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Identification of metabolic pathways using pathfinding approaches: a systematic review

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Abstract

Metabolic pathways have become increasingly available for various microorganisms. Such pathways have spurred the development of a wide array of computational tools, in particular, mathematical pathfinding approaches. This article can facilitate the understanding of computational analysis of metabolic pathways in genomics. Moreover, stoichiometric and pathfinding approaches in metabolic pathway analysis are discussed. Three major types of studies are elaborated: stoichiometric identification models, pathway-based graph analysis and pathfinding approaches in cellular metabolism. Furthermore, evaluation of the outcomes of the pathways with mathematical benchmarking metrics is provided. This review would lead to better comprehension of metabolism behaviors in living cells, in terms of computed pathfinding approaches.

Key words: pathfinding algorithms; stoichiometric approaches; graph methods; metabolic pathways; identification

Introduction

Metabolism is a biological subsystem in cells, which is responsible for extracting the energy. The process of generating energy and necessary materials is considered as a highly complex cellular process. Enzymes play a critical role in catalyzing biochemical reactions within the cell [1–3]. Cooperatively, the reactions of these cellular machinery components produce energy metabolism. Metabolism integrates all parts of cells, and its study is important to understand the function of the system and furthermore, to understand alterations that occur in disease state, [4] and, hence, for subsequent applications in drug discovery [5]. Therefore, the reconstruction of genome-scale metabolic graph representation from genomics and other molecular or biochemical data is now feasible.

In biological research, one of the most important topics is identifying different metabolic pathways within species, which might be exposed to subtle shifts or malfunctions. Metabolism

has many important activities that can lead to finding the drug resistance of pathogenic bacteria. However, identifying a pathway in the laboratory is a complicated process. The process includes difficult subtasks such as metabolic flux analyses [6] and labeling techniques for dynamic metabolism profiling [7]. All these require advanced technologies, which are expensive and time consuming. Another direction is to make use of the qualified approach by comparing metabolic networks of related species. A shorter pathway might be preferred over a longer pathway because of the smaller number of enzymes required. This is both advantageous because the genome capacity is often limited and because the shortest pathway is more likely to be conserved in evolution. Hence, we classified these approaches into stoichiometric approaches and pathfinding approaches. Stoichiometric approaches, which underlie flux balance analysis (FBA) approach, elementary flux modes (EFMs) and extreme pathways (EPs), define a metabolic pathway as a minimal set of

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biochemical reactions in pseudo steady state. Pathfinding approaches view a metabolic pathway as a set of biochemical re-actions that contain a directed path from a given source com-pound to a given target compound [8–10].

However, pathfinding relies on a metabolism network where compounds and reactions are nodes linked by edges represent-ing substrate/product relationships [11–13]. Various algorithms can be used to the find single shortest path or k-shortest paths between a given pair of start and end nodes. Experimental find-ings on various organisms indicate that (despite the presence of many possible biochemically feasible pathways) organisms often have a single ‘preferred’ pathway when converting a source com-pound into a target compound [14]. However, this terminology is not unique, and many authors described these pathways using diverse terms, for instance, annotated pathway [15], consensus pathway [8], empirically elucidated pathway [16] and experimen-tally determined pathway [17]. Of course, it is important to note that from the physiological viewpoint, metabolism pathways do not operate in isolation, and many pathways work together to produce an overall global flux distribution in reactions. Much re-search has been proposed to analyze pathways based on graph models for identifying biologically relevant pathways in meta-bolic pathways [18]. Graph-based metabolism pathfinder algo-rithms complement stoichiometric approaches, as they focus on different aspects of modeling and understanding metabolism [19–21]. In addition, they are typically used for modeling specific organisms or metabolism systems [22]. Most models are based on the steady-state assumption and, therefore, require explicit labeling of internal and external compounds [23].

In recent years, there has been an increasing amount of lit-erature on the metabolic pathway model’s design. Some model design have problems with large-scale data for cell biology and the applications of graph theory [24]. The authors used compu-tational approaches to reconstruct the genome-scale metabolic models into numerical graphs. In this article, we discuss the main purpose of representing cell biology information in a mathematical graph model form. Moreover, to present biologic pathway data in a useful graph form, the characteristics and mechanisms of the inner workings of the cell must be con-sidered [25]. Although the pathway data sets have been col-lected worldwide through observations and experiments, there is still a lack of satisfying explanations and theories to give them sound biological meaning [26]. The varieties of data sets available have expanded from a handful in the mid-1990s to a several thousand today [27]. These data sets are categorized into main roots such as MetaCyc, KEGG, Reactome, Model SEED and BiGG families [28].

This systematic review focuses on two major points: first, it highlights the most relevant mathematical metabolism path-way models with pathfinding approaches; second, it exports the progress of pathfinding algorithms on metabolic pathways and illustrates the formalization and constraint rules. The rest of the article is organized as follows. Section 2 reviews the relevant previous surveys on metabolism, Section 3 briefly reviews the details of metabolic pathways, Section 4 reviews the pathfind-ing approaches, Section 5 validates the measurements for pathfinding approaches and Section 6 discusses the limitations and gaps in this area. The article is concluded in Section 7.

Stoichiometric approaches

There are two key distinctions between stoichiometric approaches and pathfinding approaches. First, the pathfinding approaches focus on searching a directed path within the metabolic pathway,

while stoichiometric approaches seek the complete pathway. Second, pathfinding approaches do not make direct use of reac-tion stoichiometry, while stoichiometric approaches do.

There are two main categories of stoichiometric approaches: flux balance analyses (FBAs) and EFMs. The FBA is a fundamen-tal computational framework applied to metabolic networks, derived from the steady-state assumption and mathematically defined metabolic pathways. The EFMs are based on analyzing metabolic networks from a pathway-oriented perspective.

FBA approach

FBA is a cornerstone in mathematical optimization methods for metabolic networks [29–32]. The main objective of this model is to achieve accuracy in the reaction metabolic network based on some conditions: First, the metabolic network must be complete and must fully cover the metabolic network capabilities to be ready for modeling. Second, the metabolic network should have no gaps or dead ends, and the representation of the metabolic network based on the metabolic phenotype of the organism must be correct. Typically, this objective function is the maxi-mization of the flux through the biomass formation reaction. Most experiments done for this approach use a mixed-integer linear program formulation [33], and with a variety of data sets such as KEGG pathway [34] and MetaCyc [35] as in Figure 1.

The most significant feature of FBA is its ability to make quantitative predictions without any need for detailed kinetic descriptions, needing only the stoichiometry of reactions. The network stoichiometry (metabolic model), a biological objective and the growth and environmental conditions (substrate avail-ability) are the only necessary inputs for FBA. One of the draw-backs of the FBA approach is that it is somewhat limited in its predictive power, unless additional constraints are appended to the optimization problem. This approach can be systematically extended into several techniques, such as regulatory FBA [36], steady-state regulatory FBA [37], gene inactivity moderated by metabolism and expression [38] and probabilistic regulation of metabolism [39], all of which have been developed to integrate regulatory information with the metabolic network.

The reason for using these models is to enable the mathemat-ical representation of the bio-transformations and metabolic processes occurring within the organism. Although a large num-ber of methodologies have been proposed, such as flux variability analysis, linear optimization for identifying the maximum bio-mass [40] and flux coupling analysis [41], constraints imply that not all fluxes in a metabolic network can vary independently.

Elementary flux modes

EFMs is a computational technique to analyze metabolic path-ways in metabolic networks [42–44]. EFMs can be defined as a minimal set of enzymes able to operate at a steady state, with the enzymes weighted by the relative flux they need to carry for the mode to function [9]. One significant aspect of EFM is that every flux distribution can be decomposed into a set of EFMs, and a number of the methods to study flux distributions origin-ate from it [45, 46]. Continuous efforts have been made to im-prove the computational speed and memory demand required to compute EFMs. Nonetheless, the distribution of any particu-lar steady-state flux can be represented as a nonnegative linear combination of elementary modes [47, 48].

In the metabolic network, the internal reversible reactions are decomposed into pairs of opposite irreversible reactions, where the corresponding flux cone is augmented and the run of

- The substrates $S \subseteq \mathcal{R}_1$ and target products $P \subseteq \mathcal{R}_1$ of a reaction r_1 are defined
- as $S_{r_j} = \{m_j | d_{ij} < 0\}$ and $P_{r_j} = \{m_j | d_{ij} > 0\}$, respectively.

A node $u_r \in V_R$ for each reaction, a node $u_m \in V_M$ for each sub-strate or product $m \in S \cup P$ of each reaction.

An edge $\delta_{u_r, u_m} \in E$ for producing metabolite m , and $\delta_{u_m, u_r} \in E$ for consuming m .

In a metabolic pathway graph context, a node to reaction or metabolite can be related. In reaction cases, reactions are represented as a directed graph G_R , and the edge $r_i, r_j \in E$ exists whenever $P_{r_i} \cap S_{r_j} \neq \emptyset$. In the metabolite case, metabolites are represented as a directed graph G_M and the edge $m_i, m_j \in E$ whenever $m_i \in S_{r_j}$ or $m_j \in P_{r_j}$ for some reactions.

Several graph-based methods have been proposed for searching and eventually enumerating pathways in metabolic networks, such as Pathfinding [20–22] and the Pathway Hunter Tool [59]. These methods are computing pathways and the shortest pathways in graphs compared with hyper-graphs. Practically, these methods concern only the main substrates (start compounds), and the main products (target compounds) are considered during construction of the pathways. In addition, these main compounds are unlike the cofactors such as co-substrates and co-products.

Subgraph based-metabolic pathway

A subgraph is represented as a subset of nodes with a specific set of edges connecting them, and the total number of subgraphs

exponentially depends on the set of nodes as in Figure 2B. Therefore, efficient and scalable heuristics are developed for detecting the given subgraphs and their frequencies in large meta-bolic networks. Many researchers mention that it is equally important to understand the organization of infrequently observed subgraphs [60–62].

In particular, the highest performance of pathfinding identification in a subgraph is through a sub-pathway mining module [63]. Substantially, the complex structure of metabolic pathways drives the sub-pathway to become a general problem. Generally, the metabolic pathways are represented as directed graphs, and the protein-to-protein interaction pathways are represented as undirected graphs. On the other hand, it is possible to identify the path based on enzymes, and subgraphs will be represented as un-directed graphs. The disadvantage of undirected subgraphs is that pathfinding approaches will not differentiate between reaction products and substrates [62, 64].

Bipartite graph-based-metabolic pathway

Recently, many researchers have analyzed the metabolic network by transforming the biochemical reactions into a bipartite graph, where the nodes and links take the form of metabolites and enzymatic reactions. Generally, a metabolic network consists of enzymes, reactions and metabolites. Based on a bipartite model graph, each enzyme is shared by two nodes, and

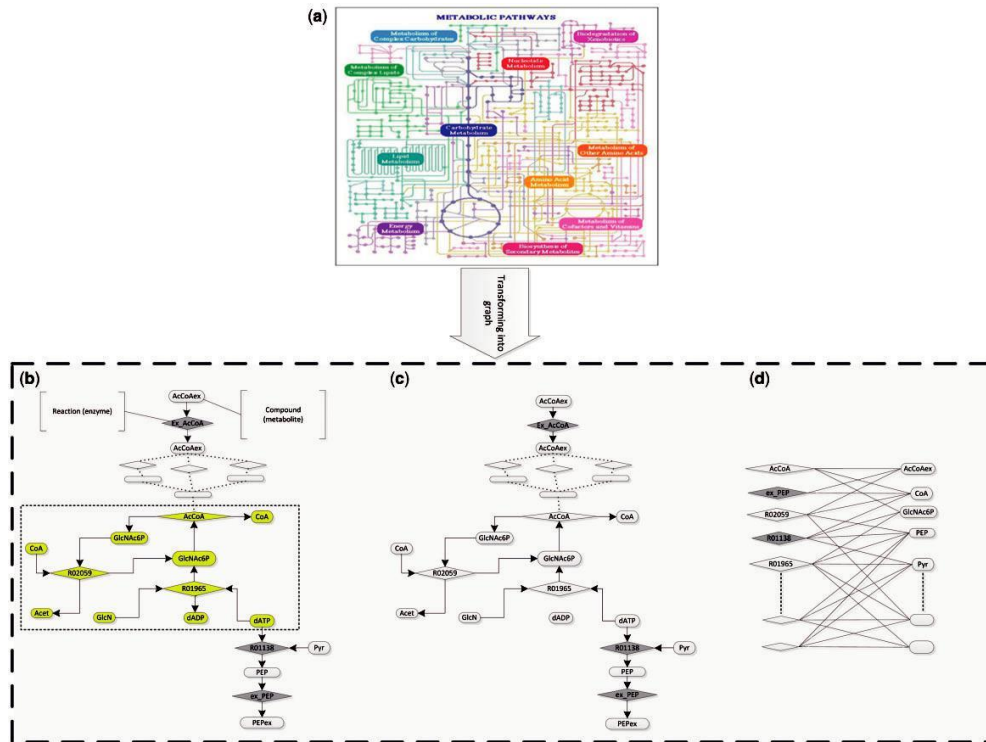


Figure 2. (A) A graph G is metabolic pathway for genome-scale, which consist set of compounds and reactions. (B) The yellow reactions and compounds represent sub-graph. (C) All chemical reactions and compounds in graph G represent the bipartite graph. (D) The hyper-graph, where each compound connects at least more than two reactions.

edges define the biological relationship between a set of metabolites and enzymes as in Figure 2C. However, this model graph only facilitates drug discovery and ranking of choke points and load points, and both points are used to find enzymes (edges), which uniquely consume or produce a particular metabolite (nodes) [65, 66].

There are online databases available as bipartite graphs, obtained from 43 different organisms, which were collected and published in recent studies [12, 67]. The bipartite graph has been used in some works related to pathfinding via the use of the metabolic data set KEGG [68]. RPAIR is a database from KEGG categorized into 'main', 'trans', 'cofac', 'ligase' and 'leave', depending on their roles in a chemical reaction [20].

Hyper-graph based-metabolic pathway

A hyper-graph is a generalization of an ordinary graph where an edge, called a hyper-edge, can connect more than two vertices [69], as in Figure 2D. The vertices in the hyper-graph are the compounds, and the hyper-edges are the reactions connecting the compounds. The metabolism of living cells can be represented using a metabolic network in the form of a directed hyper-graph that encodes a set of elementary biochemical reactions taking place within the cell. In this hyper-graph, the nodes represent the involved metabolites, and the edges represent the metabolic fluxes or reaction rates.

Identification of the most relevant pathways based on hyper-graphs have been proposed by [70]. The hyper-graph can model the metabolic network where the reactions are represented by hyper-arc. The hyper-arc will be used as an enzyme-catalyzed reaction, which in turn leads to transforming the set of substrates' compounds into product compounds [71]. In a hyper-graph, each hyper-arc connects a set of vertices, corresponding to reactants, to a disjoint set of vertices, representing the products. Each hyper-arc corresponds to a reaction that can be catalyzed by an enzyme. The hyper-graph models have already been used to find minimal sets of metabolites sufficient to produce a set of target metabolites [72].

Pathfinding approaches for metabolic pathway identification

An interactive navigation through metabolic networks is possible, given a set of biochemical reactions belonging to a particular organism or cell, by using different algorithms based on artificial intelligence to compute the meaningful metabolic pathways from a source compound to a target compound as in Figure 3. However, searching without information other than the connectivity (for example, two successive reactions are connected if they have a metabolite in common) often delivers meaningless results. Several pathfinding algorithms have been proposed, such as A* (A star), best-first search and depth-first-search (DFS; backtracking) [15, 57, 73–76]. Because the algorithms do not depend on predefined pathways, they can efficiently identify plausible routes using known biochemical transformations.

Metabolic networks in any living organism can be represented as a directed graph. Practically, to formalize the traveling cost in state-space, we need to define the difference between any two compounds as Dx . We denote a compound as x and state-space describe it by a set of chemical descriptors, x_k . Thus, every metabolite m can be placed at a point in hyper-space, which is defined by $x = (x_1, x_2, x_3 \dots x_n)$. The formulation $t = \sum Dx$, simply state-transition, and jDx_j , the distance, that can be

calculated using the Euclidean metric or the Manhattan metric are given in Equations (1) and (2), respectively. Both distance metrics (Euclidean or Manhattan) are heuristic functions H that always represent the shortest distance between any two compounds or reactions. However, the Manhattan distance is computationally more efficient than the Euclidean distance in terms of identifying the path in discrete chemical changes [73,

77]. Below are the general formalizations and constraints:

$$jDx_j = \sqrt{\sum_{k=0}^{k=N} Dx_k^2} \quad (1)$$

$$jDx_j = \sum_{k=0}^{k=N} Dx_k \quad (2)$$

Using metric distance to identify the shortest path leads to evaluation of the functions F , G and H , which are required for a heuristic search [78, 79]. F is the heuristic evaluation function, which can be calculated using different methods, G is the cost of reaching the current state to the initial state and H is the greedy search, which minimizes the cost of reaching the goal state from the current state.

By considering the hypothetical pathway as $p^0 \rightarrow x^1 \rightarrow \dots \rightarrow x^m \rightarrow x^L$, which begins with the initial state x^0 , ends with the final state x^L and has any intermediate state x^m , the total cost can be calculated by G and H at the intermediate state, x^m , as given in Equations (3) and (4), respectively.

$$G(0; m) = \sum_{i=0}^{i=m} x^i \quad (3)$$

$$H(m; L) = \sum_{j=m}^j x^L \quad (4)$$

For pathfinding algorithms, the main target is to identify the path with minimum total cost, $F = G + H$, as shown in Equation (5), where $G(0, m)$ is the actual distance through chemical transitions between x^0 to x^m , and $H(m, L)$ is 'estimation' for the shortest path to the target state x^L .

$$F(0; m; L) = G(0; m) + H(m; L) = \sum_{i=0}^{i=m} x^i + \sum_{j=m}^j x^L \quad (5)$$

The pathfinding approach based on a heuristic search can provide a series of efficient biochemical transformations that transform the start compound into a target compound. The heuristic function will monitor any chemical proximity for an intermediate compound to target compound. Equation (5) is used to evaluate and select the pathway that efficiently converts the input compound to the output compound. The efficiency of transforming is not based on the length of the path, but is determined by an optimal value of the heuristic function

F [73].

Identification-based-weighted pathway

Here, the metabolic network is described as a weighted graph, in which all the compounds are included, and each compound is assigned a weight equal to the number of reactions in which it participates. The simplest one ('unit weight') sets all node weights to one. The complex one ('compound degree weight') penalizes highly connected compounds by assigning each compound a weight equal to its degree, while setting each reaction to a weight of one. The result from shortest-pathfinding is also

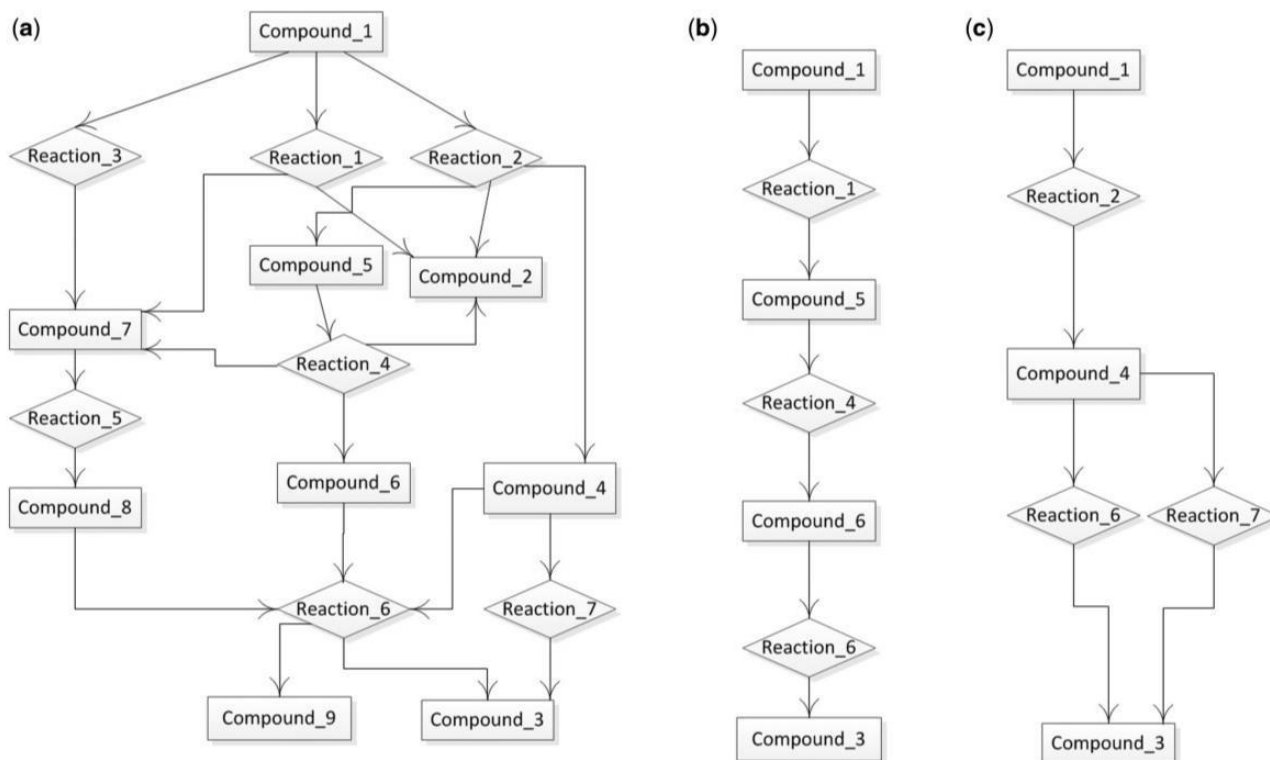


Figure 3. (A) A simple example of metabolic pathway for converting compound_1 'source' into compound_3 'goal'. (B) Shows a possible pathway to convert compound_1 into compound_3 and (C) is another possible way to reach the compound_3.

dependent on the weights associated with nodes or edges, which are modeled differently in various approaches [68]. The weights are assigned to the edges based on compound structure similarity [59]. In a degree-weighted graph representing a meta-bolic network [15], each node is assigned a weight equal to its degree. A weighted graph will reduce the probability of finding unfeasible biotransformation paths during the pathfinding process [80]. Recently, the weighted graph representation has all the compounds included in the graph, whereas the weight (cost) is associated with each compound equaling its connectivity in the entire metabolic network. Pathfinding algorithms will tend to avoid highly connected compounds whenever possible [81, 82].

Several researchers have proposed the use of metabolic pathfinding methods that use weighted atom maps [10, 20, 83–85]. In metabolic paths, at least one atom is transferred between adjacent metabolites and computed. Additionally, the edges are weighted according to the degree of metabolite nodes, to reduce the number of paths that traverse via high-connectivity metabolites [86, 87]. To cope with this problem, high-degree metabolites can be removed from the network, or edges of a metabolite graph can be weighted according to the degree of metabolite nodes, such that low-degree nodes are preferred [62, 68, 88].

Branched metabolic pathway

Branched pathways are the nonlinear pathways that can arrive at a target compound through combinations of pathways that split compounds into smaller ones, work in parallel with many compounds and join compounds into larger ones. The identification of branched pathways has a number of important applications in areas that require deeper understanding of metabolism, including metabolic engineering and drug target identification.

Furthermore, branched pathways enable the analysis of meta-bolic processes with a more comprehensive perspective as compared with the limited picture provided by linear pathways [89, 90]. However, pathfinding requires specifying a single start and a single end node. It cannot deal with branched pathways or with sets of query reactions. A more challenging question is to predict pathways from multiple seed nodes (e.g. reactions catalyzed by a cluster of co-expressed genes) by extracting the subnetwork that connects them best [20, 57, 62].

Several algorithms have been proposed to handle branched pathways, in a multi-genome scale, and metabolic data such as the KEGG RPAIR data set [91]. BPAT-M is a graph-based algorithm for identifying branched metabolic pathways [92]. This algorithm is based on two techniques; the first is the rapid search algorithm 'Linear Pathfinding with Atom Tracking', which can track across thousands of reactions and compounds from multiple species; and the second is Branched Pathfinding using Atom Tracking, 'BPATS', which is based on seed pathways [93]. The BPAT-M algorithms will perform better if all branches conserve at least the given number of atoms and are of similar length. In contrast, the algorithm does not perform well with all pathways such as the 'inosine monophosphate' pathway.

Metabolic pathway tools and systems

Metabolic pathway tools treat a genome as far more than a sequence and a set of annotations. Moreover, it links the molecular parts list of the cell to the genome, and to a carefully constructed web of functional interactions. The Pathway Tools ontology is defined as an extensive set of object attributes and object relations that allows a rich conceptualization of biology to be represented within a Pathway/Genome database (PGDB).

Table 1. Pathway tools and types of MODs

Tool	Task	Link Accessibility (URL)	Reference
PathFinder	Dynamically represents and provides visualization of biochemical information	http://bibiserv.TechFak.Uni-Bielefeld.DE/pathfinder	[95]
PathMiner	Identifies plausible routes using known biochemical transformations	http://pathminer.uchsc.edu/	[73]
Pathway Hunter Tool (PHT)	Analyzes the shortest paths and calculates the average shortest paths	http://www.pht.uni-koeln.de	[59, 65]
aMAZE	Web interface to the aMAZE relational database	http://www.amaze.ulb.ac.be	[96]
Pathway Prediction System (PPS)	Predicts microbial catabolism of organic compounds	http://umbdd.ahc.umn.edu/predict/	[97]
KEGG genes	Identifies the link between genomic information in the GENES database	http://www.genome.jp/kegg	[98]
MetaRoute	Explores genome-scale metabolic networks	http://www-bs.informatik.uni-tuebingen.de/Services/	[86]
KEGG pathway	Provides reference knowledge for pathway mapping	http://www.genome.jp/kegg/	[99]
Pathway Tools version 13.0	Allows the user to interrogate and explore relationships within the network	http://www.biocyc.org/download.shtml	[94]
Pathway projector	Provides intuitive browser pathway map with the addition of gene and enzyme nodes	http://www.g-language.org/PathwayProjector/	[100]
PathPred	Functions as knowledge-based prediction system	http://www.genome.jp/tools/pathpred/	[101]
Atom tracking system	Enables pathfinding algorithms to avoid unrealistic connections	http://www.kavrakilab.org/atommetanet	[93]
EcoCyc Database	Provides pathway/genome navigator software with the EcoCyc database	http://ecocyc.org/	[102]
MetaCyc Database	Provides a uniquely high-quality resource for metabolic pathways and enzymes	http://metacyc.org/	[103]

which is queried and manipulated by the user [94]. Pathway Tools provides a broad range of functionalities. It can manipulate genome data, metabolic networks and regulatory networks. For each data type, it provides query, visualization, editing and analysis functions. It also provides model-organism databases (MODs), development capabilities, editors who allow for refinement of a PGDB, web publishing and comparative analysis. A family of curated PGDBs has been developed using these tools for modeling important organisms. The software also provides visual tools for analysis of omics data sets, and tools for the analysis of biological networks. Table 1 shows the investigated pathway tools and the common types of MODs.

Evaluating pathfinding approaches

Evaluating pathfinding approaches to metabolic pathways can be hard, even for linear pathways, because there is no standard test set [93]. In other words, the effectiveness of any pathfinding approach is tested by seeing how well it performs with respect to a known metabolic pathway. If the source and goal compound and the entire metabolic network are given, how well does a specific pathfinding approach perform at navigating the reactions and compounds involved in a known metabolic path or pathway? Generally, by using benchmarking metrics functions commonly used for computed path.

When we use a particular pathfinding approach, it is necessary to compare the results with other methods or other works. Thus, we need some measurement to evaluate the accuracy of metabolic pathways. Here, we present some criteria frequently used by researchers for comparison [14, 15, 20, 86]. These criteria are used to compare algorithm results with the ground truth labeling, to define the following corresponding values which indicate, numerically, correspondence between the computed path and the metabolic path. Here, we introduce some criteria

to measure the degree of correspondence between any computed path and metabolic path:

- True Positives (TP), in which the total number of metabolic path of reactions and compounds are found (except for source and target nodes whether reaction or compound are not considered).
- False Negatives (FN), signifies the total number of computed path found for number of reactions and compounds.
- False Positives (FP), signifies the total number of reactions and compounds found in the computed path that are not in the metabolic path.

For each pathway, measurements found previously in the literature are used to calculate the

- Sensitivity (S_n) $\frac{1}{4} TP / (TP \cup FN)$, which is the fraction of the reactions and compounds in the metabolic path,
- Positive Predictive Value (PPV) $\frac{1}{4} TP / (TP \cup FP)$ and
- Accuracy (Ac) $\frac{1}{4} (S_n \cup PPV) / 2$

The above measurement criteria are used to compare the computed path (by pathfinding approach) and the metabolic path or pathway. Next to these criteria, we must take into account the execution time and the memory overhead for pathfinding approaches. Table 2 shows the summary results for pathfinding approaches in different databases. The most common data set that has been used frequently by researchers is the KEGG network. For each of A* (A-star) search, breadth-first search (BFS) and depth-first search (DFS), heuristic search algorithms have been used to predict metabolic pathways that are based on a biochemical state-space. The results show that using these algorithms always produces biochemical paths that are optimal in terms of the heuristic. Recently, DFS search strategy was used to generate EFMs, where it shows the scalability, low memory overhead, a CPU-limited problem and can incorporate additional flux constraints to generate a full subset of EFMs of interest. Another approach of pathfinding is k-shortest

Table 2. Summarizing results for pathfinding approaches

Algorithm	Operating system	Year	Time		Worst performance	Average (Best)		Accuracy	Data set	Reference
			Best performance	Time		Sn	PPV			
3A*Linux7. operating system.		2003	831. ms		906. ms	—	—	—	KEGG network	[73]
BFS	Sony PCG-C1MW laptop.		6. ms/76		19. ms/42	—	—	—		
DFS	Transmeta CrusoeTM5800 Processor.		1. ms/64		104 ms>	—	—	—		
384 MB of main memory.										
DFS	—	2006	—		—	2%92.	1%95.	Most accurate with EcoCyc 7%pathways(weightedgraph)93.	KEGG and EcoCyc networks	[15]
k-shortest path	—	2009	—		—	100%	100%	Reaction-reaction for 10-k paths 100%	Escherichia coli	[14]
						46%	77%	Compound-compound for 10-k paths 62%		
BPAT-M	XML representations of the KEGG	2011	4 min		33 min	—	—	—	KEGG	[91]
BPAT-S	Single core from a 2. GHz/83		200 min>		600 min>	—	—	—		
ReTrace	Intel Xeon E5440 with access		40 min		300 min>	—	—	—		
to 16 GB of RAM										
Branch-and-Bound	18. version of Pathway Tools0	2014	0. s3		3. s6	—	—	—	EcoCyc and MetaCyc version 17.5	[79]
2. GHz computer:3										
DFS	Linux OS	2014	310 s		5000 s	—	—	—	Efmtool EFNs	[75]
Intel Core i7 860										
93Processor2. GHz										
RAM 8 GB										
MATLAB (R2011a)										
6 weighting schemes		2014	40 min		—	—	—	—	KEGG	[104]

path, where ‘shortest path’ is interpreted as minimizing the number of arcs (reactions) involved in the path, and k refers to the number of shortest paths; for instance, $k = 1$ corresponds to the shortest path, $k = 2$ corresponds to the second shortest and $k = 3$ to the third shortest path, etc. Giving weights to a metabolic graph can reflect various kinetic and thermo-dynamic parameters.

Discussion

Pathfinding-based distance metric

Finding shortest paths in metabolic pathways constitutes a considerable advance with respect to stoichiometric approaches. In genome-scale metabolic networks, k -shortest path is a well-known graph theory problem for computational tracking in metabolic networks. The most suitable distance metric will determine the computed k -shortest paths instead of computing all paths because not all computed paths will have biological significance. Because analysis of the computed paths becomes simpler, k is usually restricted to a small number to determine biologically meaningful metabolic paths; thus, the distance metric appears to be the most effective metric presented to date [15, 80]. The found paths are implicitly and completely determined by the distance metric adopted, thus having biological significance.

One major drawback of pathfinding approaches is that they are relatively inflexible in terms of adding additional biologically meaningful constraints. Currently, for instance, extracting stoichiometric information for a metabolic path must be done as a separate stage (e.g. by balancing intermediate compounds in the path) once the path has been computed without using stoichiometric information. Being able to add biologically-based constraints (e.g. stoichiometric, regulatory [105], topological or energetic [106]) as an intrinsic part of the pathfinding process would significantly refine the search for biologically meaningful metabolic paths, provided this can be done without excessively complicating the algorithmic/computational expense of finding k -shortest paths.

Metabolic pathfinding limitation

A limitation of metabolic pathfinding in the graph-theoretical setting is that all metabolites are by default considered equal in importance. Many currency and cofactor metabolites appear in a large number of reactions, constituting a large fraction of high-degree metabolites in a typical metabolic network. Because of their high degree of connectivity, a random shortest path traverses through such a metabolite with a high probability. However, in many cases, the biological relevance of such a path is low. For instance, almost all functionally dissimilar parts of metabolism can be connected with short paths using adenosine triphosphate as an intermediate. To cope with this problem, high-degree metabolites can be removed from the network or edges of a metabolite graph can be weighted according to the degree of metabolite nodes, such that low-degree nodes are preferred [80]. However, non-cofactor metabolites with a high degree, such as pyruvate, then become a challenge to metabolic pathfinding. Indeed, deciding a suitable set of cofactor metabolites is a nontrivial problem, depending on the modeling task [107].

Several pathfinding algorithms are not efficient, such as A*, BFS and DFS (backtracking). For example, they either have a large overhead, yield far from optimal paths, do not

easily scale up to many cores or are cache unfriendly. Therefore, in recent years, many researchers have proposed several new algorithms to solve these weaknesses of previous algorithms. Algorithms such as Jump point Search [108, 109] and Sub [110] are high-performance algorithms in terms of time and memory overhead complexities, and they can provide optimality paths (shortest paths). Finally, an important topic of metabolic path-finding is further refinement of the approach and integration with other techniques, which is a useful methodology. For better results in the future, we suggest using these algorithms or new algorithms for biological purposes such as metabolic pathways.

Conclusion and future works

In this article, we have described stoichiometric and pathfinding approaches that are related with metabolic pathways. Notwithstanding that stoichiometric approaches have a theoretical basis, FBA, EFMs and EPs face many difficulties from both the computational and analytic points of view when applied to large-scale experimental data for metabolic biology pathways. Contrary to stoichiometric approaches, pathfinding approaches do enable analysis of genome-scale metabolic networks to be performed. We believe the key research challenges are choice of an appropriate distance metric and addition of biologically based constraints. We would emphasize here that pathways produced by any mathematical/computational approach need a clear validation with experimentally determined metabolic pathways from the bio-chemical literature. Being better able to model mathematically metabolic pathways will help in the metabolic engineering of organisms to create (currently) unknown, novel pathways useful for biotechnological or biomedical purposes.

Most importantly, each algorithm should guarantee the optimality of the routes found when the cost of the atoms is lost in the routes as a part of the optimality criteria. Future work should take into account the symmetry of compounds for atom mappings, where the atoms lost and conserved in routes are more precisely tracked. In addition, any pathfinding algorithm should consider the cost of side compounds, the toxicity of some of the metabolites produced and the taxonomic range of the new enzymes introduced in routes. Another worthy re-search topic of metabolic pathfinding in the near future is to find optimal routes from multiple start compounds, and to identify more complex multiple target compounds because the possible candidate solutions are no longer linear routes but multiple linear routes merged together.

Key points

- A computational problem in metabolic engineering is finding efficient metabolic routes from a source to a target compound in genome-scale reaction networks.
- There exist a multitude of tools freely available for metabolic pathway analysis.
- The article clearly reviews stoichiometric approaches, graph theory and pathfinding approaches to metabolic pathways.
- Pathfinding approaches use shortest path and k-shortest path concepts.
- Stoichiometric approaches involve FBA, EFMs and EPs.

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