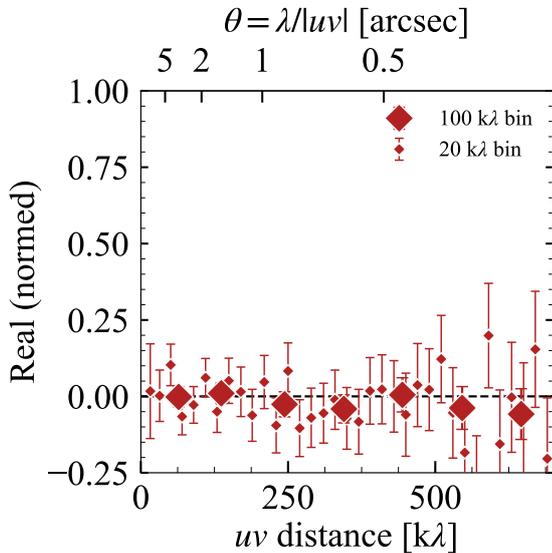
Figure 6 visualizes the data, best-fit model, and residual as a form of visibility data for 16 single objects that we created in Section 3.2. The average velocity range of 16 single galaxies is  $485.0\text{ km/s}$ . The data is extracted by the `getdata` function of a `casatool` ms. In Figure 6, average values and standard deviations of the real part of visibility data per  $100\text{ k}\lambda$  bin are shown. The residual data is created by subtracting the best-fit model from the data. For all galaxies, the data and the best-fit model show a good agreement, and we do not find an excess at the residual data in the shortest  $uv$  distance bin ( $\sim 50\text{ k}\lambda$ ). This indicates that the visibility profile can be well fit by an exponential disk model and an extended secondary component is not necessary to explain the data.

To further confirm this, we stack the visibility data of 16 single galaxies and again perform the visibility modeling in the

same manner. We perform both single component and double component fittings. The result of the single component fitting is shown in the left panel of Figure 7. As well as the visibility data of the individual galaxies, the stacked visibility data is fit well by a single exponential disk profile. The model is characterized by an effective radius of  $R_{e,[\text{CII}]} = 1.97 \pm 0.10\text{ kpc}$ , assuming an average redshift of  $z = 5.22$ , which is consistent with the average radius ( $\langle R_{e,[\text{CII}]} \rangle = 1.90\text{ kpc}$ ) of the entire CRISTAL galaxies. At the smallest  $20\text{ k}\lambda$  bin of the residual visibility, we find a flux excess of  $0.15\text{ mJy}$  ( $1.2\sigma$  significance level). The result of the double component fitting is shown in the right panel of Figure 7. Here, we assume two concentric exponential disk components. The brighter component ( $1.68 \pm 0.23\text{ mJy}$ ; hereafter “galaxy” component) has a radius of  $R_{e,\text{gal}} = 1.91 \pm 0.20\text{ kpc}$ , which is similar to the best-fit single component. The other component ( $0.16 \pm 0.27\text{ mJy}$ ; hereafter “halo” component) has an extended radius of  $R_{e,\text{halo}} = 9.17 \pm 28.2\text{ kpc}$ . Since the fittings converge to the same reduced  $\chi^2$  value, we cannot statistically favor either the single or double component model. However, the existence of an extended, diffuse component remains uncertain due to its faintness and large uncertainties. The flux of the “halo” component constitutes  $8.7 \pm 13.4\%$  of the total flux, and this is smaller than what has been suggested in previous [C II] line observations (e.g.,  $\sim 30\%$  for A1689-zD1 reported in Akins et al. 2022, but see Jones et al. 2023 for faint gaseous halo detected in CO  $J = 3 - 2$  line emission). The flux becomes negative within the range of the uncertainty, and the standard deviation of  $\pm 0.13\text{ mJy}$  at the smallest  $20\text{ k}\lambda$  bin gives the detection of  $1.2\sigma$  level, which both point out that the detection is not significant. As we have



**Fig. 7.** Real part of the stacked visibility (circles) and the residual visibility (diamonds) as a function of  $uv$  distances for single component (left) and double component (“galaxy” + “halo”; right) fittings. Average values of two types of binning (20  $k\lambda$  and 100  $k\lambda$ ) are shown. Uncertainties represent a standard deviation of binned visibility data. The best-fit models are shown as a solid black line (total) and solid purple lines (each component). The flux and effective radius of the best-fit models are summarized at the upper right corners. At the smallest 20  $k\lambda$  bin, the residual show an excess at  $1.2\sigma$  and  $0.7\sigma$  significance levels, which corresponds to 8.8% and 5.5% of the total flux density for single and double component fittings, respectively.



**Fig. 8.** Real part of the stacked residual visibility as a function of  $uv$  distances. Average values of two types of binning (20  $k\lambda$  and 100  $k\lambda$ ) are shown. Uncertainties represent a standard deviation of binned visibility data.

identified various axis ratios ( $q = 0.31 - 0.90$ ) in our sample (Table B.1), it is possible that the extended [C II] line emission along the major axis is diluted by the stacking and create the “halo” component artificially.

Alternatively, we now focus on the stacked residual of the visibility data where the main disk component obtained from a single exponential disk fitting is subtracted. Figure 8 shows the stacked residual visibility as a function of  $uv$ -distances. In order to avoid the stacked visibility data being skewed by the

bright objects in which the amplitude of residual visibility is also bright, we normalize the residual visibility by the total [C II] flux obtained from the best-fit model before the stacking. We show the average values per both 20  $k\lambda$  and 100  $k\lambda$  bins, but no clear excess can be found in either case. By adopting standard deviations of visibility data within each bin as uncertainties, the small deviations from the horizontal axis at shorter- $uv$  distances ( $\lesssim 200 k\lambda$ ) are below the  $1\sigma$  level. If the fitting results are dragged by data from the shorter  $uv$ -distances, we would find an excess at larger  $uv$ -distances as a remnant of the fitting, but no such feature can be found.

To summarize, from the double component fitting in the stacked visibility data (Figure 7 right), we do not find a statistically significant evidence of [C II] halo as a secondary component. The modeled secondary component consists of  $8.7 \pm 13.4\%$  of the total flux, which is smaller by several times than what has been suggested in the previous [C II] line observations at high redshift. Based on Figures 6, 7, and 8, we conclude that the [C II] line emission of the CRISTAL galaxies can be adequately explained by a single exponential disk component.

#### 4.3. What determines the spatial extent of the [C II] line?

In this section, we discuss the origin of extended [C II] line emission. The correlation between [C II] luminosity and SFR, which holds true for several orders of magnitude, suggests that the [C II] line emission can be considered a good tracer of PDRs on molecular cloud surface ( $n \approx 10^3 - 10^5 \text{ cm}^{-3}$ ,  $T \approx 10^2 \text{ K}$ ) surrounding young massive stars. However, [C II] line emission can arise from more diffuse gaseous components ( $n \lesssim 10^3 \text{ cm}^{-3}$ ) than PDRs. Following the description of the ISM conditions in Madden et al. (1997), these are cold neutral medium ( $n \approx 10^2 \text{ cm}^{-3}$ ,  $T \approx 10^2 \text{ K}$ ), warm neutral medium ( $n \approx 1 \text{ cm}^{-3}$ ,  $T \approx 5 \times 10^3 \text{ K}$ ), and ionized medium ( $n \lesssim 1 \text{ cm}^{-3}$ ,

$T \approx 10^4$  K; Section 4.3.2). In neutral ISM conditions, atomic hydrogen would be the dominant collision partner, while in PDRs either atomic or molecular hydrogen can be effective in the [C II] excitation (Goldsmith et al. 2012).

As FIR continuum emission traces a dust re-emission, the spatial extent of FIR continuum emission can be regarded as regions where PDRs are dominant. Hence, the comparable spatial extent between the [C II] line and FIR continuum emission ( $R_{e,[CII]}/R_{e,FIR} \approx 1$ ) indicates that the [C II] line emission coincides with star formation activity traced by the PDRs. Umehata et al. (2021) report the [C II] line and FIR continuum observations of galaxies in the SSA22 protocluster at  $z = 3.1$  and discuss that [C II] line emission is mainly associated with star formation activity, although other origins and potential effects from the overdense environment are not ruled out. Novak et al. (2020) also draw a similar conclusion for  $z > 6$  quasars. However, as those samples are limited to IR-bright galaxies with  $L_{IR} \gtrsim 10^{12}L_{\odot}$ , the results may not apply to typical SFGs ( $L_{IR} \lesssim 10^{12}L_{\odot}$ ) at corresponding redshifts. Previous studies have reported few galaxies showing  $R_{e,[CII]}/R_{e,FIR} \approx 1$  (Fujimoto et al. 2020; Pozzi et al. 2024), and thanks to the sensitivity of ALMA observations taken by the CRISTAL Survey, we can now postulate whether such galaxies comprise of the majority of the SFGs at  $z \sim 4 - 6$ , which is consistent with the general picture that the [C II] line emission is coming from the PDRs.

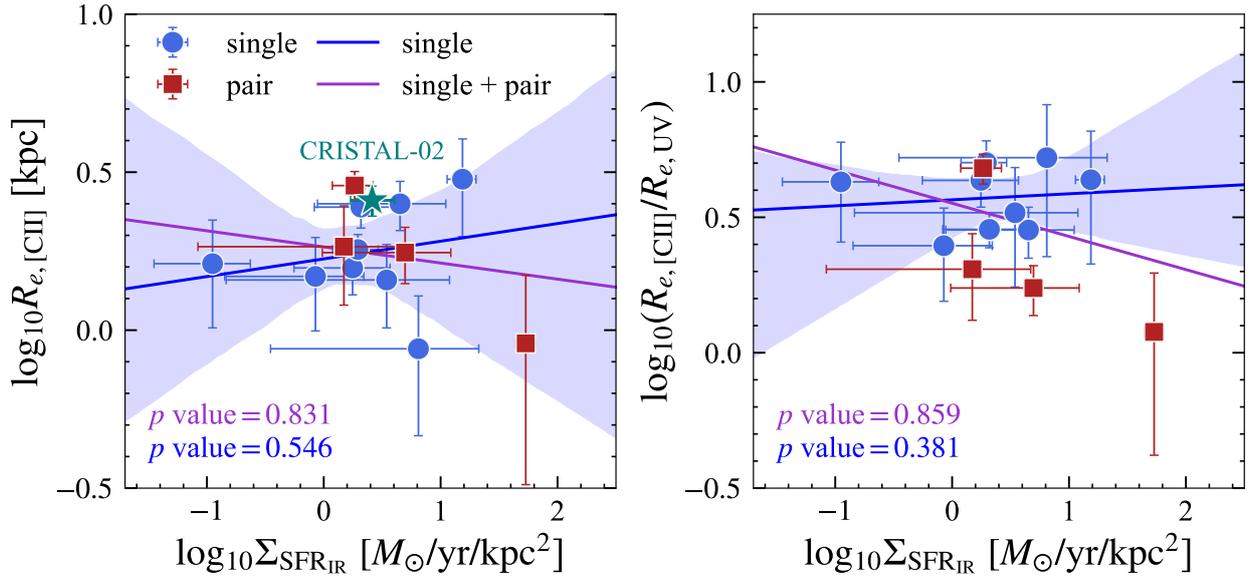
From the size comparisons that we presented in Section 4.1, we find that the sizes of the [C II] line emission in our sample are on average 2.90 and 1.54 times larger compared to the rest-frame UV and FIR continuum emission, respectively (Figure 5), suggesting that [C II] line emission is approximately twice more extended than the main star-forming regions. This indicates that the contribution from the PDRs is not sufficient to explain the [C II] line emission beyond the radius of star-forming regions. For simplicity, if we assume that the [C II] radius is exactly twice more larger than the radius that encloses half of the SFR, and the contribution from PDRs is dominant (100%) within the [C II] radius ( $r < R_{e,[CII]}$ ), the average contribution from PDRs at  $r > R_{e,[CII]}$  is roughly estimated to be  $\approx 20\%$ . When spatially integrated, the PDR fraction is then  $\approx 60\%$ . Low contribution from PDRs at the outskirts of the galaxies is qualitatively consistent with Li et al. (2024), who find that the spatially resolved  $\Sigma_{[CII]} - \Sigma_{SFR}$  has a steeper slope in about half of the CRISTAL galaxies that are examined than the ones found in nearby star-forming galaxies (e.g., De Looze et al. 2014; Herrera-Camus et al. 2015). While this could be caused by the [C II] deficit in the central regions, since we do not find such evidence as we show later (see Figure 10 in Section 4.3.3; see also Herrera-Camus et al. 2021 and Posses et al. 2024 for individual cases), we suggest that the  $\Sigma_{[CII]} - \Sigma_{SFR}$  does not hold at large radii as the central region tends to deviate toward brighter [C II] surface densities.

In the Milky Way, Pineda et al. (2013) report that about 20% of the [C II] line emission arises from the cold neutral medium. In M33, Kramer et al. (2013) discover an increasing contribution from a cold neutral medium to the [C II] line emission with radius. For Haro 11, a nearby dwarf galaxy that has similar [C II] and IR luminosities to the CRISTAL galaxies, Cormier et al. (2012) report a contribution from PDRs to the [C II] line emission of 10%, while the rest of the [C II] line emission is coming from diffuse low-ionization gas. de Blok et al. (2016) compare the spectra of [C II], CO  $J=1-0$ , and HI lines of a sample of 10 nearby galaxies. They find that the radial profile of the [C II] line emission is taking an intermediate slope between CO  $J=1-0$  and HI lines (see also Tarantino et al. 2021). These studies

motivate us to think that by measuring the spatial extent of [C II] line emission at a kiloparsec-scale resolution, we are looking at the intermediate spatial extent between molecular and atomic gas distributions. Considering that the average HI gas fraction ( $M_{HI}/(M_{HI} + M_{\star})$ ) monotonically increases with redshift, from 25% at  $z = 0$  to 70% at  $z \sim 4-6$  (Walter et al. 2020; Heintz et al. 2021), and that HI gas is thought to be extended up to a circumgalactic scale along the filaments of the cosmic web (e.g., Katz et al. 2017), the extended [C II] line emission in the CRISTAL galaxies is likely to be a combination of that coming from PDRs and cold/warm neutral medium, where most of the mass can be traced by molecular and atomic hydrogen, respectively. In nearby galaxies, the dust mass surface density correlates with the total gas mass surface density better than the molecular or atomic surface densities at a kiloparsec scale (e.g., Casasola et al. 2022). Since the atomic gas distribution is generally more extended than that of the molecular gas, the strong correlation between dust and total gas mass suggests that at large radii, dust can be a good tracer of atomic gas rather than molecular gas. While we cannot assume the same correlation to the CRISTAL galaxies due to the differences in gas fraction and metallicity, this correlation in nearby galaxies supplements our argument that the contribution from atomic gas to the [C II] line emission becomes increasingly dominant with radius.

Numerous theoretical works have been presented to constrain the properties of FIR fine-structure lines at high redshift (e.g., Nagamine et al. 2006; Vallini et al. 2013, 2015; Katz et al. 2017; Pallottini et al. 2017; Olsen et al. 2018; Lagache et al. 2018; Popping et al. 2019; Arata et al. 2020; Ramos Padilla et al. 2023; Gurman et al. 2024; Casavecchia et al. 2025, 2024; Muñoz-Elgueta et al. 2024). Some of the studies that align with the discussion above include Ramos Padilla et al. (2023) who simulated the dominant fraction (up to  $\approx 70-90\%$ ) of [C II] line emission coming from the atomic gas phase in high-redshift galaxies (see also Casavecchia et al. 2025). Similarly, Gurman et al. (2024) report that the contribution from warm neutral medium (not necessarily molecular gas) is dominant ( $\approx 30 - 40\%$ ) particularly at sub-solar metallicity while H II region may be comparably important, based on high-resolution hydrodynamical simulations of a self-regulated ISM. In contrast, Vallini et al. (2015) discuss that the [C II] line emission from cold gas may be attenuated by cosmic microwave background (CMB) by a factor of 0.1–0.2, because the CMB temperature approaches the spin temperature of the [C II] line transition in the cold neutral medium ( $\sim 20$  K). This results in a minor contribution of cold neutral gas ( $\lesssim 10\%$ ) to the [C II] line emission (see also Olsen et al. 2018; Lagache et al. 2018). It should be noted that these simulated galaxies are affected by slightly higher CMB temperatures since they are at higher redshifts ( $z \gtrsim 6$ ) than our sample.

The cause of variations in  $R_{e,[CII]}/R_{e,FIR}$  among individual galaxies is still not clear. If extended [C II] line emission originates from a diffuse neutral medium, then it is possible that the [C II] line emission can be taken away from the host galaxies during merger events, as has been demonstrated in simulated galaxies (Pallottini et al. 2022). While we fail to statistically confirm that pair systems have more extended [C II] sizes than others (Section 3.2), JWST images reveal that some single galaxies identified by HST images are actually composed of multiple stellar components (Lines et al. 2024). This includes two galaxies, CRISTAL-07c and CRISTAL-11, which have  $R_{e,[CII]}/R_{e,FIR} > 2$ . Future assessments of how the  $R_{e,[CII]}/R_{e,FIR}$  (and  $R_{e,[CII]}/R_{e,UV}$ ) varies during past merger events using zoom-in cosmological simulations will give an insight into our results. Alternatively,



**Fig. 9.** Dependence of the spatial extent of [C II] line emission on the  $\text{SFR}_{\text{IR}}$  surface density. (Left) [C II] line radius as a function of the  $\text{SFR}_{\text{IR}}$  surface density. The solid blue and purple lines show a best-fit linear regression for single and single+pair sources, respectively. The shaded region shows a 95% confidence level of the fit for single galaxies. The  $p$  values of a Spearman’s rank correlation test for both single and single+pair parent samples are shown in the lower-left corner. We also highlight CRISTAL-02 (multiple-UV), a galaxy which shows an evidence of broad [C II] wing component in multiple spatially resolved elements of the galaxy (Davies et al. in prep). (Right) Same as the left panel, but taking the [C II]-to-UV size ratio as the vertical axis. Given the  $p$  values, we cannot rule out the null hypothesis that there is no correlation between these parameters.

the variations in  $R_{e,[\text{CII}]} / R_{e,\text{FIR}}$  in our sample may reflect the presence of extraplanar gas and dust, as is demonstrated by the observations of NGC 891, a nearby edge-on galaxy. Reach et al. (2020) report that the [C II] line emission in a thick disk of NGC 891 has larger scale height (2.8 kpc) compared to mid-IR emission tracing PAHs, as well as FIR emission (1.4 kpc; Bocchio et al. 2016). Nonetheless, the data with deeper sensitivity and higher spatial resolution are required to verify this scenario in our sample.

In the following, we discuss four alternative mechanisms that could be the cause of extended [C II] line emission in addition to diffuse neutral gas: outflows (Section 4.3.1), ionized gas (Section 4.3.2), radial variation in the [C II] deficit (Section 4.3.3), and shock heating (Section 4.3.4).

#### 4.3.1. Outflows

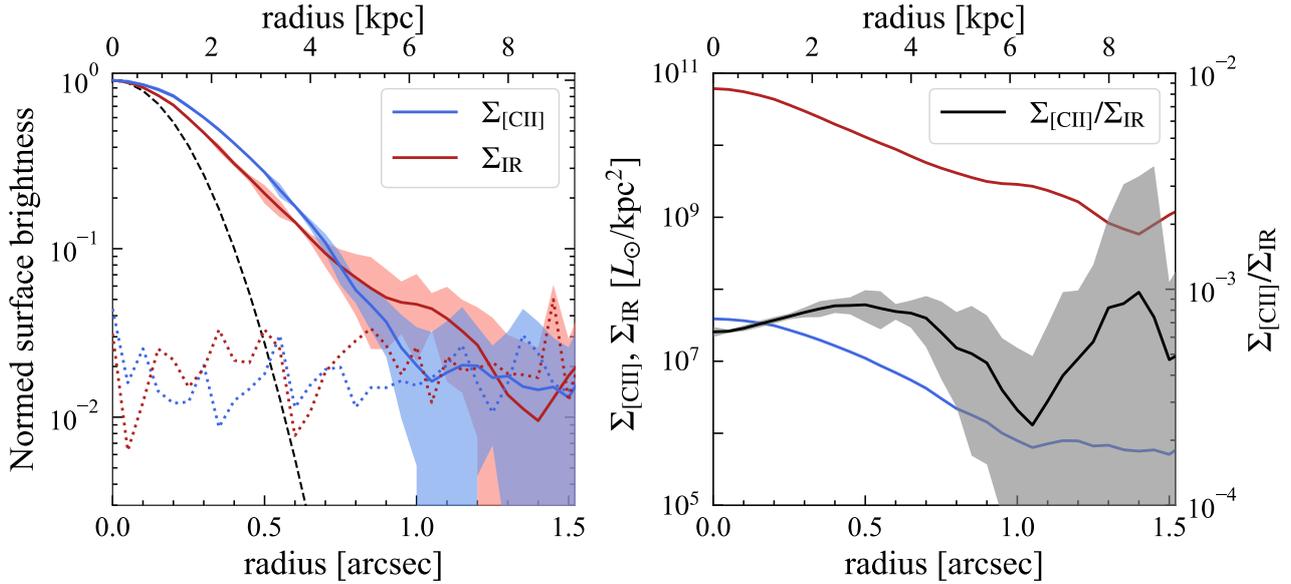
One of the supporting scenarios for the extended [C II] line emission is ongoing outflows driven by star formation activity. Semi-analytical models predict that cold-mode outflows could reproduce the extended [C II] line emission (Pizzati et al. 2020, 2023), and this has been observationally supported by the spectra stacking analysis of [C II] line emission for both star-forming galaxies at  $4 < z < 6$  (Gallerani et al. 2018; Ginolfi et al. 2020b) and local low-metallicity dwarf galaxies (Romano et al. 2023). On the other hand, Akins et al. (2022) do not find an outflow signature in [C II] line from a strongly lensed galaxy A1689-zD1 at  $z = 7.13$ , but detect a broad component in [O III] 88  $\mu\text{m}$  line emission, indicating the presence of ionized outflowing gas that will subsequently cool and emit the [C II] line emission at larger radius (see also Wong et al. 2022). For  $z > 6$  quasars, Novak et al. (2020) report null detection of broad spectral feature from [C II] line based on spectral stacking (see also Decarli et al. 2018).

As such, it is still not clear whether there is a physical association between outflows and the extended [C II] line emis-

sion seen in projected sky distribution at  $z > 4$ . The situation has become more puzzling, since recent ALMA observations (Spilker et al. 2020; Salak et al. 2024; Nianias et al. 2024) report the detection of a blueshifted OH 119  $\mu\text{m}$  absorption feature as evidence of molecular outflows, while a broad [C II] line feature is not detected for the same sources. These results indicate that the [C II] line emission is not always a robust tracer of molecular outflows. Levy et al. (2023) present a [C II] line observation of the outflow region of a nearby starburst galaxy M 82. The authors find that the fraction of [C II] line flux associated with the outflow region is about one-quarter of the total [C II] line emission, and the majority (>55%) of the [C II] line flux in the outflow region arises from the atomic component. If the composition of the [C II] line in high-redshift galaxies is similar to M 82, it is not surprising to have a weak or no detection of the broad [C II] line feature.

It has also been suggested that AGN outflows can enhance [C II] line emission due to an additional contribution from either X-ray-dominated or ionized regions (Smirnova-Pinchukova et al. 2019, but also see Stacey et al. 2010). Since the original sample selection in the ALPINE Survey excluded Type I AGN with broad optical spectral line (Le Fèvre et al. 2020), our sample similarly does not include bright Type I AGN. However, Li et al. (2024) discuss that CRISTAL-25 may be an AGN, because the spatially resolved SED fitting analysis shows poor fit at the central region, possibly due to the contamination of broad emission lines from AGN to the broad band photometry. Nonetheless, we confirm that [C II] line emission in CRISTAL-25 is not particularly bright compared to the FIR continuum ( $L_{[\text{CII}]} / L_{\text{FIR}} = 3.7 \times 10^{-3}$ ), and so the possible effect of AGN on the enhancement of [C II] line emission is not likely playing a role in this galaxy.

In this study, we are likely measuring the sizes of [C II] line emission arising from both galactic ISM and outflows, if they exist. The median velocity width we use to measure the spatial extent of the [C II] line emission is 440 km/s, which



**Fig. 10.** Radial profiles of the stacked [C II] line and FIR continuum emission. (Left) Normalized radial surface density profile of the  $uv$ -stacked image in [C II] line ( $R_{e,[\text{CII}]} = 1.97 \pm 0.17$  kpc) and FIR continuum ( $R_{e,\text{FIR}} = 1.53 \pm 0.22$  kpc) emission. The dotted lines show average surface density derived by setting random apertures on blank regions, which are also shown in color-shaded regions as uncertainties. The dashed black curve represents the clean PSF. The top axis is converted to a physical scale assuming an average redshift of  $z = 5.22$  among the stacked sample. (Right) Absolute radial surface density profiles of the [C II] line and FIR continuum emission, in which the unit is converted to  $L_{\odot}/\text{kpc}^2$ . The solid black line shows the ratio between the [C II] line and IR emission (axis shown on the right hand side). As we do not see a strong radial variation in the [C II]-to-IR luminosity ratio, we suggest that the [C II] deficit is not responsible for the extended [C II] line emission.

is broad enough that star-formation-driven outflows can contribute to the observed structure of the [C II] line emission. Sugahara et al. (2019) report a positive correlation between SFR and outflow velocity up to  $z \sim 6$ . A similar correlation between SFR (or its surface density  $\Sigma_{\text{SFR}}$ ) and mass outflow rate is also reported for nearby galaxies (e.g., Fluetsch et al. 2019; see also Veilleux et al. 2020; Förster Schreiber & Wuyts 2020 and references therein).

Among the CRISTAL galaxies, CRISTAL-02 only shows a strong broad wing component in the [C II] line spectrum (Davies et al. in prep) and weak evidence of broad wing component is detected when the [C II] spectra are stacked among the CRISTAL galaxies (Birkin et al. in prep). Based on these findings, if outflows contribute to the extended [C II] line emission, we might see a correlation between [C II] sizes and galactic properties.

Figure 9 shows the [C II] size and [C II]-to-UV size ratio as a function of the  $\text{SFR}_{\text{IR}}$  surface density ( $\Sigma_{\text{SFR}_{\text{IR}}} = \text{SFR}_{\text{IR}}/2\pi R_{e,\text{FIR}}^2$ ) of the CRISTAL galaxies. We use the values of  $\text{SFR}_{\text{IR}}$  measured in Mitsuhashi et al. (2024) who convert FIR continuum flux ( $S_{158\mu\text{m}}$ ) into IR luminosity ( $L_{\text{IR}}$ ) and then into obscured SFR ( $\text{SFR}_{\text{IR}}$ ) following the same method as Béthermin et al. (2020). According to a linear regression fitting, we find a positive trend for single galaxies in both panels in Figure 9, but a negative trend when pair galaxies are included. Nonetheless, the Spearman's rank correlation tests give the  $p$  values of 0.546 (single fit) and 0.831 (single+pair fit) for  $\log_{10} \Sigma_{\text{SFR}_{\text{IR}}} - \log_{10} R_{e,[\text{CII}]}$  relation (Figure 9 left), and 0.381 (single fit) and 0.859 (single+pair fit) for  $\log_{10} \Sigma_{\text{SFR}_{\text{IR}}} - \log_{10} (R_{e,[\text{CII}]} / R_{e,\text{UV}})$  relation (Figure 9 right). We similarly investigated the [C II] size and [C II]-to-UV size ratio as a function of SFR, but none of the correlations were significant ( $p$  value  $> 0.05$ ). Therefore, regardless of the merging events, we fail to rule out the null hypothesis that there is no association between star-formation-driven (atomic) outflows and the extended [C II] line emission. In addition, we find that CRISTAL-02 does not have particularly large [C II] size

nor  $\text{SFR}_{\text{IR}}$  surface density among the CRISTAL galaxies. These results may imply that there is no strong association between (atomic) outflows and the extended [C II] line emission.

#### 4.3.2. Contribution from ionized gas

Due to the low-ionization potential of carbon, [C II] line could originate from ionized regions. Because nitrogen has a higher ionization potential than hydrogen, the [N II] 205  $\mu\text{m}$  line, which has a similar critical density as the [C II] line when collisionally excited by electrons, has been widely used to discern the contribution of the [C II] line from ionized gas. Alternatively, [O III] 88  $\mu\text{m}$  can also be used as a tracer of ionized gas (e.g., Herrera-Camus et al. 2018a; Harikane et al. 2020), but unfortunately the [O III] 88  $\mu\text{m}$  line from the redshifts of our sample is hardly accessible through the atmospheric windows.

Studies of nearby galaxies with measurements of both [C II] and [N II] 205  $\mu\text{m}$  lines suggest that ionized gas, either diffuse ionized gas or H II regions, is not the main contributor of [C II] line emission (e.g., Croxall et al. 2017; Herrera-Camus et al. 2018a; Sutter et al. 2019; Tarantino et al. 2021). Nearby luminous infrared galaxies (LIRGs) are reported to have a PDR fraction of [C II] line larger than 60%, up to 95% (Díaz-Santos et al. 2017). For high-redshift galaxies, Pavesi et al. (2016) study [N II] 205  $\mu\text{m}$  line for two Lyman-break galaxies, CRISTAL-02 (LBG-1) and CRISTAL-22 (HZ10), and report higher [C II]-to-[N II] luminosity ratio for CRISTAL-02, which is less dusty than CRISTAL-22 (see also Umehata et al. 2017; Cunningham et al. 2020). The estimated contributions from ionized gas are  $\sim 5\%$  and 10–25% for CRISTAL-02 and CRISTAL-22, respectively.

Croxall et al. (2017) find a trend of decreasing [C II]-to-[N II] luminosity ratio with decreasing gas-phase metallicity in the local SFGs; that is, a low contribution to the [C II] line emission from the ionized gas at high metallicity (see also Cormier et al. 2019). Assuming that the mass-metallicity

relations (Nakajima et al. 2023) hold true in the CRISTAL galaxies, the empirical relation presented in Croxall et al. (2017) provides an ionized fraction of 13–27% in a stellar mass range of  $\log(M_*/M_\odot) = [9.5, 11.0]$ . This agrees with the estimated ionized fraction of CRISTAL-22 with  $\log(M_*/M_\odot) = 10.35 \pm 0.37$  (Mitsuhashi et al. 2024). Since the majority of the CRISTAL galaxies have lower stellar masses than this, we infer that the [C II] line flux contributed from the ionized medium is not as significant as  $\sim 25\%$ , indicating that the contribution from ionized gas has little impact on the spatial extent of [C II] line emission.

However, some theoretical studies show mixed results regarding the impact of diffuse ionized gas on [C II] line emission (e.g., Olsen et al. 2018; Ramos Padilla et al. 2023). Future high-resolution [N II] 205  $\mu\text{m}$  observations will be crucial to elucidate the spatial distribution of [C II] line emission associated with ionized gas at high redshift.

#### 4.3.3. [C II] deficit in the central region of galaxies

It is known that the [C II]-to-(F)IR luminosity ratio varies depending on the ISM conditions; for instance the ratio is particularly low in regions where (F)IR surface density is high. Several physical explanations have been made, such as low photoelectric heating efficiency due to small grain destruction or charging, high ionization parameter, and thermal saturation of the [C II] line emission (e.g., Malhotra et al. 2001; Muñoz & Oh 2016; Díaz-Santos et al. 2017; Herrera-Camus et al. 2018b). Because this so-called [C II] deficit is prominent in the central region of galaxies (e.g., Smith et al. 2017; Litke et al. 2019; Venemans et al. 2020), it is possible that the larger sizes measured in [C II] line emission compared to FIR continuum emission accompany the radial dependence on the [C II] deficit.

To inspect this, we stacked ten single galaxies, in which both [C II] line and FIR continuum emission is detected. The stacking was performed in visibility using the CASA/concat task. The phase centers of individual visibility data are shifted to match the coordinates at which the [C II] line emission peaks. We image both stacked [C II] line and FIR continuum emission using the CASA/tclean task with natural weighting, and clean down to  $1.5\sigma$  noise level by applying  $3''$  aperture mask, where  $\sigma$  is the rms noise level of the dirty image. We show the normalized surface density profiles of the stacked clean image in the left panel of Figure 10. Both [C II] line and FIR continuum emission exhibit an extended structure beyond the PSF Gaussian profile with an effective radius of  $1.97 \pm 0.17$  kpc and  $1.53 \pm 0.22$  kpc, respectively. Beyond a beam-convolved radius of  $1''$ , the surface densities of [C II] line and FIR continuum emission become comparable to the surface densities derived from setting random apertures, and the emission is likely not genuine. The IR surface density profile shows a small bump at  $1''$ . By inspecting the stacked image, we confirm that this bump results from the elongated structure at the  $2\text{--}3\sigma$  significance level of the FIR continuum emission. We therefore do not attribute the bump at  $1''$  to mergers or halo structure.

In the right panel of Figure 10, we show the absolute surface density profiles (left axis) and their ratio (right axis). The  $\Sigma_{[\text{C II}]}/\Sigma_{\text{IR}}$  profile fluctuates around the global value of  $8 \times 10^{-4}$ , with a gradual increase until  $0''.5$  (3 kpc) and subsequent decrease at least up to  $\sim 0''.8$  (5 kpc). The global value of  $\Sigma_{[\text{C II}]}/\Sigma_{\text{IR}} = 8 \times 10^{-4}$  is in fact smaller than the expected value of  $\Sigma_{[\text{C II}]}/\Sigma_{\text{IR}} = (1 - 4) \times 10^{-3}$  (e.g., Herrera-Camus et al. 2018a; Zanella et al. 2018) for the CRISTAL galaxies with  $\Sigma_{\text{IR}} \sim 10^{10} - 10^{11} L_\odot/\text{kpc}^2$  (Mitsuhashi et al. 2024). We attribute this lower ratio in the stacked image to the IR-bright galaxies in our

sample (CRISTAL-21 and CRISTAL-24), which are an order of magnitude brighter in IR luminosity than the rest of the CRISTAL galaxies. However, our interest here is the radial variation in  $\Sigma_{[\text{C II}]}/\Sigma_{\text{IR}}$ , and so we have confirmed that the overall trend is unchanged when such exceptionally IR-bright galaxies are excluded from the stacking. Because the radial variations in  $\Sigma_{[\text{C II}]}/\Sigma_{\text{IR}}$  are not monotonically decreasing toward the center and instead are relatively flat, the [C II] deficit is not particularly strong in the central region. This may be at odds with nearby galaxies (Smith et al. 2017), but consistent with some of the quasar-host galaxies at  $z \gtrsim 6$  (Venemans et al. 2020) and the individual CRISTAL galaxies (Herrera-Camus et al. 2021; Posses et al. 2023; Li et al. 2024). In summary, we suggest that radial variation in the [C II] deficit is not the primary cause of the extended [C II] line emission.

#### 4.3.4. Shocked gas

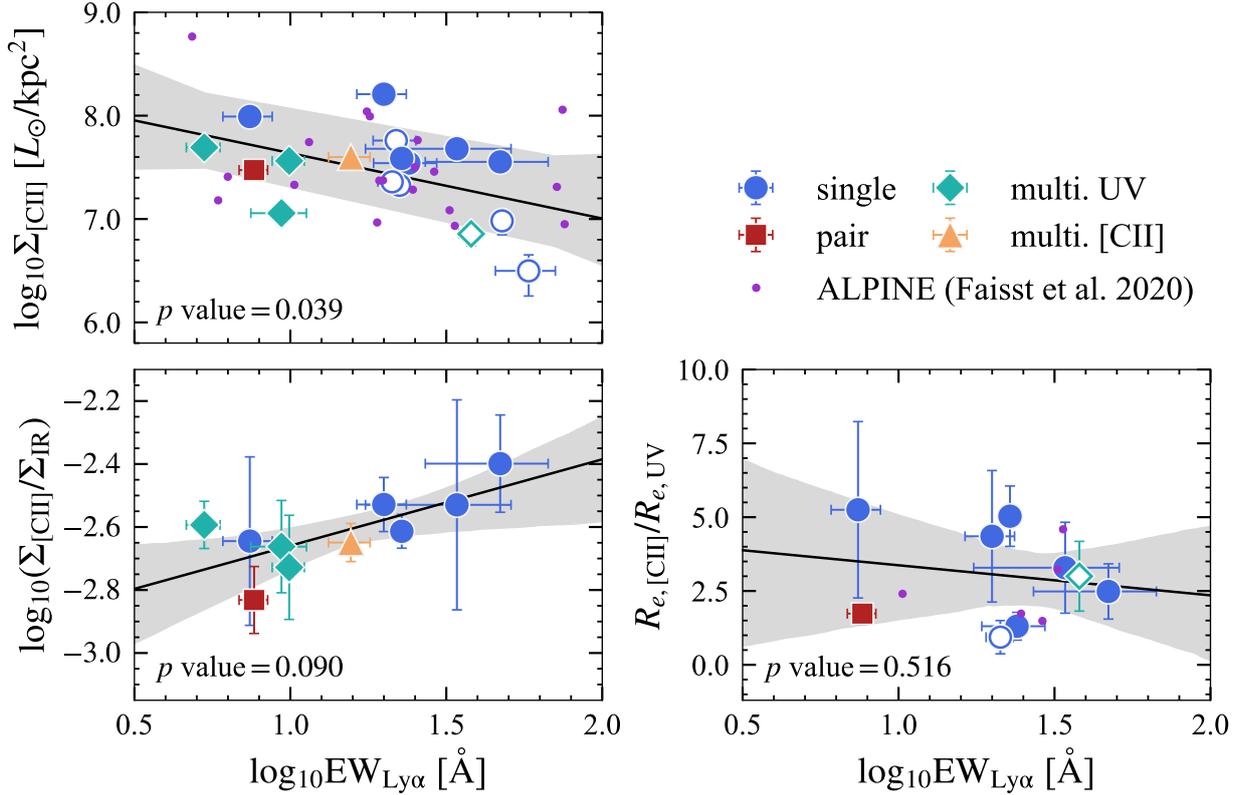
The alternative mechanism that can enhance the [C II] line emission without star formation activity is shock heating produced in a merging system or in a galaxy group (Appleton et al. 2013; Peterson et al. 2018; Fadda et al. 2023): kinetic energy from shocks and turbulence is injected into the gas and excite the ionized carbon by collisions. We refer the readers to Posses et al. (2024) for detailed discussion on the argument that the [C II] line emission in CRISTAL-05 is likely to be enhanced by shock heating. In short, the enhanced [C II] line emission due to shock heating is suggested from evidence of merging activity and a high [C II]-to-IR luminosity ratio ( $L_{[\text{C II}]} / L_{\text{IR}} \gtrsim 10^{-2}$ ). The latter can also be tested by comparing the [C II] surface density to SFR surface density.

Among the CRISTAL galaxies except for CRISTAL-05 (Posses et al. 2024), the pair and multiple-UV systems are the likely candidates that may emit [C II] line emission induced by shock heating. However, as we show in Table B.2 and discuss at the beginning of Section 4.3, most of these systems have a moderate size ratio between the [C II] line and FIR continuum ( $R_{e,[\text{C II}]} / R_{e,\text{FIR}} \sim 0.7 - 1.5$ ), so their [C II] line emission can mostly be explained by PDRs. Two exceptions are CRISTAL-04a ( $R_{e,[\text{C II}]} / R_{e,\text{FIR}} = 2.1 \pm 1.2$ ) and CRISTAL-13 ( $R_{e,[\text{C II}]} / R_{e,\text{FIR}} = 2.7 \pm 2.1$ ), but neither of them shows high [C II]-to-IR luminosity ratio ( $L_{[\text{C II}]} / L_{\text{IR}} \approx 3 \times 10^{-3}$ ). Shocked gas heating is not likely the driver of extended [C II] line emission.

#### 4.4. Connection to Ly $\alpha$ and H $\alpha$ emission

Harikane et al. (2018) find an anti-correlation between [C II] luminosity and Lyman- $\alpha$  line (Ly $\alpha$  line,  $\lambda = 1216 \text{ \AA}$ ) equivalent width (EW) for Ly $\alpha$  emitters at  $z = 4 - 7$ . This anti-correlation is likely to exist for each galaxy population, such as Lyman- $\alpha$  emitters and star-forming main sequence galaxies, since typical [C II] luminosity at fixed Ly $\alpha$  EW differs across galaxy populations (Díaz-Santos et al. 2021). However, Endsley et al. (2022) do not find such anti-correlation for UV-bright galaxies at  $z \approx 7$ , possibly due to either a limited dynamic range of Ly $\alpha$  EW ( $< 20 \text{ \AA}$ ) or insufficient statistics.

To study how the [C II] line properties of our sample correlate with Ly $\alpha$  emission, we plot the [C II] line surface density ( $\Sigma_{[\text{C II}]} = L_{[\text{C II}]} / 2\pi R_{e,[\text{C II}]}^2$ ), the [C II]-to-IR surface density ratio ( $\Sigma_{[\text{C II}]} / \Sigma_{\text{IR}}$ ) within the [C II] effective radius, and the [C II]-to-UV size ratio ( $R_{e,[\text{C II}]} / R_{e,\text{UV}}$ ) as a function of the Ly $\alpha$  EW (EW $_{\text{Ly}\alpha}$ ) in Figure 11. We estimate the IR luminosity within the [C II] radius based on the best-fit model in the visibility modeling. The values of EW $_{\text{Ly}\alpha}$  are presented in the catalogs



**Fig. 11.** [C II] surface density (top left), [C II]-to-IR surface density ratio (bottom left), and [C II]-to-UV size ratio (bottom right) of the CRISTAL galaxies as a function of the rest-frame EW of Ly $\alpha$  emission. The Ly $\alpha$  properties are taken from Faisst et al. (2020). The galaxies without dust continuum detection are denoted by open symbols. Small purple circles shown in the top left and bottom right panels are the ALPINE galaxies in which [C II] surface density, [C II]-to-UV size ratio (Fujimoto et al. 2020), and Ly $\alpha$  EW (Faisst et al. 2020) are available. We show the linear regression fitting (Table 1) in the solid black line, with the shaded region representing the 95% confidence interval. The  $p$  value of a Spearman’s rank correlation test is shown in the lower-left corner of each panel.

**Table 1.** Summary of the best-fit parameters in Figure 11.

$y$	$m$	$b$
$\log_{10} \Sigma_{[\text{C II}]}$	-0.633	8.27
$\log_{10}(\Sigma_{[\text{C II}]}/\Sigma_{\text{IR}})$	0.274	-2.93
$R_{e,[\text{C II}]} / R_{e,\text{UV}}$	-1.02	4.39

**Notes.** Slope ( $m$ ) and intercept ( $b$ ) of the linear regression fittings performed in Figure 11. Parameters are determined from the form of  $y = m \log_{10} \text{EW}_{\text{Ly}\alpha} + b$ .

of both Faisst et al. (2020) and Cassata et al. (2020). Since Cassata et al. (2020) report the  $\text{EW}_{\text{Ly}\alpha}$  value only for the galaxies with [C II] line detection in the ALPINE Survey, we adopt the values from Faisst et al. (2020) to increase the sample size. Here, we convert the  $\text{EW}_{\text{Ly}\alpha}$  reported in the observed-frame to the rest-frame by applying a correction factor of  $(1+z)^{-1}$ . In agreement with previous findings, we find a decreasing trend of the [C II] line surface density with increasing  $\text{EW}_{\text{Ly}\alpha}$ , with a Spearman’s rank correlation coefficient of  $-0.51$  and a  $p$  value of  $0.039$ . Moreover, we find the [C II]-to-IR surface density ratio positively correlates with  $\text{EW}_{\text{Ly}\alpha}$  with a correlation coefficient of  $0.56$  and a  $p$  value of  $0.090$ . The size ratio of [C II] line and UV radii appears to decrease with  $\text{EW}_{\text{Ly}\alpha}$ , which aligns with the results from Fujimoto et al. (2020), although a Spearman’s rank correlation test give a  $p$  value of  $0.516$ . We perform a linear regression fitting for each correlation and present the fitting

results in Table 1. As a side note, we do not find a correlation between [C II] line radius and  $\text{EW}_{\text{Ly}\alpha}$ .

The correlations we present in Figure 11 imply that there is physical interplay between [C II] line, dust, and Ly $\alpha$  emission. Noticeably, we find that three galaxies (CRISTAL-01a, 12, and 17) with the lowest [C II] surface density with  $\Sigma_{[\text{C II}]} < 10^7 L_{\odot}/\text{kpc}^2$  have large Ly $\alpha$  EW ( $\text{EW}_{\text{Ly}\alpha} \gtrsim 10^{1.5} \text{\AA}$ ) and are not detected in FIR continuum emission (Mitsuhashi et al. 2024). On the other hand, galaxies with small Ly $\alpha$  EW ( $\text{EW}_{\text{Ly}\alpha} \lesssim 10^{1.5} \text{\AA}$ ) exhibit a high [C II] surface density ( $\Sigma_{[\text{C II}]} > 10^7 L_{\odot}/\text{kpc}^2$ ) and a low [C II]-to-IR surface density ratio ( $\Sigma_{[\text{C II}]}/\Sigma_{\text{IR}} \lesssim 10^{-2.5}$ ); in other words, a [C II] deficit. These ratios indicate that the low dust content in the ISM of these galaxies facilitates the escape of Ly $\alpha$  photons and vice versa. In such ISM conditions, the ionization parameter is expected to be higher compared to the galaxies with strong FIR continuum detection. Simultaneously, the limited amount of dust likely leads to low [C II] surface density by reducing the efficiency of photoelectric heating.

It is known that the velocity offsets between the systemic velocity (measured from [C II] line or optical emission lines) and the velocity of the peak of Ly $\alpha$  line anti-correlate with  $\text{EW}_{\text{Ly}\alpha}$  (Hashimoto et al. 2013, 2019; Erb et al. 2014; Valentino et al. 2022), which has also been confirmed for the ALPINE sample (Cassata et al. 2020). As large velocity offsets indicate high HI column density, the galaxies with small  $\text{EW}_{\text{Ly}\alpha}$  have higher HI column densities than the ones with large  $\text{EW}_{\text{Ly}\alpha}$ , which may explain extended [C II] line emission if it arises from the atomic gas (Section 4.3). Therefore, although it is not conclusive whether the weak anti-correlation between  $R_{e,[\text{C II}]} / R_{e,\text{UV}}$  and

$\text{Ly}\alpha$  EW is real, the large  $\text{Ly}\alpha$  EW, low H I column density, small amount of dust, and small  $R_{e,[\text{CII}]} / R_{e,\text{UV}}$  are consistent with each other, and larger fraction of the [C II] line emission may arise from the ionized gas in such galaxies (Section 4.3.2).

However, we note that the  $\text{Ly}\alpha$  properties currently available are taken by slit spectroscopy (Cassata et al. 2020), and only global properties without spatial information can be inferred. We thus expect that future  $\text{Ly}\alpha$  observations by integral field spectroscopy (IFS) would be crucial to compare the spatial extent and morphology between [C II] line and  $\text{Ly}\alpha$  emission.

Another fundamental tracer emitted from hydrogen atoms is the Balmer- $\alpha$  line ( $\text{H}\alpha$  line,  $\lambda = 6563 \text{ \AA}$ ).  $\text{H}\alpha$  line traces an instantaneous star formation activity ( $\sim 10\text{--}100 \text{ Myr}$ ), so if the  $\text{H}\alpha$  line is more extended than continuum emission tracing star-formation activity over  $\sim 100 \text{ Myr}$ , this would support the idea that these galaxies are in a phase of “inside-out” growth and neutral gas at larger radii is heated by recent star formation activity. Herrera-Camus et al. (2015) show that [C II] line emission can arise and hold the [C II]-SFR relation with a short duration (2 Myr) of star formation activity with high heating efficiency from FUV to [C II] line emission ( $\epsilon_{\text{H}} \simeq 1 - 3\%$ ), suggesting the possibility that recent star formation activity causing the extended [C II] line emission may be traced by  $\text{H}\alpha$  line emission.

As JWST has recently enabled us to study the spatial distribution of the  $\text{H}\alpha$  line at comparable redshifts to our sample (e.g., Birkin et al. 2023; Übler et al. 2024; Matharu et al. 2024; Nelson et al. 2024), it is of great interest to compare the morphological and kinematical properties of  $\text{H}\alpha$  and [C II] lines (Kohandel et al. 2024). Two of the galaxies among our sample (CRISTAL-20 and CRISTAL-22) have been observed in JWST/NIRSpec IFU mode (Parlanti et al. 2024; Jones et al. 2024), offering new insights into the ionized gas properties of typical star-forming galaxies at high redshift. In CRISTAL-20, Parlanti et al. (2024) reveal ionized outflows traced by the [O III]5007 $\text{ \AA}$  and  $\text{H}\alpha$  lines, which are co-spatial to the neutral outflows traced by [C II] line. Jones et al. (2024) discover brighter  $\text{H}\alpha$  line emission in CRISTAL-22b than CRISTAL-22a, whereas dust continuum is weaker, suggesting different evolutionary phases among the complex merging system. A future systematic census of ionized gas properties in the CRISTAL galaxies with JWST will provide unprecedented insights into the spatial correlation between neutral and ionized gas.

## 5. Conclusions

We have presented the [C II] size measurements and size comparisons with other tracers for typical SFGs at  $z = 4 - 6$  taken by the CRISTAL Survey. The data of the survey benefits from the deep sensitivity ( $1\sigma \sim 0.1 - 0.2 \text{ mJy}$  per 20 km/s channel bin) to search faint extended emission and high spatial resolution ( $\theta_{\text{beam}} \sim 0''.3$ ), which enables us to identify and characterize multiple galaxies in proximity. Our main findings are as follows:

1. [C II] sizes are similar among various merger states. We performed size measurements of [C II] line emission via visibility modeling analysis. The structural parameters of 33 components are reported in Table B.1, including pairs (e.g., CRISTAL-07ab) and complex UV systems (e.g., CRISTAL-02, CRISTAL-10). In spite of a variety of merger states, we do not statistically confirm the difference in [C II] sizes between single and pair ( $p$  value = 0.23)/multiple-UV ( $p$  value = 0.12) systems.
2. Extended [C II] line emission revealed by size comparison. Based on the comparisons between [C II] line radius and rest-frame UV, and FIR radii, we find average size ratios

and standard deviations of  $\langle R_{e,[\text{CII}]} / R_{e,\text{UV}} \rangle = 2.90 \pm 1.40$  and  $\langle R_{e,[\text{CII}]} / R_{e,\text{FIR}} \rangle = 1.54 \pm 0.63$ , respectively. This indicates that [C II] line emission is approximately twice more extended than the main star-forming regions traced by rest-frame UV and FIR continuum emission.

3. [C II] line emission as a single extended disk component. We assessed whether the [C II] line emission can be characterized by a disk with a secondary halo structure by performing both single and double component fittings in visibility. While we have obtained the two-component model ( $R_{e,\text{gal}} = 1.91 \pm 0.20 \text{ kpc}$ ,  $R_{e,\text{halo}} = 9.17 \pm 28.2 \text{ kpc}$ ), the flux density of “[C II] halo” is weaker than the typical uncertainty of the visibility data in short  $uv$  distances ( $\sim 20 \text{ k}\lambda$ ), and the single extended disk component ( $R_e = 1.97 \pm 0.10 \text{ kpc}$ ) characterizes the observed [C II] line emission with an equal level of statistical support. In the stacked residual visibility, we did not detect any significant flux excess, thus we conclude that the [C II] line emission in our sample can be adequately characterized by a single disk component.
4. Origin of [C II] line emission. While the [C II] line emission in about half of our sample can be explained by PDRs associated with the star formation activity, the extent of [C II] line emission in the rest of the sample appears to require an additional source of excitation. The most likely is [C II] line emission coming from the diffuse medium, either neutral atomic gas or ionized gas, although the effect of such components at high redshift is unsettled from a theoretical perspective. We argue that the diversity in [C II] sizes may be further caused by different merger history and the existence of extraplanar gas and dust. In contrast, the [C II] deficit in the central region of the galaxies, and shocked gas heating induced by mergers are not likely to be responsible for the extended [C II] line emission.
5. Correlations with the  $\text{Ly}\alpha$  properties. We find a negative correlation between [C II] surface density ( $\Sigma_{[\text{CII}]}$ ) and  $\text{Ly}\alpha$  EW ( $p$  value = 0.039), and a tentative positive correlation between [C II]-to-IR surface density ratio ( $\Sigma_{[\text{CII}]} / \Sigma_{\text{IR}}$ ) and  $\text{Ly}\alpha$  EW ( $p$  value = 0.090). These correlations between [C II] and  $\text{Ly}\alpha$  properties can be understood by the amount of gas and dust content, which is essential for producing the [C II] line emission via photoelectric heating. High [C II] surface density suggests high neutral gas column density, leading to strong attenuation of  $\text{Ly}\alpha$  emission (low  $\text{Ly}\alpha$  EW). We also find a possible negative correlation between [C II]-to-UV size ratio ( $R_{e,[\text{CII}]} / R_{e,\text{UV}}$ ) and  $\text{Ly}\alpha$  EW. If the correlation is real, this would support the scenario that extended [C II] line emission at large radii is arising from the atomic gas component. Future IFS studies of both  $\text{Ly}\alpha$  and  $\text{H}\alpha$  lines are expected to explain the variations in the [C II] line and dust properties among the typical SFGs at this epoch.

*Acknowledgements.* We thank the anonymous referee for valuable comments that improved the content of this paper. R.I. would like to thank Seiji Fujimoto, Mahsa Kohandel, Rebecca C. Levy, Zongnan Li, Yuichi Matsuda, Marcel Neeleman, and Andrea Pallottini for illuminating discussions and suggestions. R.I. is supported by Grants-in-Aid for Japan Society for the Promotion of Science (JSPS) Fellows (KAKENHI Grant Number 23KJ1006). K.-i.T. is supported by JSPS KAKENHI grant No. 23K03466. M.A. acknowledges support from the ANID BASAL project FB210003. I.D.L. has received funding from the European Research Council (ERC) under the European Union’s Horizon 2020 research and innovation programme DustOrigin (ERC-2019-StG-851622) and from the Flemish Fund for Scientific Research (FWO-Vlaanderen) through the research projects G023821N and G0A1523N. R.H.-C. thanks the Max Planck Society for support under the Partner Group project “The Baryon Cycle in Galaxies” between the Max Planck for Extraterrestrial Physics and the Universidad de Concepción. R.H.-C. also gratefully acknowledge financial support from ANID

BASAL projects FB210003. R.A.A.B. acknowledges support from an STFC Ernest Rutherford Fellowship [grant number ST/T003596/1]. E.d.C acknowledges support from the Australian Research Council (projects DP240100589 and CE170100013). R.L.D. is supported by the Australian Research Council through the Discovery Early Career Researcher Award (DECRA) Fellowship DE240100136 funded by the Australian Government. T.D.S. was supported by the Hellenic Foundation for Research and Innovation (HFRI) under the “2nd Call for HFRI Research Projects to support Faculty Members & Researchers” (Project Number: 3382). A.F. acknowledges support from the ERC Advanced Grant INTERSTELLAR H2020/740120. M.K. was supported by the ANID BASAL project FB210003. M.S. was financially supported by Becas-ANID scholarship #21221511, and also acknowledges ANID BASAL project FB210003. K.T. was supported by ALMA ANID grant number 31220026 and by the ANID BASAL project FB210003. H.Ü. gratefully acknowledges support by the Isaac Newton Trust and by the Kavli Foundation through a Newton-Kavli Junior Fellowship. V.V. acknowledges support from the ALMA-ANID Postdoctoral Fellowship under the award ASTRO21-0062. This paper makes use of the following ALMA data: ADS/JAO.ALMA#2017.1.00428.L, #2018.1.01359.S, #2018.1.01605.S, #2019.1.00226.S, #2019.1.01075.S, and #2021.1.00280.L. ALMA is a partnership of ESO (representing its member states), NSF (USA), and NINS (Japan), together with NRC (Canada), MOST and ASIAA (Taiwan), and KASI (Republic of Korea), in cooperation with the Republic of Chile. The Joint ALMA Observatory is operated by ESO, AUI/NRAO, and NAOJ. We thank the ALMA staff and, in particular, the EA-ARC staff for their support. Data analyses were carried out in part on the Multiwavelength Data Analysis System operated by the Astronomy Data Center (ADC) at the National Astronomical Observatory of Japan.

## References

- Akins, H. B., Fujimoto, S., Finlator, K., et al. 2022, *ApJ*, 934, 64
- Appleton, P. N., Guillard, P., Boulanger, F., et al. 2013, *ApJ*, 777, 66
- Arata, S., Yajima, H., Nagamine, K., Abe, M., & Khochfar, S. 2020, *MNRAS*, 498, 5541
- Aravena, M., Heintz, K., Dessauges-Zavadsky, M., et al. 2024, *A&A*, 682, A24
- Bertin, E., & Arnouts, S. 1996, *A&AS*, 117, 393
- Béthermin, M., Fudamoto, Y., Ginolfi, M., et al. 2020, *A&A*, 643, A2
- Bigiel, F., de Looze, I., Krabbe, A., et al. 2020, *ApJ*, 903, 30
- Birkin, J. E., Hutchison, T. A., Welch, B., et al. 2023, *ApJ*, 958, 64
- Bischetti, M., Choi, H., Fiore, F., et al. 2024, *ApJ*, 970, 9
- Bocchio, M., Bianchi, S., Hunt, L. K., & Schneider, R. 2016, *A&A*, 586, A8
- Bowler, R. A. A., Dunlop, J. S., McLure, R. J., & McLeod, D. J. 2017, *MNRAS*, 466, 3612
- Capak, P., Carilli, C. L., Lee, N., et al. 2008, *ApJ*, 681, L53
- Capak, P. L., Carilli, C., Jones, G., et al. 2015, *Nature*, 522, 455
- Carilli, C. L., & Walter, F. 2013, *ARA&A*, 51, 105
- Carniani, S., Maiolino, R., Amorin, R., et al. 2018, *MNRAS*, 478, 1170
- CASA Team (Bean, B., et al.) 2022, *PASP*, 134, 114501
- Casasola, V., Bianchi, S., Magrini, L., et al. 2022, *A&A*, 668, A130
- Casavecchia, B., Maio, U., Péroux, C., & Ciardi, B. 2024, *A&A*, 689, A106
- Casavecchia, B., Maio, U., Péroux, C., & Ciardi, B. 2025, *A&A*, 693, A119
- Cassata, P., Morselli, L., Faisst, A., et al. 2020, *A&A*, 643, A6
- Cormier, D., Leboutteiller, V., Madden, S. C., et al. 2012, *A&A*, 548, A20
- Cormier, D., Abel, N. P., Hony, S., et al. 2019, *A&A*, 626, A23
- Croxall, K. V., Smith, J. D., Pellegrini, E., et al. 2017, *ApJ*, 845, 96
- Cunningham, D. J. M., Chapman, S. C., Aravena, M., et al. 2020, *MNRAS*, 494, 4090
- de Blok, W. J. G., Walter, F., Smith, J. D. T., et al. 2016, *AJ*, 152, 51
- Decarli, R., Walter, F., Venemans, B. P., et al. 2018, *ApJ*, 854, 97
- De Looze, I., Cormier, D., Leboutteiller, V., et al. 2014, *A&A*, 568, A62
- Dessauges-Zavadsky, M., Ginolfi, M., Pozzi, F., et al. 2020, *A&A*, 643, A5
- Devereaux, T., Cassata, P., Ibar, E., et al. 2024, *A&A*, 686, A156
- Díaz-Santos, T., Armus, L., Charmandaris, V., et al. 2013, *ApJ*, 774, 68
- Díaz-Santos, T., Armus, L., Charmandaris, V., et al. 2017, *ApJ*, 846, 32
- Díaz-Santos, T., Assef, R. J., Eisenhardt, P. R. M., et al. 2021, *A&A*, 654, A37
- Di Cesare, C., Ginolfi, M., Graziani, L., et al. 2024, *A&A*, 690, A255
- Endsley, R., Stark, D. P., Bouwens, R. J., et al. 2022, *MNRAS*, 517, 5642
- Erb, D. K., Steidel, C. C., Trainor, R. F., et al. 2014, *ApJ*, 795, 33
- Fadda, D., Sutter, J. S., Minchin, R., & Polles, F. 2023, *ApJ*, 957, 83
- Faisst, A. L., Schaefer, D., Lemaux, B. C., et al. 2020, *ApJS*, 247, 61
- Fluetsch, A., Maiolino, R., Carniani, S., et al. 2019, *MNRAS*, 483, 4586
- Förster Schreiber, N. M., & Wuyts, S. 2020, *ARA&A*, 58, 661
- Fudamoto, Y., Smit, R., Bowler, R. A. A., et al. 2022, *ApJ*, 934, 144
- Fujimoto, S., Ouchi, M., Ferrara, A., et al. 2019, *ApJ*, 887, 107
- Fujimoto, S., Silverman, J. D., Béthermin, M., et al. 2020, *ApJ*, 900, 1
- Gallerani, S., Pallottini, A., Feruglio, C., et al. 2018, *MNRAS*, 473, 1909
- Ginolfi, M., Jones, G. C., Béthermin, M., et al. 2020a, *A&A*, 643, A7
- Ginolfi, M., Jones, G. C., Béthermin, M., et al. 2020b, *A&A*, 633, A90
- Goldsmith, P. F., Langer, W. D., Pineda, J. L., & Velusamy, T. 2012, *ApJS*, 203, 13
- Grogan, N. A., Kocevski, D. D., Faber, S. M., et al. 2011, *ApJS*, 197, 35
- Gullberg, B., Swinbank, A. M., Smail, I., et al. 2018, *ApJ*, 859, 12
- Gurman, A., Hu, C.-Y., Sternberg, A., & van Dishoeck, E. F. 2024, *ApJ*, 965, 179
- Harikane, Y., Ouchi, M., Shibuya, T., et al. 2018, *ApJ*, 859, 84
- Harikane, Y., Ouchi, M., Inoue, A. K., et al. 2020, *ApJ*, 896, 93
- Hashimoto, T., Ouchi, M., Shimasaku, K., et al. 2013, *ApJ*, 765, 70
- Hashimoto, T., Inoue, A. K., Mawatari, K., et al. 2019, *PASJ*, 71, 71
- Heintz, K. E., Watson, D., Oesch, P. A., Narayanan, D., & Madden, S. C. 2021, *ApJ*, 922, 147
- Heintz, K. E., Oesch, P. A., Aravena, M., et al. 2022, *ApJ*, 934, L27
- Herrera-Camus, R., Bolatto, A. D., Wolfire, M. G., et al. 2015, *ApJ*, 800, 1
- Herrera-Camus, R., Sturm, E., Graciá-Carpio, J., et al. 2018a, *ApJ*, 861, 94
- Herrera-Camus, R., Sturm, E., Graciá-Carpio, J., et al. 2018b, *ApJ*, 861, 95
- Herrera-Camus, R., Förster Schreiber, N., Genzel, R., et al. 2021, *A&A*, 649, A31
- Hollenbach, D. J., & Tielens, A. G. G. M. 1999, *Rev. Mod. Phys.*, 71, 173
- Izumi, T., Matsuoka, Y., Fujimoto, S., et al. 2021a, *ApJ*, 914, 36
- Izumi, T., Onoue, M., Matsuoka, Y., et al. 2021b, *ApJ*, 908, 235
- Jones, G. C., Béthermin, M., Fudamoto, Y., et al. 2020, *MNRAS*, 491, L18
- Jones, G. C., Maiolino, R., Circosta, C., et al. 2023, *MNRAS*, 518, 691
- Jones, G. C., Bunker, A. J., Telikova, K., et al. 2024, ArXiv e-prints [arXiv:2405.12955]
- Kapala, M. J., Sandstrom, K., Groves, B., et al. 2015, *ApJ*, 798, 24
- Katz, H., Kimm, T., Sijacki, D., & Haehnelt, M. G. 2017, *MNRAS*, 468, 4831
- Kennicutt, R. C., Jr 1998, *ApJ*, 498, 541
- Kohandel, M., Pallottini, A., Ferrara, A., et al. 2024, *A&A*, 685, A72
- Kramer, C., Abreu-Vicente, J., García-Burillo, S., et al. 2013, *A&A*, 553, A114
- Lagache, G., Cousin, M., & Chatzikos, M. 2018, *A&A*, 609, A130
- Lambert, T. S., Posses, A., Aravena, M., et al. 2023, *MNRAS*, 518, 3183
- Langer, W. D., Velusamy, T., Pineda, J. L., Willacy, K., & Goldsmith, P. F. 2014, *A&A*, 561, A122
- Lapham, R. C., Young, L. M., & Crocker, A. 2017, *ApJ*, 840, 51
- Le Fèvre, O., Béthermin, M., Faisst, A., et al. 2020, *A&A*, 643, A1
- Levy, R. C., Bolatto, A. D., Tarantino, E., et al. 2023, *ApJ*, 958, 109
- Li, J., Da Cunha, E., González-López, J., et al. 2024, *ApJ*, 976, 70
- Liang, L., Feldmann, R., Murray, N., et al. 2024, *MNRAS*, 528, 499
- Lines, N. E. P., Bowler, R. A. A., Adams, N. J., et al. 2024, ArXiv e-prints [arXiv:2409.10963]
- Litke, K. C., Marrone, D. P., Spilker, J. S., et al. 2019, *ApJ*, 870, 80
- Madden, S. C., Poglitsch, A., Geis, N., Stacey, G. J., & Townes, C. H. 1997, *ApJ*, 483, 200
- Madden, S. C., Cormier, D., Hony, S., et al. 2020, *A&A*, 643, A141
- Malhotra, S., Kaufman, M. J., Hollenbach, D., et al. 2001, *ApJ*, 561, 766
- Martí-Vidal, I., Vlemmings, W. H. T., Muller, S., & Casey, S. 2014, *A&A*, 563, A136
- Matharu, J., Nelson, E. J., Brammer, G., et al. 2024, *A&A*, 690, A64
- Mitsuhashi, I., Tadaki, K.-I., Ikeda, R., et al. 2024, *A&A*, 690, A197
- Momcheva, I. G., van Dokkum, P. G., van der Wel, A., et al. 2017, *PASP*, 129, 015004
- Muñoz, J. A., & Oh, S. P. 2016, *MNRAS*, 463, 2085
- Muñoz-Elgueta, N., Arrigoni Battaia, F., Kauffmann, G., et al. 2024, *A&A*, 690, A392
- Nagamine, K., Wolfe, A. M., & Hernquist, L. 2006, *ApJ*, 647, 60
- Nakajima, K., Ouchi, M., Isobe, Y., et al. 2023, *ApJS*, 269, 33
- Nelson, E., Brammer, G., Giménez-Arteaga, C., et al. 2024, *ApJ*, 976, L27
- Nianias, J., Lim, J., & Yeung, M. 2024, *ApJ*, 963, 19
- Novak, M., Venemans, B. P., Walter, F., et al. 2020, *ApJ*, 904, 131
- Olsen, K., Greve, T. R., Narayanan, D., et al. 2018, *ApJ*, 857, 148
- Pallottini, A., Ferrara, A., Bovino, S., et al. 2017, *MNRAS*, 471, 4128
- Pallottini, A., Ferrara, A., Gallerani, S., et al. 2022, *MNRAS*, 513, 5621
- Parlanti, E., Carniani, S., Venturi, G., et al. 2024, *A&A*, submitted [arXiv:2407.19008]
- Pavesi, R., Riechers, D. A., Capak, P. L., et al. 2016, *ApJ*, 832, 151
- Peng, C. Y., Ho, L. C., Impey, C. D., & Rix, H.-W. 2002, *AJ*, 124, 266
- Peterson, B. W., Appleton, P. N., Bitsakis, T., et al. 2018, *ApJ*, 855, 141
- Pineda, J. L., Langer, W. D., Velusamy, T., & Goldsmith, P. F. 2013, *A&A*, 554, A103
- Pineda, J. L., Langer, W. D., & Goldsmith, P. F. 2014, *A&A*, 570, A121
- Pizzati, E., Ferrara, A., Pallottini, A., et al. 2020, *MNRAS*, 495, 160
- Pizzati, E., Ferrara, A., Pallottini, A., et al. 2023, *MNRAS*, 519, 4608
- Popping, G., Narayanan, D., Somerville, R. S., Faisst, A. L., & Krumholz, M. R. 2019, *MNRAS*, 482, 4906
- Posses, A. C., Aravena, M., González-López, J., et al. 2023, *A&A*, 669, A46
- Posses, A., Aravena, M., González-López, J., et al. 2024, *A&A*, submitted [arXiv:2403.03379]

- Pozzi, F., Calura, F., D'Amato, Q., et al. 2024, *A&A*, **686**, A187
- Ramos Padilla, A. F., Wang, L., van der Tak, F. F. S., & Trager, S. C. 2023, *A&A*, **679**, A131
- Reach, W. T., Fadda, D., Rand, R. J., & Stacey, G. J. 2020, *ApJ*, **902**, 28
- Riechers, D. A., Carilli, C. L., Capak, P. L., et al. 2014, *ApJ*, **796**, 84
- Romano, M., Nanni, A., Donevski, D., et al. 2023, *A&A*, **677**, A44
- Romano, M., Donevski, D., Junais, J., et al. 2024, *A&A*, **683**, L9
- Salak, D., Hashimoto, T., Inoue, A. K., et al. 2024, *ApJ*, **962**, 1
- Schaerer, D., Ginolfi, M., Béthermin, M., et al. 2020, *A&A*, **643**, A3
- Smirnova-Pinchukova, I., Husemann, B., Busch, G., et al. 2019, *A&A*, **626**, L3
- Smith, J. D. T., Croxall, K., Draine, B., et al. 2017, *ApJ*, **834**, 5
- Solimano, M., González-López, J., Aravena, M., et al. 2024, *A&A*, **689**, A145
- Spilker, J. S., Phadke, K. A., Aravena, M., et al. 2020, *ApJ*, **905**, 85
- Stacey, G. J., Geis, N., Genzel, R., et al. 1991, *ApJ*, **373**, 423
- Stacey, G. J., Hailey-Dunsheath, S., Ferkinhoff, C., et al. 2010, *ApJ*, **724**, 957
- Sugahara, Y., Ouchi, M., Harikane, Y., et al. 2019, *ApJ*, **886**, 29
- Sutter, J., Dale, D. A., Croxall, K. V., et al. 2019, *ApJ*, **886**, 60
- Tacconi, L. J., Genzel, R., & Sternberg, A. 2020, *ARA&A*, **60**, 157
- Tadaki, K.-I., Belli, S., Burkert, A., et al. 2020, *ApJ*, **901**, 74
- Tarantino, E., Bolatto, A. D., Herrera-Camus, R., et al. 2021, *ApJ*, **915**, 92
- Telikova, K., González-López, J., Aravena, M., et al. 2024, *A&A*, submitted [arXiv:2411.09033]
- Übler, H., D'Eugenio, F., Perna, M., et al. 2024, *MNRAS*, **533**, 4287
- Umehata, H., Matsuda, Y., Tamura, Y., et al. 2017, *ApJ*, **834**, L16
- Umehata, H., Smail, I., Steidel, C. C., et al. 2021, *ApJ*, **918**, 69
- Valentino, F., Brammer, G., Fujimoto, S., et al. 2022, *ApJ*, **929**, L9
- Vallini, L., Gallerani, S., Ferrara, A., & Baek, S. 2013, *MNRAS*, **433**, 1567
- Vallini, L., Gallerani, S., Ferrara, A., Pallottini, A., & Yue, B. 2015, *ApJ*, **813**, 36
- Veilleux, S., Maiolino, R., Bolatto, A. D., & Aalto, S. 2020, *A&ARv*, **28**, 2
- Venemans, B. P., Walter, F., Neeleman, M., et al. 2020, *ApJ*, **904**, 130
- Villanueva, V., Herrera-Camus, R., González-López, J., et al. 2024, *A&A*, **691**, A133
- Virtanen, P., Gommers, R., Oliphant, T. E., et al. 2020, *Nat. Methods*, **17**, 261
- Vizgan, D., Greve, T. R., Olsen, K. P., et al. 2022a, *ApJ*, **929**, 92
- Vizgan, D., Heintz, K. E., Greve, T. R., et al. 2022b, *ApJ*, **939**, L1
- Walter, F., Carilli, C., Neeleman, M., et al. 2020, *ApJ*, **902**, 111
- Wang, F., Yang, J., Fan, X., et al. 2024, *ApJ*, **968**, 9
- Wolfire, M. G., Vallini, L., & Chevance, M. 2022, *ARA&A*, **60**, 247
- Wong, Y. H. V., Wang, P., Hashimoto, T., et al. 2022, *ApJ*, **929**, 161
- Zanella, A., Daddi, E., Magdis, G., et al. 2018, *MNRAS*, **481**, 1976
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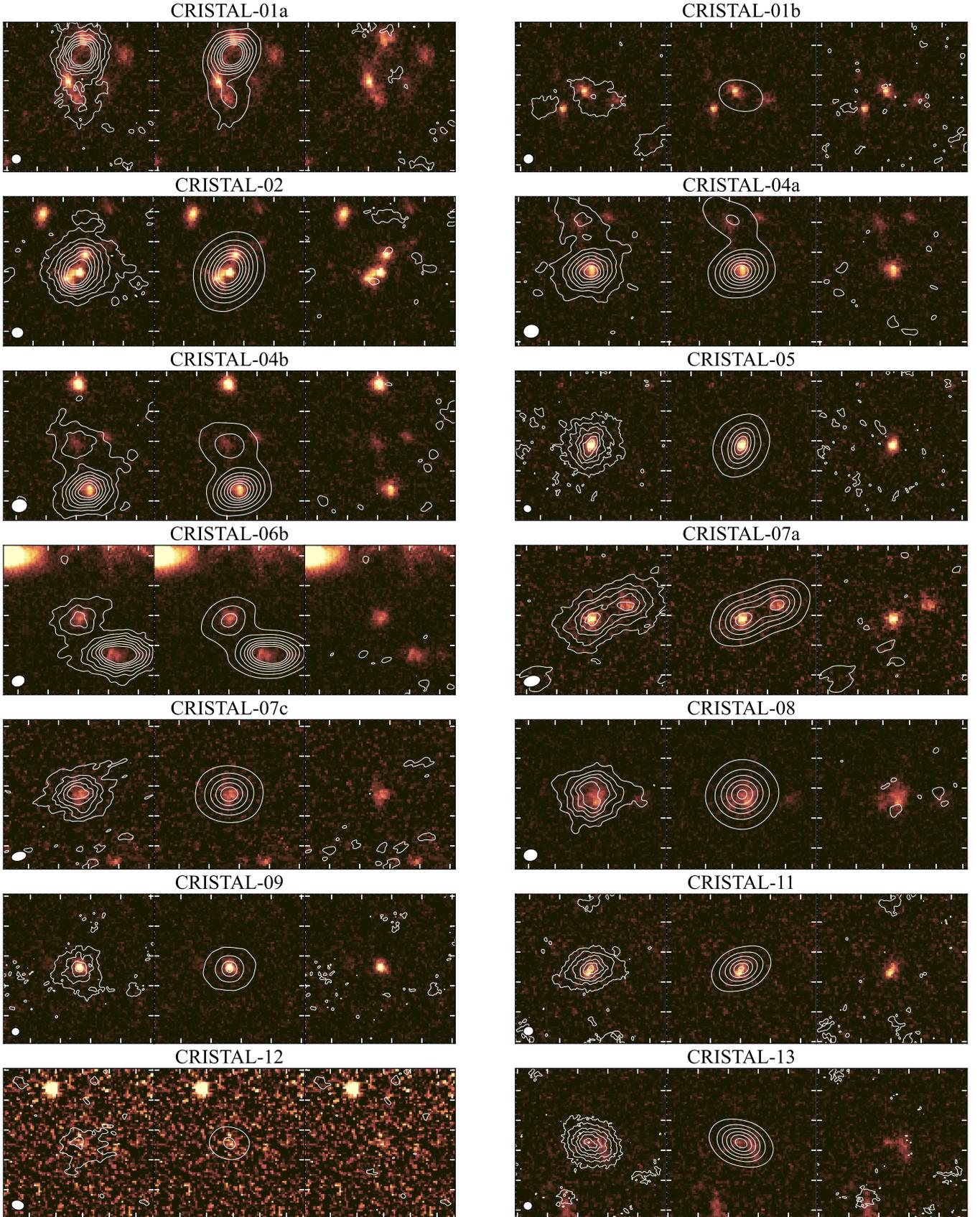
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## Appendix A: The sample name and postage stamps of the fit images

**Table A.1.** Other names and references of the CRISTAL galaxies.

ID	Other names	Ref.
CRISTAL-01a	DC842313	1
CRISTAL-01b	–	–
CRISTAL-02	DC848185, HZ6, LBG-1	1, 2, 3
CRISTAL-03	DC536534, HZ1	1, 2
CRISTAL-04a	vc5100822662, DC514583	1
CRISTAL-04b	vc5100822662, DC514583	1
CRISTAL-05	DC683613, HZ3	1, 2
CRISTAL-06a	vc5100541407	1
CRISTAL-06b	vc5100541407	1
CRISTAL-07a	DC873321, HZ8	1,2
CRISTAL-07b	DC873321, HZ8W	1,2
CRISTAL-07c	–	–
CRISTAL-08	ve530029038, CG15	1
CRISTAL-09	DC519281	1
CRISTAL-10	DC417567, HZ2	1, 2
CRISTAL-11	DC630594	1
CRISTAL-12	CG21	1
CRISTAL-13	vc5100994794	1
CRISTAL-14	DC709575	1
CRISTAL-15	vc5101244930	1
CRISTAL-16	CG38	1
CRISTAL-17	DC742174	1
CRISTAL-18	vc5101288969, DC679410	1
CRISTAL-19	DC494763	1
CRISTAL-20	DC494057, HZ4	1, 2
CRISTAL-21	HZ7	1
CRISTAL-22a	HZ10, HZ10-C	2, 4
CRISTAL-22b	HZ10, HZ10-W	2, 4
CRISTAL-23a	DC818760	1
CRISTAL-23b	DC818760	1
CRISTAL-23c	–	–
CRISTAL-24	DC873756	1
CRISTAL-25	vc5101218326	1

**References.** 1. Béthermin et al. (2020); 2. Capak et al. (2015); 3. Riechers et al. (2014); 4. Villanueva et al. (2024).



**Fig. A.1.** Visualization of the visibility modeling of the [C II] line emission in images. The [C II] line contours are overlaid on the HST/WFC3 F160W image. The left panel shows the dirty image of a single cube used for the visibility modeling (Section 3.2). The FWHM of the dirty beam is shown as a white ellipse in the lower-left corner. The middle and right panel show the best-fit model and the residual created by subtracting the model from the data, respectively. A  $5'' \times 5''$  region is shown. The contours start at  $2\sigma$  and increase in steps of  $3\sigma$  until  $20\sigma$ .

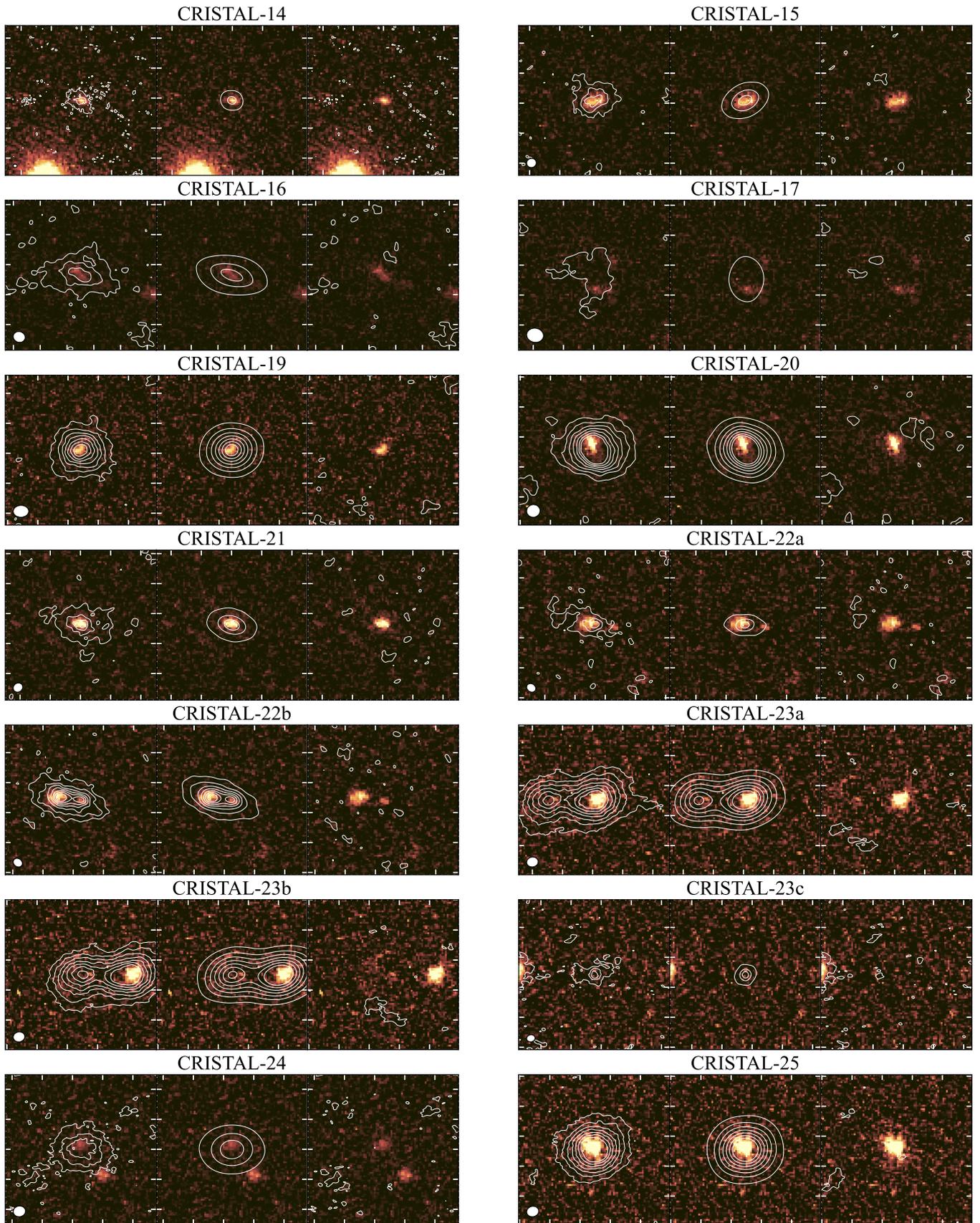


Fig. A.2. continued.

## Appendix B: Structural parameters of the CRISTAL galaxies

**Table B.1.** Structural parameters of [C II] line emission in the CRISTAL galaxies.

ID	R.A.	Decl.	$I_{[\text{CII}]}$ (Jy km/s)	$\Delta v^{(a)}$ (km/s)	$R_{e,[\text{CII}]}$ (kpc)	$q_{[\text{CII}]}$	PA <sub>[CII]</sub> (deg)	$\log_{10}(L_{[\text{CII}]} / L_{\odot})$
CRISTAL-01a	10:00:54.508	2:34:34.46	0.68 ± 0.16	789	3.05 ± 1.19	0.59 ± 0.27	21 ± 24	8.62 <sup>+0.09</sup> <sub>-0.12</sub>
CRISTAL-01b	10:00:54.778	2:34:28.27	0.67 ± 0.13	376	2.40 ± 0.92	0.44 ± 0.22	67 ± 15	8.62 <sup>+0.08</sup> <sub>-0.09</sub>
CRISTAL-02	10:00:21.499	2:35:11.01	2.63 ± 0.16	533	2.58 ± 0.28	0.52 ± 0.07	153 ± 5	9.31 <sup>+0.03</sup> <sub>-0.03</sub>
CRISTAL-03	9:59:53.254	2:07:05.40	0.44 ± 0.05	490	1.33 ± 0.47	0.81 ± 0.34	90 ± 54	8.59 <sup>+0.04</sup> <sub>-0.05</sub>
CRISTAL-04a	9:58:57.907	2:04:51.36	0.94 ± 0.07	308	1.76 ± 0.36	0.90 ± 0.21	50 ± 66	8.76 <sup>+0.03</sup> <sub>-0.04</sub>
CRISTAL-04b	9:58:57.928	2:04:52.85	0.32 ± 0.07	129	3.37 ± 1.27	0.74 ± 0.31	57 ± 42	8.30 <sup>+0.09</sup> <sub>-0.12</sub>
CRISTAL-05	10:00:09.422	2:20:13.84	0.94 ± 0.08	523	1.57 ± 0.28	0.31 ± 0.08	160 ± 5	8.90 <sup>+0.03</sup> <sub>-0.04</sub>
CRISTAL-06a W	10:01:00.894	1:48:33.66	0.89 ± 0.07	298	1.49 ± 0.22	0.50 ± 0.08	94 ± 6	8.74 <sup>+0.03</sup> <sub>-0.03</sub>
CRISTAL-06a E	10:01:00.940	1:48:33.81	0.44 ± 0.06	298	1.23 ± 0.22	–	–	8.44 <sup>+0.06</sup> <sub>-0.07</sub>
CRISTAL-06b	10:01:00.999	1:48:34.85	0.52 ± 0.07	332	2.63 ± 0.66	0.71 ± 0.20	123 ± 23	8.51 <sup>+0.06</sup> <sub>-0.06</sub>
CRISTAL-07a	10:00:04.058	2:37:35.84	0.49 ± 0.09	325	1.84 ± 0.64	0.89 ± 0.39	0 ± 13	8.57 <sup>+0.07</sup> <sub>-0.09</sub>
CRISTAL-07b	10:00:03.974	2:37:36.36	0.50 ± 0.08	351	1.95 ± 0.71	0.73 ± 0.31	67 ± 40	8.58 <sup>+0.07</sup> <sub>-0.08</sub>
CRISTAL-07c	10:00:03.223	2:37:37.75	1.56 ± 0.15	413	2.51 ± 0.45	0.74 ± 0.15	70 ± 19	9.07 <sup>+0.04</sup> <sub>-0.04</sub>
CRISTAL-08	3:32:19.044	-27:52:38.21	1.35 ± 0.12	320	3.47 ± 0.47	0.74 ± 0.12	8 ± 15	8.91 <sup>+0.04</sup> <sub>-0.04</sub>
CRISTAL-09	9:59:00.893	2:05:27.57	0.56 ± 0.07	518	0.87 ± 0.41	0.78 ± 0.46	13 ± 66	8.67 <sup>+0.05</sup> <sub>-0.06</sub>
CRISTAL-10	10:02:04.134	1:55:44.30	0.51 ± 0.07	386	2.49 ± 0.71	0.73 ± 0.23	122 ± 29	8.65 <sup>+0.06</sup> <sub>-0.07</sub>
CRISTAL-11	10:00:32.598	2:15:28.44	1.05 ± 0.11	529	1.44 ± 0.43	0.65 ± 0.23	105 ± 23	8.80 <sup>+0.04</sup> <sub>-0.05</sub>
CRISTAL-12	3:32:11.943	-27:41:57.44	0.10 ± 0.03	224	1.19 ± 0.89	0.53 ± 0.54	18 ± 44	7.93 <sup>+0.10</sup> <sub>-0.14</sub>
CRISTAL-13	10:00:41.171	2:17:14.24	0.95 ± 0.09	382	1.61 ± 0.39	0.47 ± 0.15	63 ± 11	8.78 <sup>+0.04</sup> <sub>-0.04</sub>
CRISTAL-14	9:59:47.068	2:22:32.92	0.35 ± 0.07	534	0.75 ± 0.24	–	–	8.31 <sup>+0.08</sup> <sub>-0.10</sub>
CRISTAL-15	10:00:47.657	2:18:02.09	0.44 ± 0.08	540	1.43 ± 0.87	0.47 ± 0.27	116 ± 20	8.44 <sup>+0.07</sup> <sub>-0.09</sub>
CRISTAL-16	3:32:15.899	-27:41:24.36	0.33 ± 0.06	445	1.39 ± 0.83	0.17 ± 0.13	68 ± 7	8.44 <sup>+0.07</sup> <sub>-0.08</sub>
CRISTAL-17	10:00:39.132	2:25:32.66	0.10 ± 0.04	312	2.13 ± 1.33	–	–	7.95 <sup>+0.15</sup> <sub>-0.24</sub>
CRISTAL-19	10:00:05.105	2:03:12.10	0.64 ± 0.05	497	1.48 ± 0.48	0.86 ± 0.24	158 ± 50	8.69 <sup>+0.03</sup> <sub>-0.04</sub>
CRISTAL-20	9:58:28.503	2:03:06.56	0.94 ± 0.04	330	1.80 ± 0.21	0.57 ± 0.07	25 ± 6	8.89 <sup>+0.02</sup> <sub>-0.02</sub>
CRISTAL-21	9:59:30.466	2:08:02.62	0.77 ± 0.12	422	1.62 ± 0.61	0.46 ± 0.17	76 ± 12	8.77 <sup>+0.06</sup> <sub>-0.07</sub>
CRISTAL-22a	10:00:59.291	1:33:19.43	4.91 ± 0.87	1032	0.91 ± 0.58	0.40 ± 0.22	107 ± 14	9.63 <sup>+0.07</sup> <sub>-0.08</sub>
CRISTAL-22b	10:00:59.250	1:33:19.42	1.66 ± 0.25	924	0.93 ± 0.25	0.49 ± 0.15	80 ± 11	9.16 <sup>+0.06</sup> <sub>-0.07</sub>
CRISTAL-23a	10:01:54.863	2:32:31.52	4.66 ± 0.27	462	2.87 ± 0.31	0.76 ± 0.08	113 ± 11	9.46 <sup>+0.02</sup> <sub>-0.03</sub>
CRISTAL-23b	10:01:54.970	2:32:31.51	2.77 ± 0.27	442	2.45 ± 0.43	0.82 ± 0.15	123 ± 28	9.24 <sup>+0.04</sup> <sub>-0.04</sub>
CRISTAL-23c	10:01:54.682	2:32:31.42	0.66 ± 0.11	465	0.52 ± 0.18	–	–	8.62 <sup>+0.07</sup> <sub>-0.08</sub>
CRISTAL-24	10:00:02.715	2:37:39.99	14.76 ± 2.50	1291	3.00 ± 1.03	0.74 ± 0.25	92 ± 31	9.96 <sup>+0.07</sup> <sub>-0.08</sub>
CRISTAL-25	10:01:12.502	2:18:52.55	3.35 ± 0.19	477	2.45 ± 0.35	0.65 ± 0.10	35 ± 10	9.32 <sup>+0.02</sup> <sub>-0.03</sub>

**Notes.** (a) Velocity range containing 95% (= [2.5%, 97.5%]) of the total [C II] line flux. To convert to the 80% (= [10%, 90%]) velocity range, it is necessary to apply a multiplication factor of 0.654.

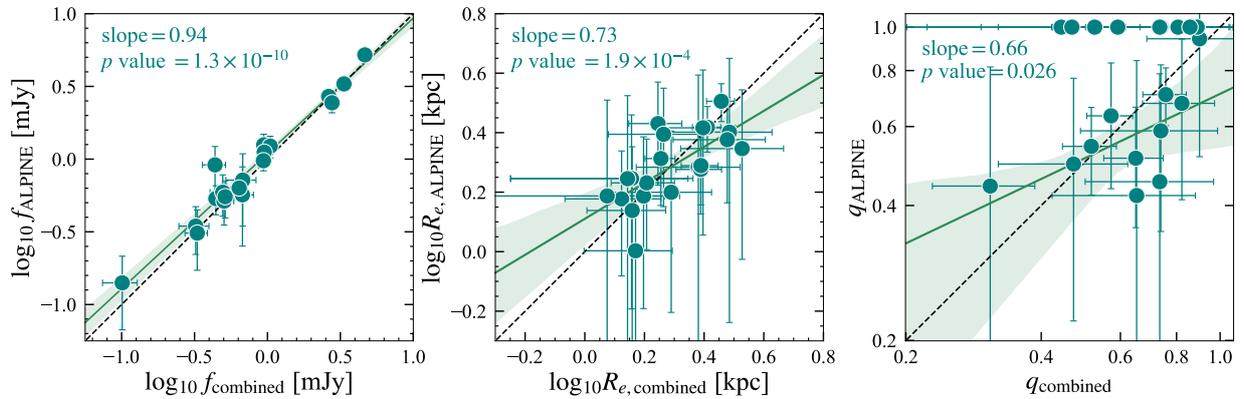
**Table B.2.** Effective radii and size ratios in continuum emission.

ID	$R_{e,UV}$ (kpc)	$R_{e,FIR}$ (kpc)	$R_{e,[CII]}/R_{e,UV}$	$R_{e,[CII]}/R_{e,FIR}$	Class.
CRISTAL-01a	$1.02 \pm 0.06$	–	$3.0 \pm 1.2$	–	multi-UV
CRISTAL-01b	$0.63 \pm 0.05$	$2.18 \pm 1.01$	$3.8 \pm 1.5$	$1.1 \pm 0.7$	multi-UV
CRISTAL-02	–	$1.99 \pm 0.46$	–	$1.3 \pm 0.3$	multi-UV
CRISTAL-03	$1.02 \pm 0.05$	–	$1.3 \pm 0.5$	–	single
CRISTAL-04a	$1.01 \pm 0.05$	$0.86 \pm 0.47$	$1.7 \pm 0.4$	$2.1 \pm 1.2$	pair
CRISTAL-04b	$0.96 \pm 0.14$	–	$3.5 \pm 1.4$	–	pair
CRISTAL-05	$0.36 \pm 0.04$	$1.45 \pm 0.63$	$4.3 \pm 0.9$	$1.1 \pm 0.5$	single
CRISTAL-06a W	–	$2.03 \pm 0.47$	–	$0.7 \pm 0.2$	multi-[C II]
CRISTAL-06a E	–	–	–	–	multi-[C II]
CRISTAL-06b	$1.25 \pm 0.07$	–	$2.1 \pm 0.5$	–	pair
CRISTAL-07a	$0.90 \pm 0.06$	$1.24 \pm 0.95$	$2.0 \pm 0.7$	$1.5 \pm 1.2$	pair
CRISTAL-07b	$1.51 \pm 0.13$	–	$1.3 \pm 0.5$	–	pair
CRISTAL-07c	$0.88 \pm 0.11$	$0.86 \pm 0.48$	$2.8 \pm 0.6$	$2.9 \pm 1.7$	single
CRISTAL-08	$2.53 \pm 0.09$	–	$1.4 \pm 0.2$	–	single
CRISTAL-09	$0.17 \pm 0.05$	$0.62 \pm 0.47$	$5.2 \pm 3.0$	$1.4 \pm 1.3$	single
CRISTAL-10	–	$2.38 \pm 1.33$	–	$1.0 \pm 0.7$	multi-UV
CRISTAL-11	$0.44 \pm 0.16$	$0.77 \pm 0.60$	$3.3 \pm 1.5$	$1.9 \pm 1.6$	single
CRISTAL-12	–	–	–	–	single
CRISTAL-13	–	$0.60 \pm 0.46$	–	$2.7 \pm 2.1$	multi-UV
CRISTAL-14	–	–	–	–	single
CRISTAL-15	–	–	–	–	single
CRISTAL-16	$1.49 \pm 0.14$	–	$0.9 \pm 0.6$	–	single
CRISTAL-17	–	–	–	–	single
CRISTAL-19	$0.60 \pm 0.11$	$1.61 \pm 0.94$	$2.5 \pm 0.9$	$0.9 \pm 0.6$	single
CRISTAL-20	$0.36 \pm 0.06$	$1.50 \pm 0.32$	$5.0 \pm 1.0$	$1.2 \pm 0.3$	single
CRISTAL-21	$0.38 \pm 0.06$	$7.11 \pm 3.06$	$4.3 \pm 1.7$	$0.2 \pm 0.1$	single
CRISTAL-22a	$0.76 \pm 0.07$	$0.88 \pm 0.06$	$1.2 \pm 0.8$	$1.0 \pm 0.7$	pair
CRISTAL-22b	–	–	–	–	pair
CRISTAL-23a	$0.60 \pm 0.04$	$3.19 \pm 0.61$	$4.8 \pm 0.6$	$0.9 \pm 0.2$	pair
CRISTAL-23b	–	–	–	–	pair
CRISTAL-23c	–	–	–	–	single
CRISTAL-24	$0.69 \pm 0.26$	$1.34 \pm 0.18$	$4.4 \pm 2.2$	$2.2 \pm 0.8$	single
CRISTAL-25	$0.86 \pm 0.03$	$2.10 \pm 0.76$	$2.9 \pm 0.4$	$1.2 \pm 0.5$	single

### Appendix C: Visibility modeling with the ALPINE data

In this section, we briefly discuss how our visibility modeling improved by adding the data taken from the CRISTAL survey. In Table C.1, we show the results of visibility modeling using the ALPINE data alone. We followed the same procedure described in Section 3.2. Out of the 33 [C II] components reported in this work, the ALPINE data was used for 24 components, and we have successfully modeled 21 components. The fittings did not converge for the rest of the three components, either due to the compactness or faintness of the [C II] line emission. Some of the merging systems (e.g., CRISTAL-04a and CRISTAL-04b pair) were able to be modeled as two distinct galaxies if we allow a circular exponential model.

Figure C.1 compares the fit values between two different datasets. A slope and  $p$  value based on a linear regression fitting are shown. For the linear regression fitting of the minor-to-major axis ratios, we exclude the galaxies for which the minor-to-major axis ratio is unconstrained by the ALPINE data ( $q_{\text{ALPINE}} = 1$ ). We find that all three correlations (total flux, effective radius, and minor-to-major axis ratio) show a good agreement with the  $p$  value smaller than 0.05, demonstrating that the ALPINE data alone could constrain three parameters well. However, the uncertainties of flux and radius become on average 2.1 and 1.8 times smaller, respectively, when the CRISTAL data is included. One major improvement is that we have successfully constrained the minor-to-major axis ratio for more than 90% of the sample, while less than half cannot be modeled when only low-resolution data is used. This could be either due to the difference in the sensitivities or the spatial resolutions of the data.



**Fig. C.1.** Comparison of total flux (left), effective radius (middle), and axis ratio (right) measured from the visibility modeling using different datasets. A slope and  $p$  value based on a linear regression fitting are shown in the top-left corner of each panel. We exclude the galaxies with  $q_{\text{ALPINE}} = 1$  for the fitting of minor-to-major axis ratio.

**Table C.1.** Structural parameters of the [C II] line emission measured from the ALPINE data alone.

ID	$I_{[\text{CII}]}$ (Jy km/s)	$R_{e,[\text{CII}]}$ (kpc)	$q_{[\text{CII}]}$	$\text{PA}_{[\text{CII}]}$ (deg)
CRISTAL-01a	$0.72 \pm 0.37$	$2.52 \pm 1.94$	–	–
CRISTAL-01b	$0.57 \pm 0.32$	$1.92 \pm 2.00$	–	–
CRISTAL-02	$2.70 \pm 0.24$	$2.62 \pm 0.46$	$0.54 \pm 0.12$	$156 \pm 9$
CRISTAL-03	$0.54 \pm 0.12$	$1.50 \pm 0.68$	–	–
CRISTAL-04a	$1.25 \pm 0.23$	$2.70 \pm 1.02$	$0.94 \pm 0.43$	$51 \pm 226$
CRISTAL-04b	$0.35 \pm 0.12$	$2.22 \pm 1.28$	–	–
CRISTAL-05	$1.01 \pm 0.18$	$1.54 \pm 0.89$	$0.44 \pm 0.37$	$146 \pm 25$
CRISTAL-07a	$0.59 \pm 0.19$	$2.48 \pm 1.06$	–	–
CRISTAL-07b	$0.51 \pm 0.16$	$1.58 \pm 0.96$	–	–
CRISTAL-09a	–	–	–	–
CRISTAL-10	$0.55 \pm 0.16$	$2.61 \pm 1.47$	$0.45 \pm 0.34$	$163 \pm 23$
CRISTAL-11	$1.23 \pm 0.21$	$1.38 \pm 0.88$	$0.42 \pm 0.42$	$83 \pm 24$
CRISTAL-12	$0.14 \pm 0.07$	$1.54 \pm 1.69$	–	–
CRISTAL-13	$1.12 \pm 0.17$	$1.70 \pm 0.69$	$0.49 \pm 0.27$	$63 \pm 19$
CRISTAL-14	–	–	–	–
CRISTAL-15	$0.91 \pm 0.31$	$1.76 \pm 1.12$	–	–
CRISTAL-16	$0.31 \pm 0.14$	$1.76 \pm 1.59$	–	–
CRISTAL-17	–	–	–	–
CRISTAL-19	$0.63 \pm 0.11$	$1.01 \pm 0.61$	–	–
CRISTAL-20	$0.97 \pm 0.10$	$2.06 \pm 0.63$	$0.63 \pm 0.20$	$37 \pm 18$
CRISTAL-23a	$5.21 \pm 0.42$	$3.20 \pm 0.47$	$0.71 \pm 0.10$	$115 \pm 13$
CRISTAL-23b	$2.44 \pm 0.36$	$1.89 \pm 0.55$	$0.68 \pm 0.26$	$149 \pm 27$
CRISTAL-24	$13.62 \pm 2.08$	$2.38 \pm 0.92$	$0.59 \pm 0.24$	$108 \pm 20$
CRISTAL-25	$3.29 \pm 0.23$	$1.95 \pm 0.51$	$0.51 \pm 0.15$	$33 \pm 10$